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LAWRENCE BERKELEY NATIONAL LABORATORY  
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# Low- $x$ QCD dynamics probed by multijets at HERA

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*on behalf of the*  
H1 and ZEUS Collaborations

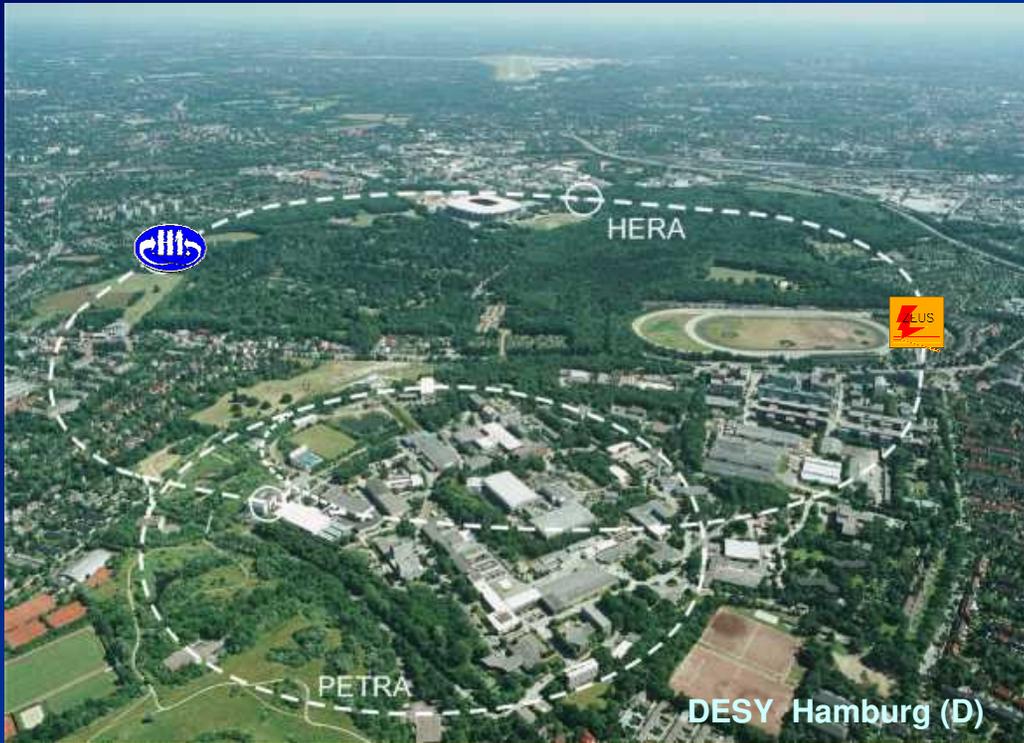


## Outline:

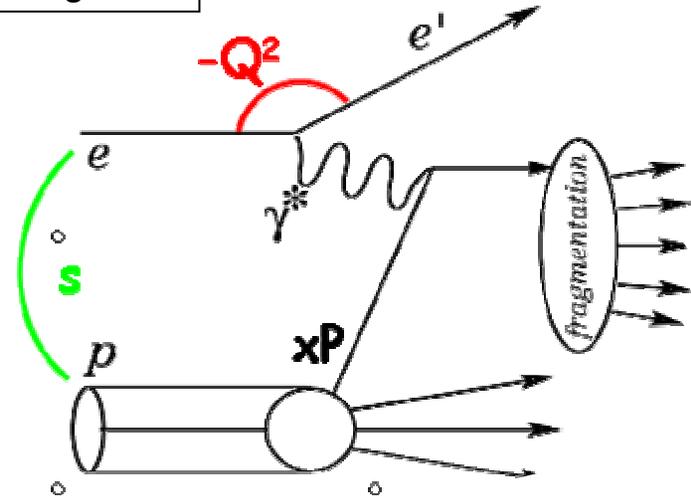
- Introduction
- Multijet production at low- $x$  in DIS
- Angular correlation between jets
- Forward jets
- Three and four-jet final states in PHP
- Summary and Outlook



# $e^\pm p$ scattering at HERA



Leading Order



$\sqrt{s}$  = 300-318 GeV (Energy C.M.)

$Q^2$  = Photon Virtuality

$X_{Bj}$  = energy carried by the struck parton in the proton

## HERA (1992-2007)

- 820-920 GeV  $p \rightarrow \leftarrow 27$  GeV  $e^\pm$
- 2001 HERA II Lumi upgrade + polarised  $e^\pm$
- Machine operation ended in June 2007
- About  $0.5 \text{ fb}^{-1}$  per experiment collected

## $Q^2$ (photon virtuality):

- $Q^2 \sim 0$  ( $< 1 \text{ GeV}^2$ )  $\rightarrow$  Photoproduction: photon-proton scattering
- $Q^2 > 1 \text{ GeV}^2$   $\rightarrow$  Deep Inelastic Scattering (DIS), probing the proton structure

# Parton Dynamics at low $x$ in $e^\pm p$ collisions

*Different approximations to the summation of the perturbative expansion of parton evolution*

## ■ DGLAP $\Sigma(\alpha_s \ln Q^2)^n$

- strong ordering in virtuality, i.e.  $k_{t,1}^2 \ll k_{t,2}^2 \ll \dots \ll Q^2$
- weak ordering in  $x$ , i.e.  $x_1 > x_2 > \dots > x_{Bj}$
- works very well at large  $Q^2$
- expected to fail at low  $Q^2$  and  $x$

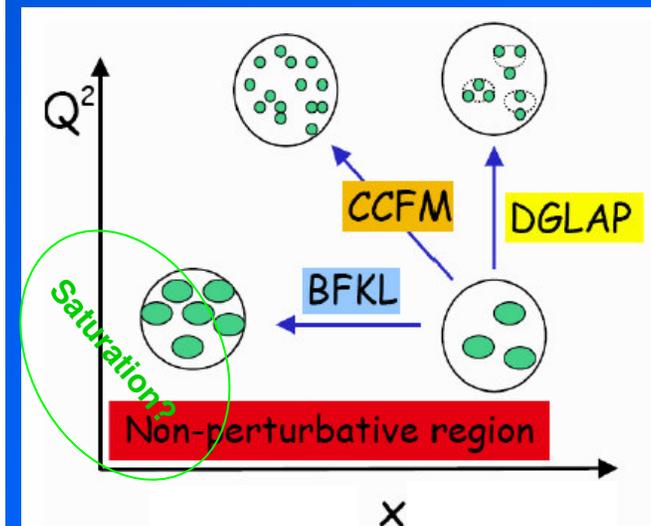
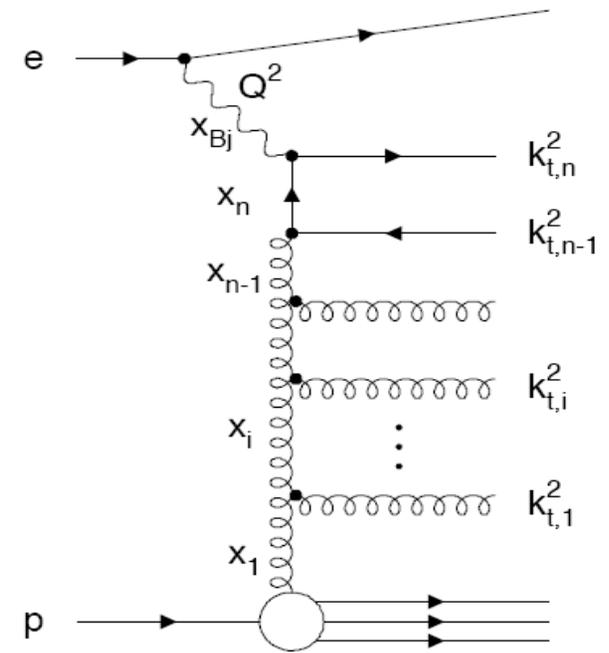
## ■ BFKL $\Sigma(\alpha_s \ln 1/x)^n$

- random walk in  $k_t$
- strong ordering in  $x$ , i.e.  $x_1 \gg x_2 \gg \dots \gg x_{Bj}$
- expected to work well at low  $x$

## ■ CCFM $\alpha_s \ln Q^2$ & $\alpha_s \ln 1/x$

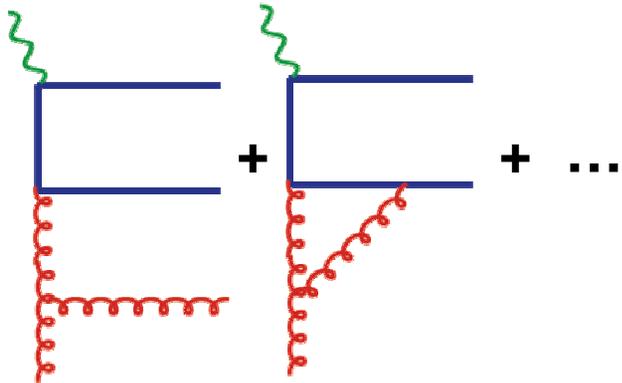
- angular ordering, i.e.  $\theta_1 \ll \theta_2 \ll \dots \ll \theta_n$
- expected to work at high  $Q^2$  and low  $Q^2$  and  $x$

➔ DGLAP well established at HERA (PDFs QCD fits,  $F_2$ ). Look at measurements with better sensitivity to BFKL effects ...



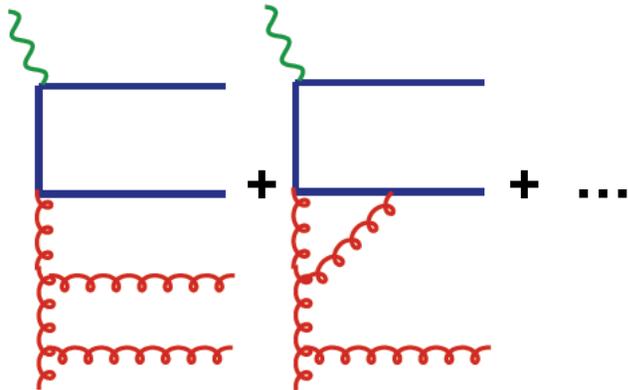
# NLO QCD calculations and Monte Carlo Models

Disent, NLOjet++



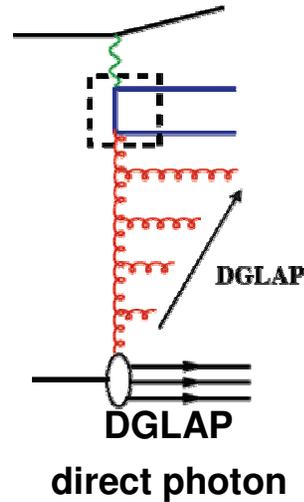
NLO Di-jet ( $\alpha_s^2$ )

NLOjet++

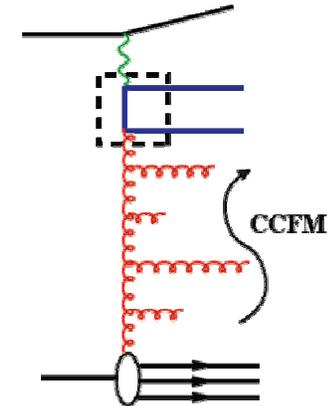


NLO Tri-jet ( $\alpha_s^3$ )

Lepto/Rapgap

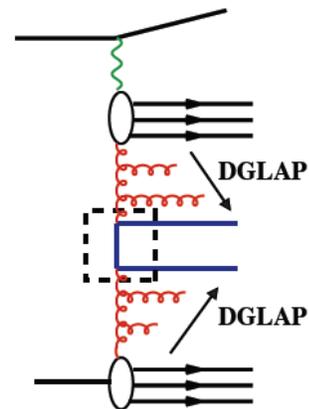


Cascade



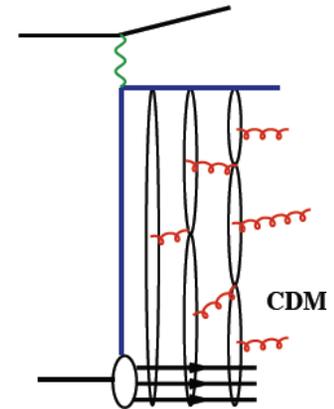
CCFM, angular ordering,  
Unintegrated  $g(x, kt, \mu)$

Rapgap



DGLAP, direct +  
resolved photon

Ariadne/DjangoH



Color Dipole Model  
No  $k_t$  ordered partons

# Multijet at low x

H1-prelim-06-034

H1 99-00 data (44 pb<sup>-1</sup>):

DIS:  $4 < Q^2 < 80 \text{ GeV}^2$ ;

$10^{-4} < x_{Bj} < 10^{-2}$

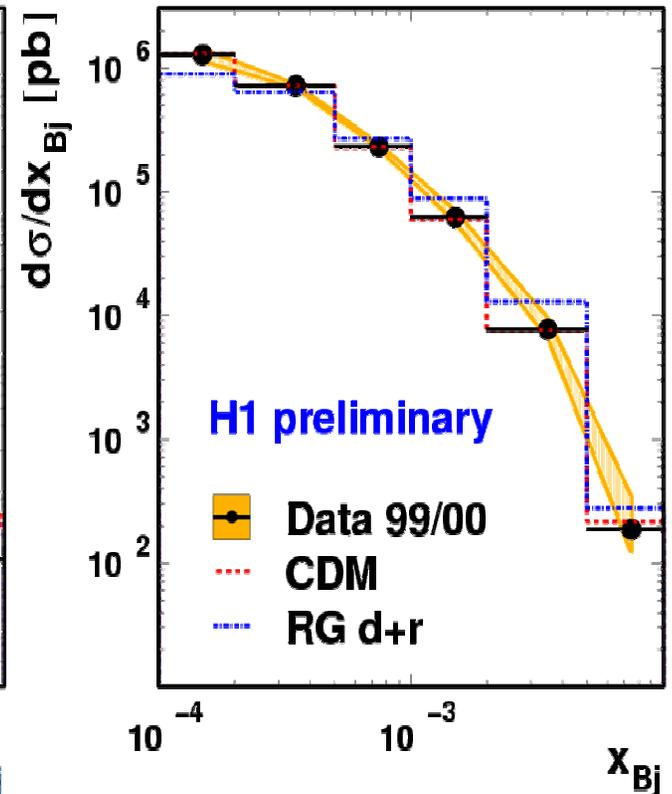
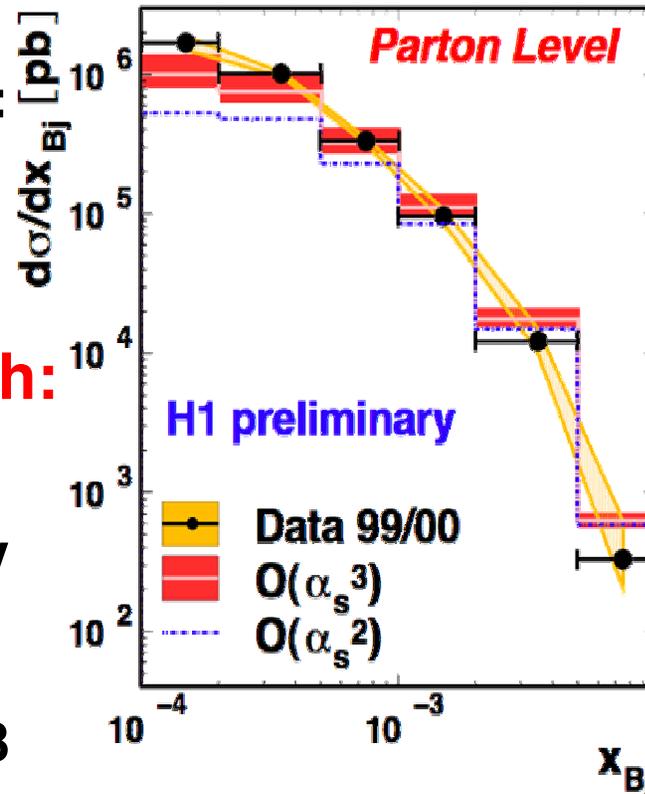
**At least 3 jets with:**

$E_{T \text{ jet1}} > 4 \text{ GeV}$  ;

$E_{T \text{ jet2}} + E_{T \text{ jet3}} > 9 \text{ GeV}$

$-1 < \eta^{\text{lab}} < 2.5$ ;

one jet  $-1 < \eta^{\text{lab}} < 1.3$



- NLOjet++  $O(\alpha_s^3)$  gives very good description of the data (with possibly the exception at very low-x)
- CDM (DjangoH) gives also a good description
- Rapgap (Dir+Res) description not as good

# Multijet at low x

DESY-07-062

ZEUS 98-00 data (82 pb<sup>-1</sup>):

DIS:  $10 < Q^2 < 100 \text{ GeV}^2$

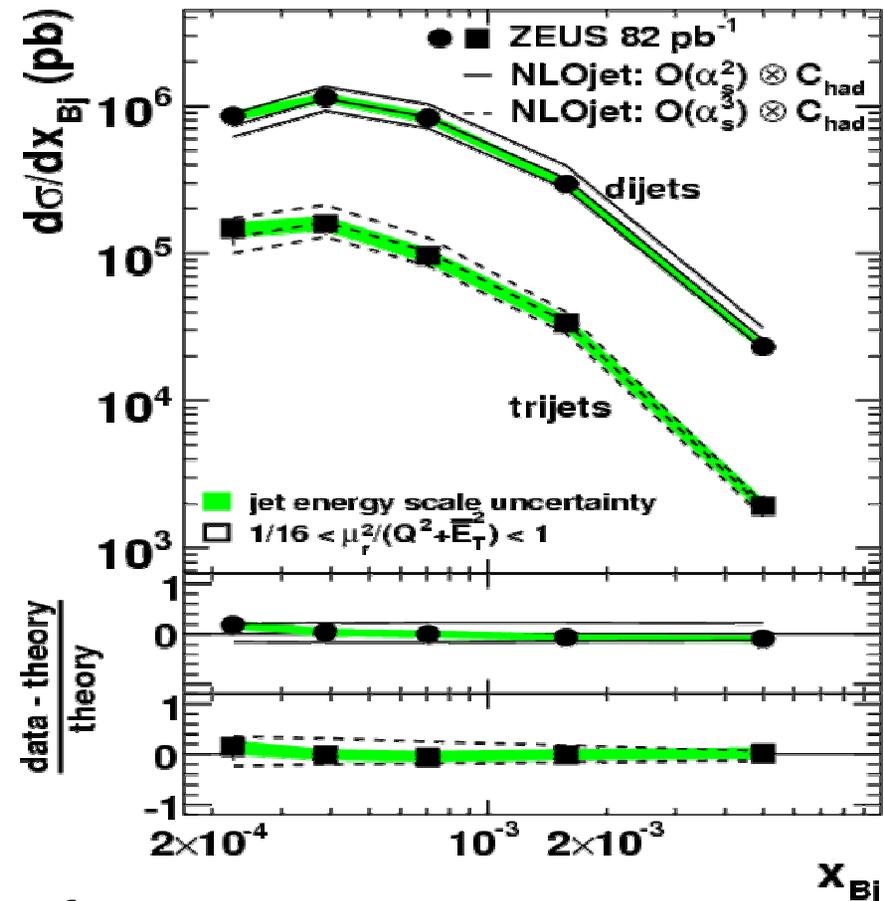
$10^{-4} < x_{Bj} < 10^{-2}$

**2 or 3 jets with:**

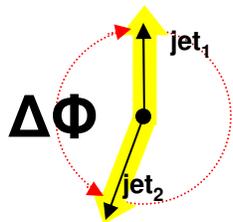
$E_t^{\text{jet1}} > 7 \text{ GeV}$  ;

$E_t^{\text{jet2(3)}} > 5 \text{ GeV}$

$-1 < \eta^{\text{lab}} < 2.5$



Look in the Hadronic Center of Mass frame:

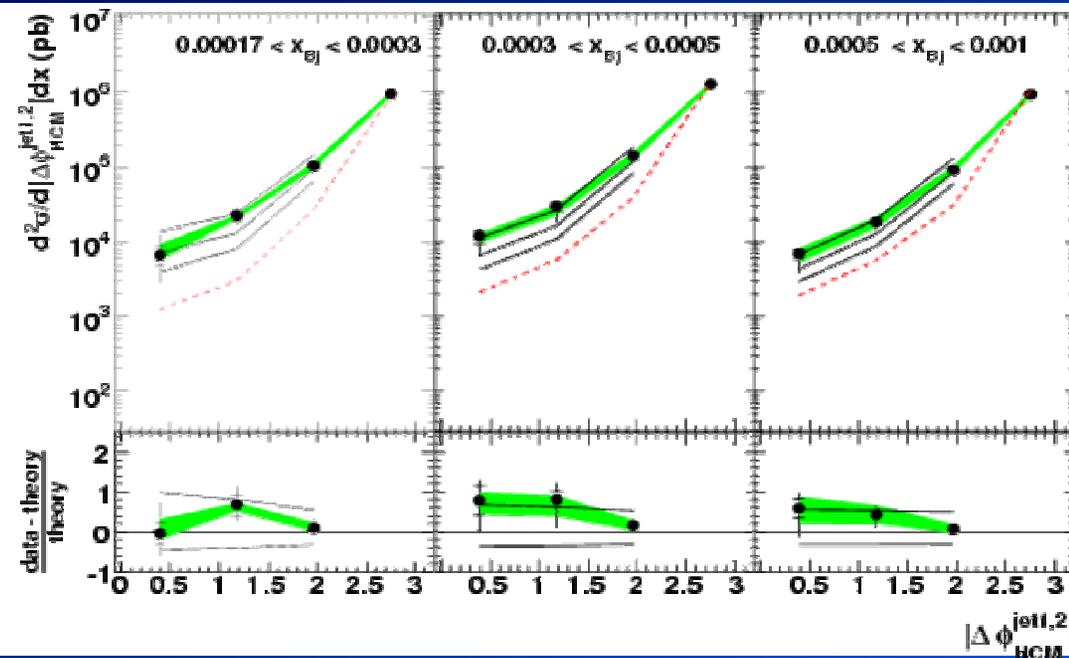


$|\Delta\Phi^{\text{jet1,2}}_{T,\text{HCM}}| =$  azimuthal separation between the two jets with the highest hadronic center of mass  $E_T$



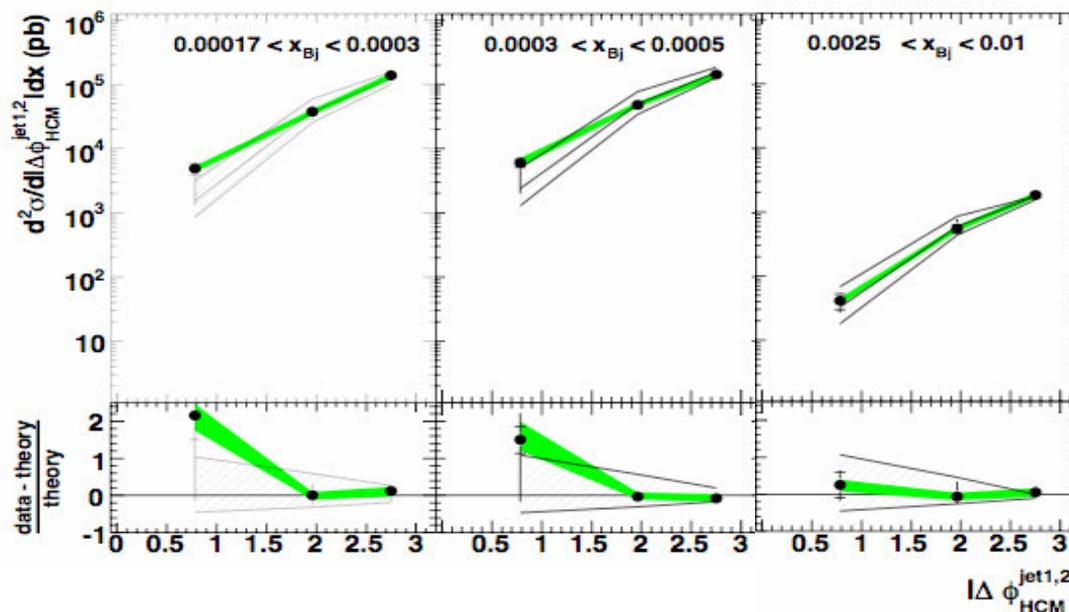
# Multijet at low x

DESY-07-062



- ZEUS 82 pb<sup>-1</sup> dijets
- NLOjet:  $O(\alpha_s^2) \otimes C_{had}$
- NLOjet:  $O(\alpha_s^3) \otimes C_{had}$
- jet energy scale uncertainty
- ▨  $1/16 < \mu_r^2 / (Q^2 + E_T^2) < 1$

Description much improved  $O(\alpha_s^2) \rightarrow O(\alpha_s^3)$

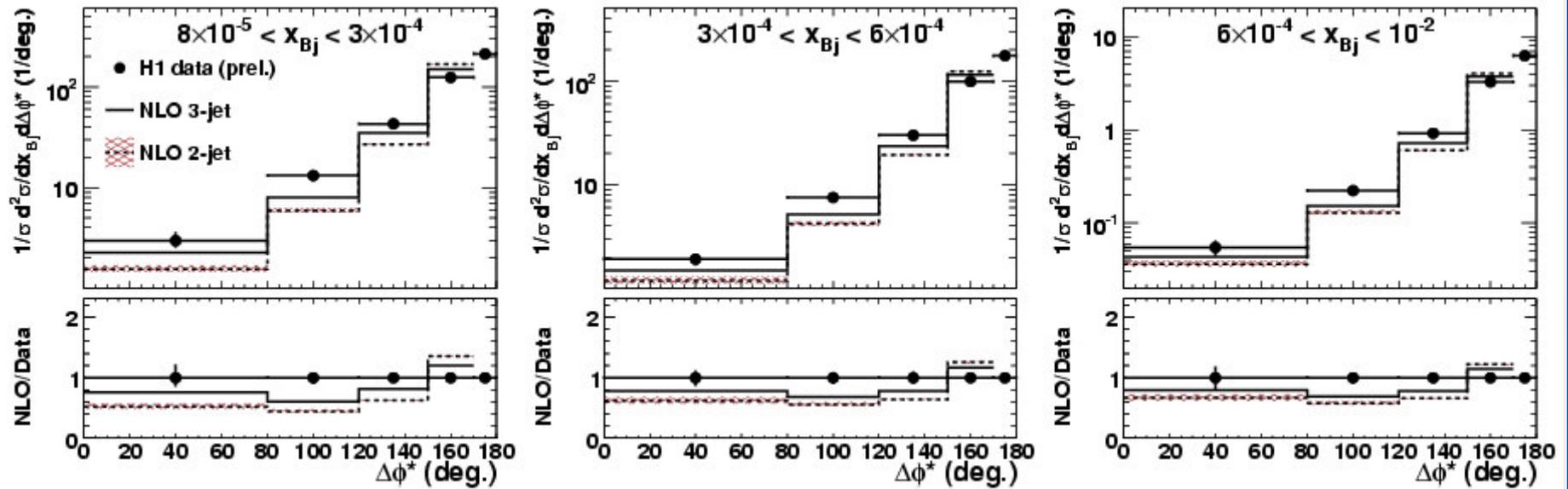


- ZEUS 82 pb<sup>-1</sup> trijets
- NLOjet:  $O(\alpha_s^3) \otimes C_{had}$
- jet energy scale uncertainty
- ▨  $1/16 < \mu_r^2 / (Q^2 + E_T^2) < 1$

Data overall well described by pQCD

# Azimuthal Correlations in Dijets

H1-prelim-06-032



H1 99-00 data (64 pb<sup>-1</sup>):

DIS:  $5 < Q^2 < 100 \text{ GeV}^2$

**2 Jets with:**

$-1 < \eta_{\text{jet}} < 2.5$  (LAB)

$E^*_{Tj} > 5 \text{ GeV}$  (HCM)

- Phase space extended toward lowest  $Q^2$  and  $x_{Bj}$

- One-parton-radiation (NLO 2-jet) not enough to describe data

- Two-parton-radiation (NLO 3-jet) systematically low for  $\Delta\phi^* < 150^\circ$

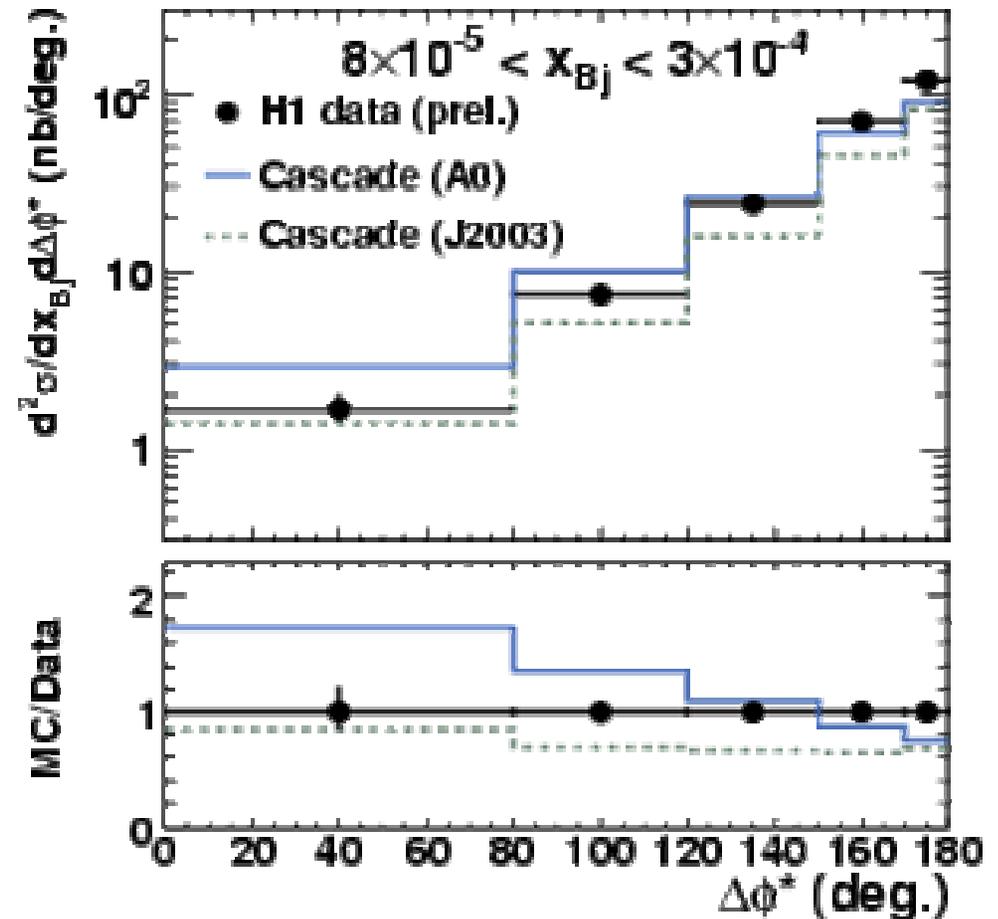
# Azimuthal Correlations in Dijets

H1-prelim-06-032

## Monte Carlo Models:

- Cascade (J2003) describes data reasonably well except in lowest  $x_{Bj}$  bin
- Cascade (A0) fails in all  $x_{Bj}$  bins. A0 has too hard  $k_T$  spectrum

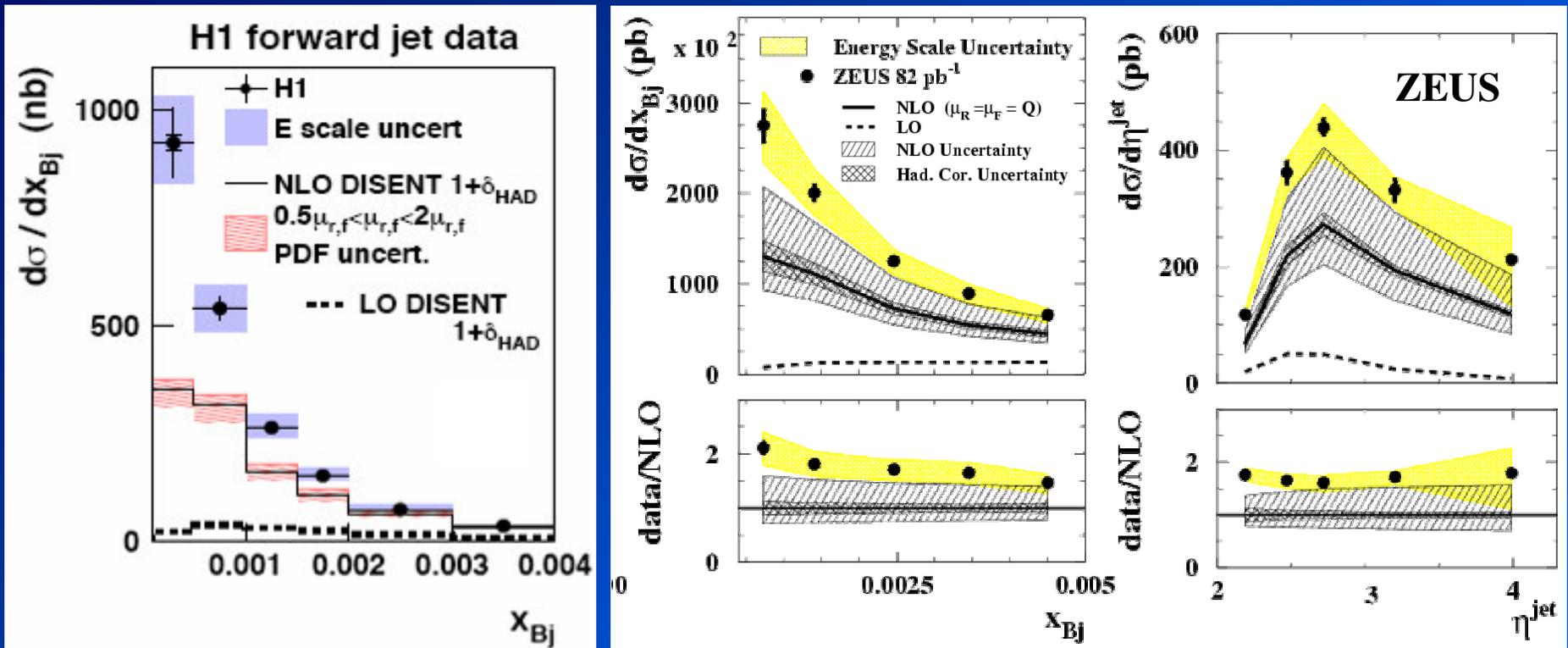
→ Data show sensitivity to the unintegrated gluon density



# Forward Jets

Eur. Phys. J. C46 (2006) 27

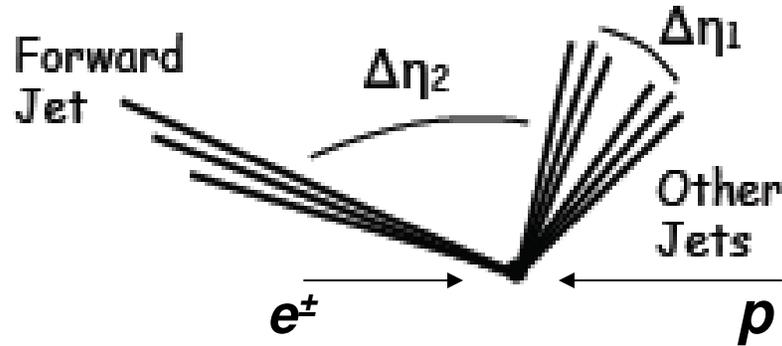
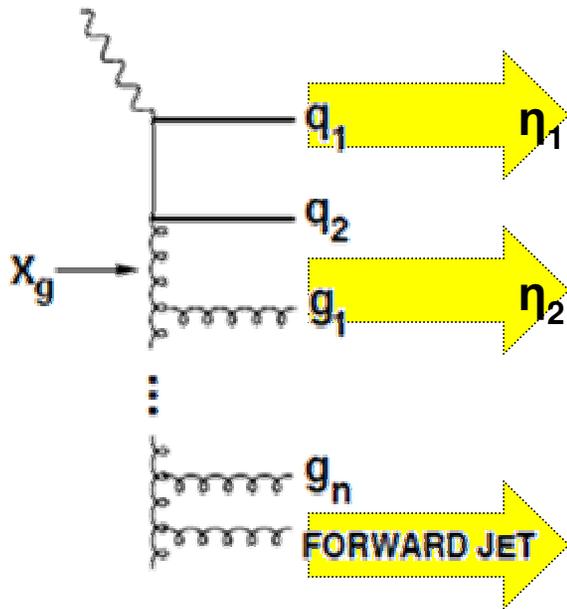
ZEUS: DESY-07-102



- New measurement ZEUS 98-00 data:  $2 < \eta_{jet} < 4.3$  (FwdPlugCal)
  - DIS:  $20 < Q^2 < 100 \text{ GeV}^2$  ;  $10^{-4} < x_{Bj} < 5 \times 10^{-3}$  ;
  - $x_{jet} > 0.036$  → Enhance BFKL expected behaviour
- LO-DGLAP fails completely
- NLO-DGLAP well below data at low  $x$  (as seen by H1)

# Forward jet & dijet

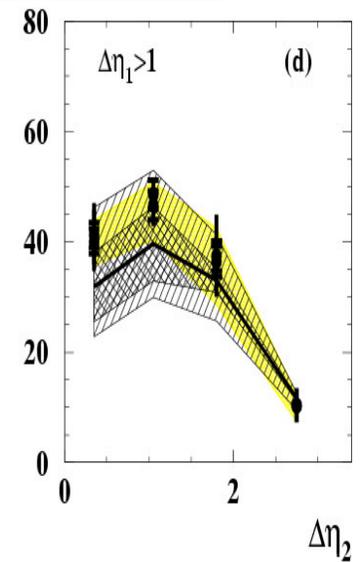
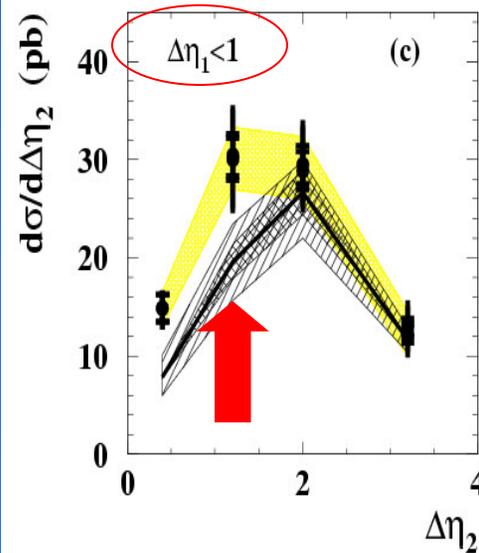
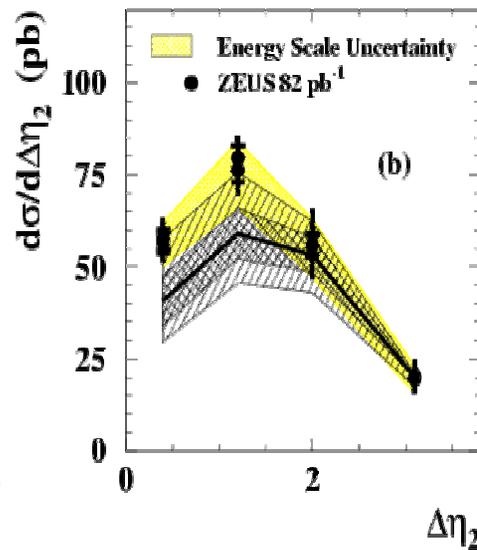
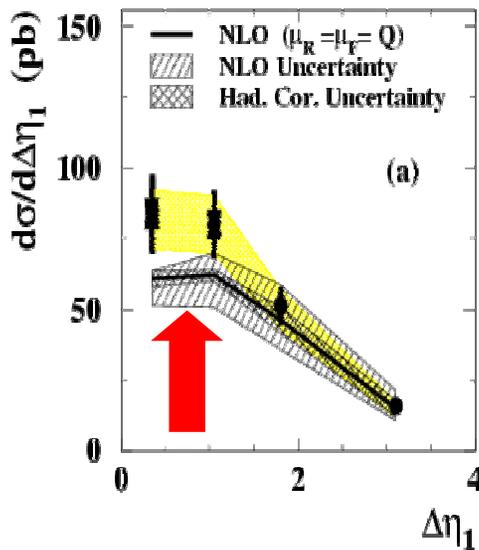
DESY-07-102



$$\Delta\eta_1 = \eta_2 - \eta_1$$

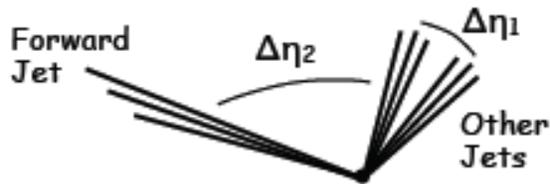
$$\Delta\eta_2 = \eta_{\text{fwd}} - \eta_2$$

- Discrepancy at low  $\Delta\eta_1$  and  $\Delta\eta_2$ , i.e. when all 3 jets tend to go forward
- Need for additional higher orders or BFKL resummation



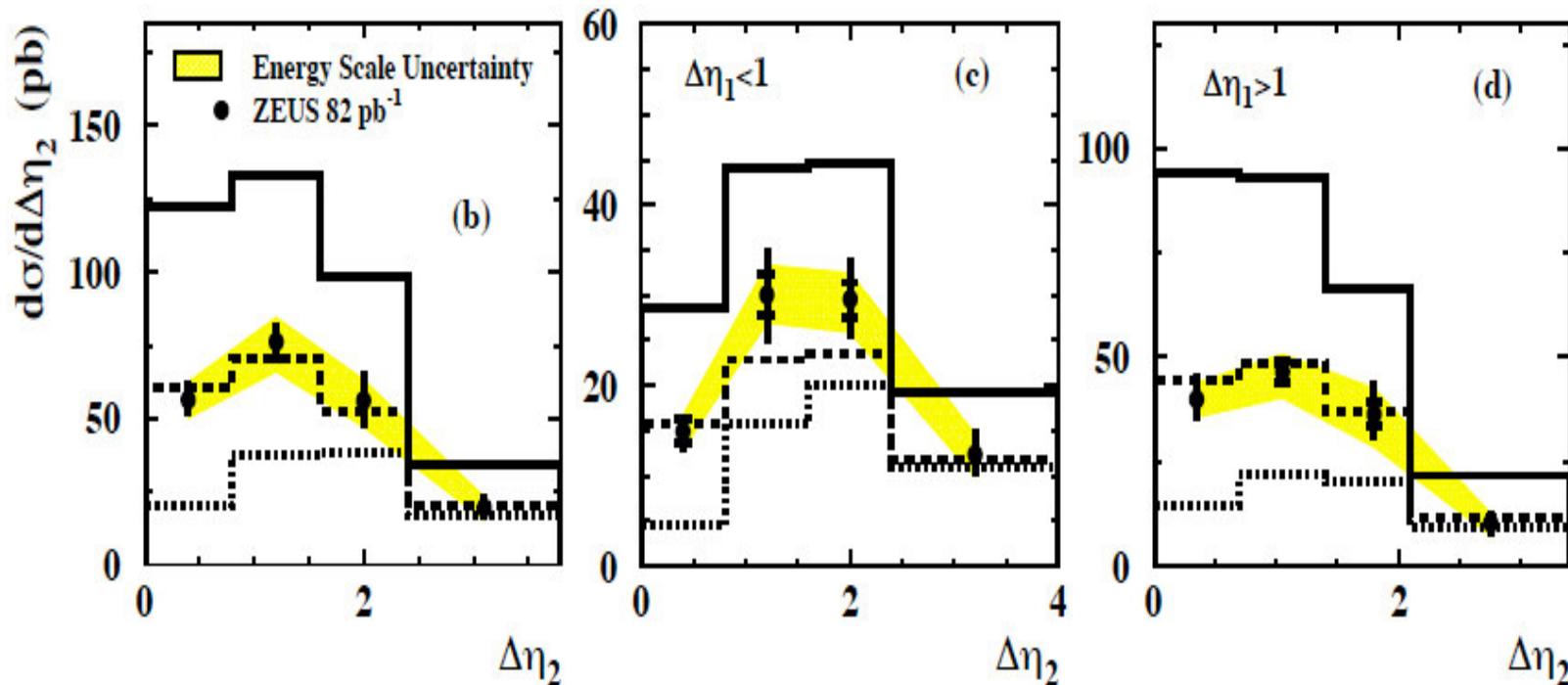
# Forward Jets & dijet: QCD Models

DESY-07-102



## ZEUS

— ARIADNE  
- - - ARIADNE (tuned)  
⋯ LEPTO



- CDM (Ariadne tuned) describes data reasonably well
- The breaking of  $k_T$  ordering is best modeled by CDM

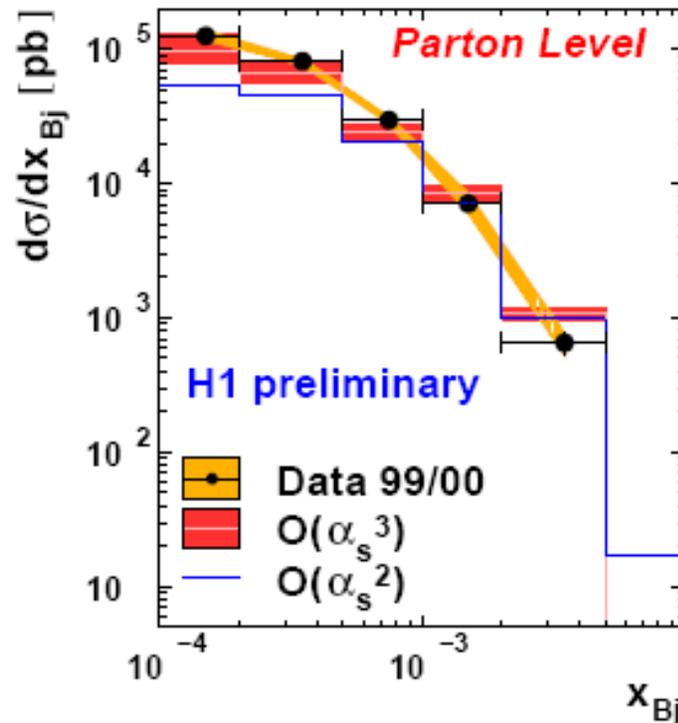
# Exclusive Trijets in DIS

H1-prelim-06-034

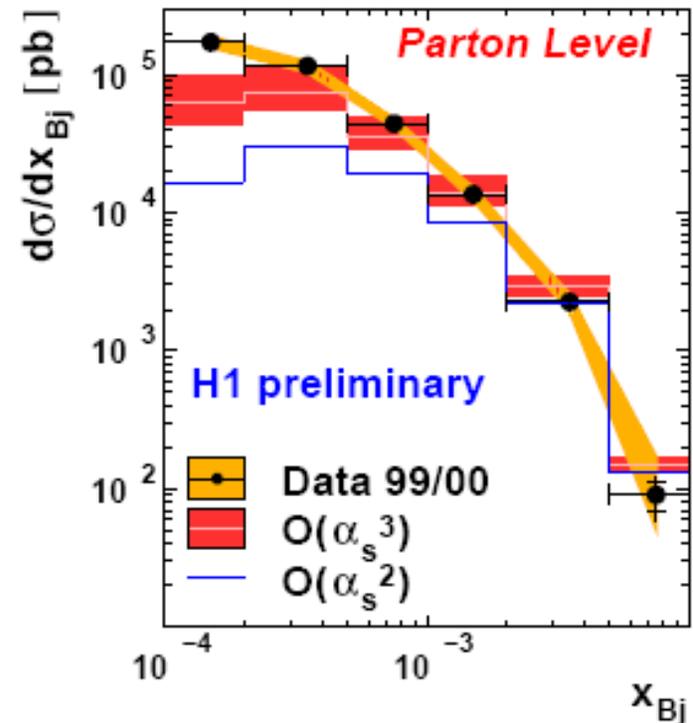
## 3 jets:

- Forward  
 $\eta_{\text{jet}} > 1$
- Central:  
 $-1 < \eta_{\text{jet}} < 1$

1 fwd & 2 central jets

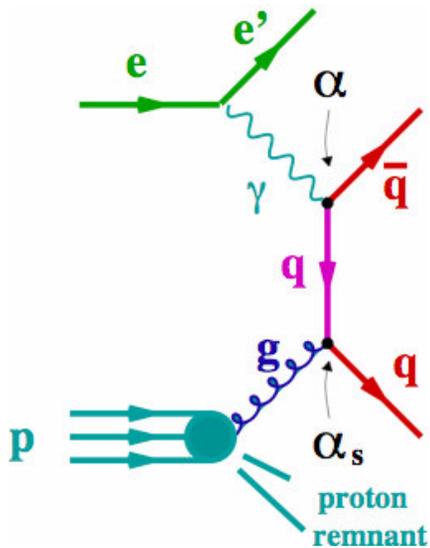


2 fwd & 1 central jets

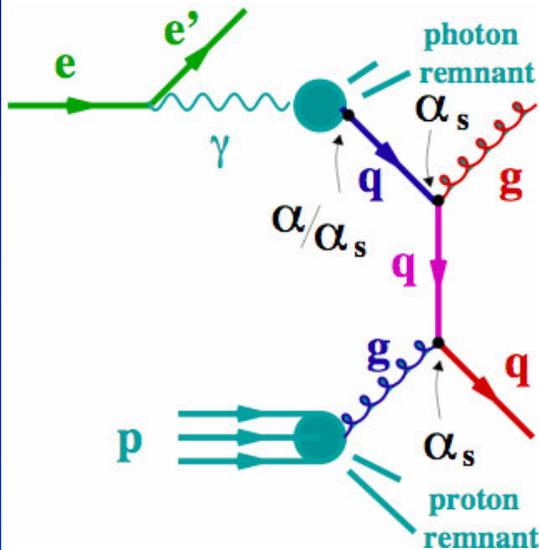


- 2 fwd-jets → mainly due to gluons according to MC studies (CDM)
- discrepancy at lowest  $x_{Bj}$  due to unordered gluon emissions? (NLO also below data for forward  $\eta$ )

# Multijets in Photoproduction



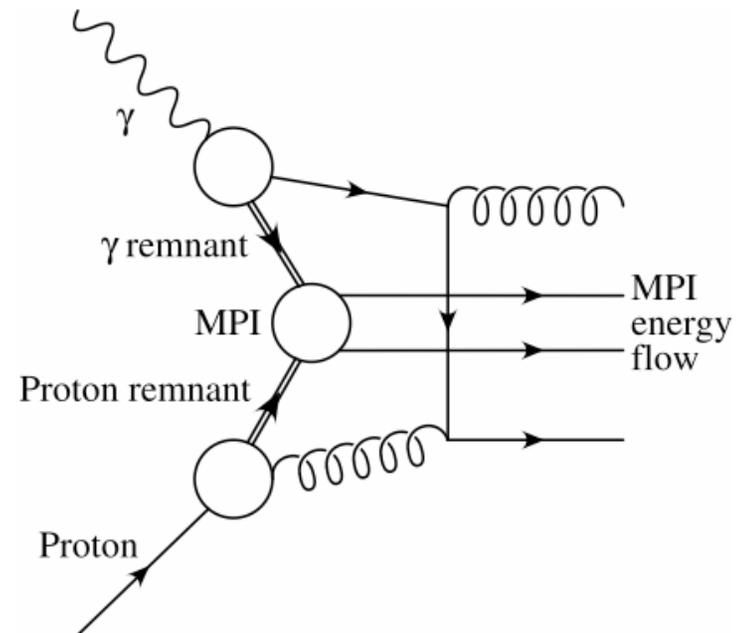
**Direct Photon**  
( $x_\gamma=1$ )



**Resolved Photon**  
( $x_\gamma < 1$ )

## Multi-Parton Interactions (MPI)

- Multijet photoproduction (**resolved  $\gamma$** ) sensitive to MPIs
- 4-jet PHP: the highest order process ever measured at HERA
- No NLO calculation available yet



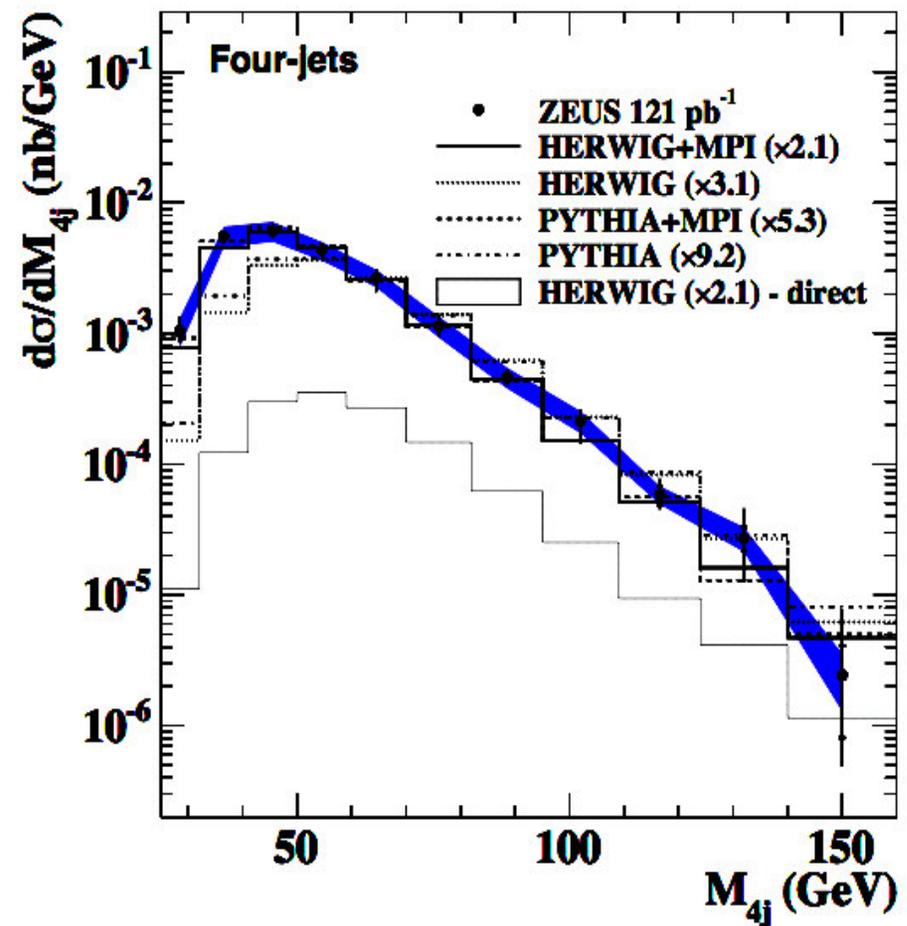
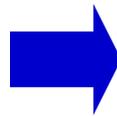
# Multijets in Photoproduction

DESY-07-100

ZEUS HERA I data ( $121\text{pb}^{-1}$ )

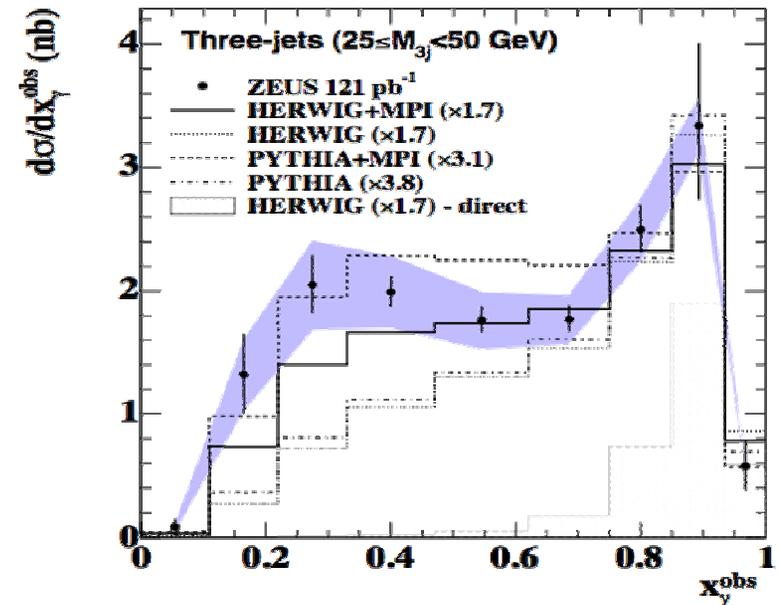
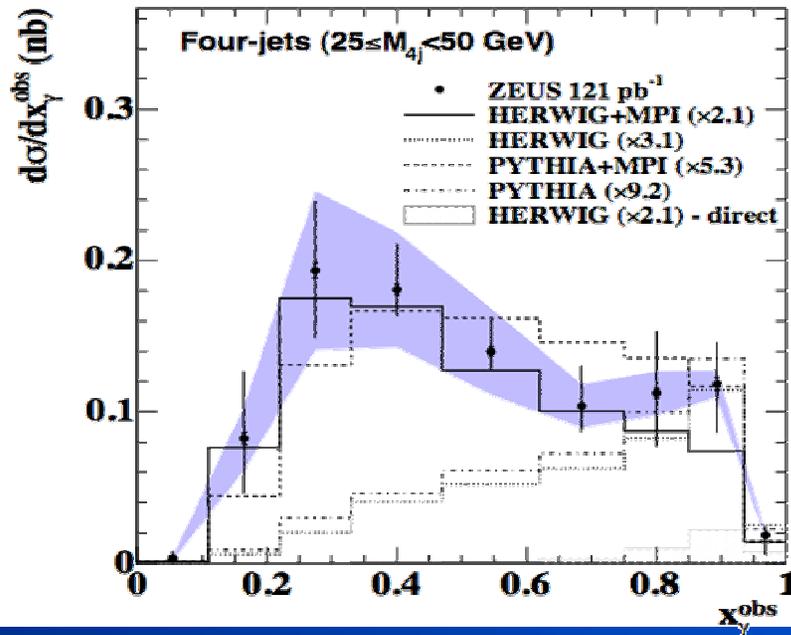
Event selection:

- Photoproduction  
 $Q^2 < 1 \text{ GeV}^2$
- 3 or 4 jets with  
 $|\eta| < 2.4; E_T > 6 \text{ GeV}$
- Good statistics of  
3- and 4-jet events

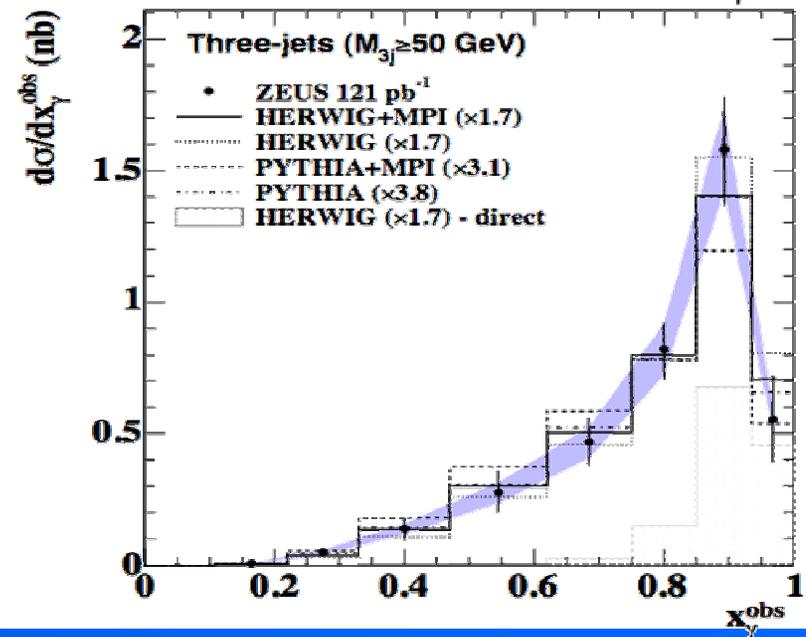


# Multijets in Photoproduction

DESY-07-100



- Two mass regions:
  - $25 \leq M_{nj} \leq 50$  GeV
  - $M_{nj} \geq 50$  GeV
- Low Mass more sensitive to MPIs (resolved photon)
- ➔ General improvement adding MPIs to LO MC



# Conclusions and Outlook

- HERA provides a versatile testing ground for pQCD
- Multi- and forward- jets production has been measured in the region  $x_{BJ} \sim 10^{-4}$  and low  $Q^2$  where NLO DGLAP pQCD is expected to fail
- Agreement between data and QCD calculations well improved when going from  $O(\alpha_s^2)$  to  $O(\alpha_s^3)$ . Nevertheless BFKL enhanced forward jet data at low  $x_{Bj}$  are not described by NLO
- CDM as implemented in Ariadne (tuned) provides a good description of most datasets
- Cascade (CCFM) with currently used sets of unintegrated gluon densities fails to describe shape of most distributions; these data could be used to determine the unintegrated gluon distributions.
- Multijet photoproduction data are better described adding Multi-Particle-Interactions to LO Monte Carlos
- HERA data will push further development of the Monte Carlo Models and hopefully stimulate NNLO DGLAP and NLO BFKL calculations
- More precise results expected with the full statistics of HERA  $O(1 \text{ fb}^{-1})$