

# Event-by-Event Average $p_T$ Fluctuations in $s_{NN}=200$ GeV Au+Au and p+p Collisions in PHENIX: Measurements and Jet Contribution Simulations

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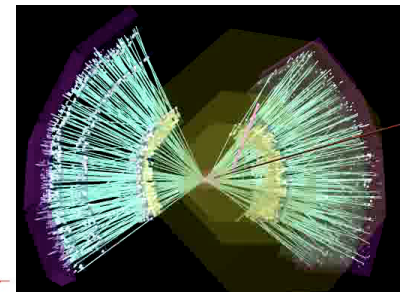
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M. J. Tannenbaum



QuarkMatter2004

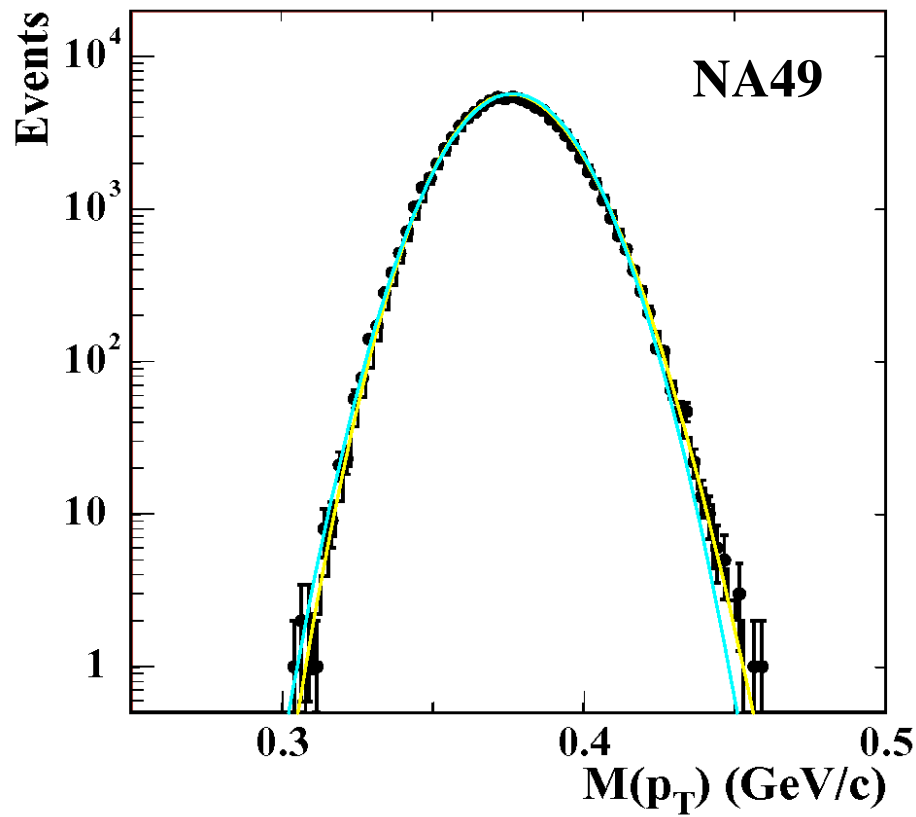


# The Event by Event Average $p_T$ ( $M_{p_T}$ ) Distribution is not a gaussian, it's a gamma distribution!

- DEFINITION

$$M_{p_T} = \overline{p_T(n)} = \frac{1}{n} \sum_{i=1}^n p_{T_i} = \frac{1}{n} E_{Tc} \quad \text{for events with } n \text{ particles.}$$

- For statistically independent emission (the sum of independent  $p_{T_i}$ ) □ analytical formula

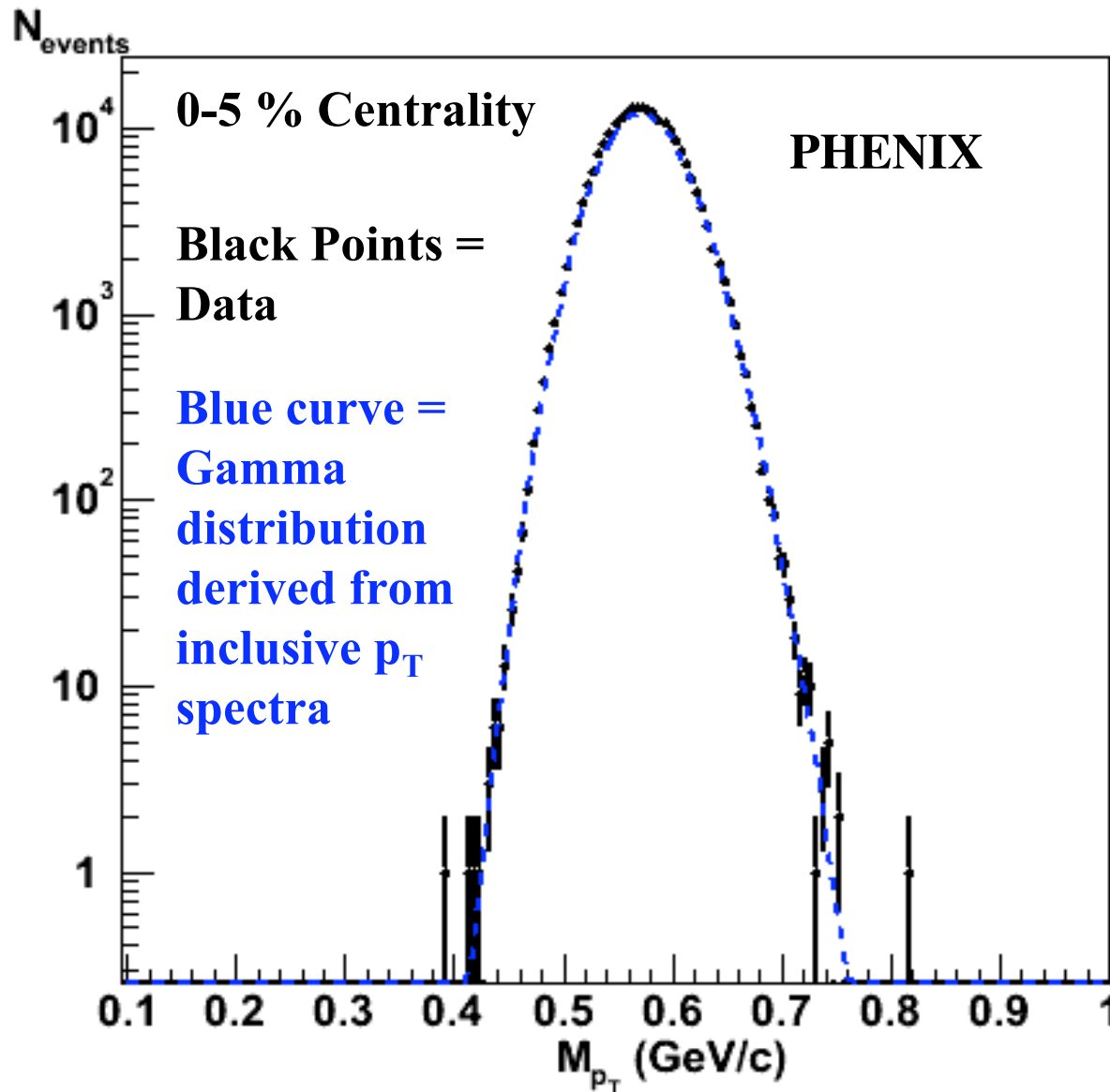


$$f(y) = \sum_{n=n_{\min}}^{n_{\max}} f_{\text{NBD}}(n, 1/k, \langle n \rangle) f_{\Gamma}(y, np, nb)$$

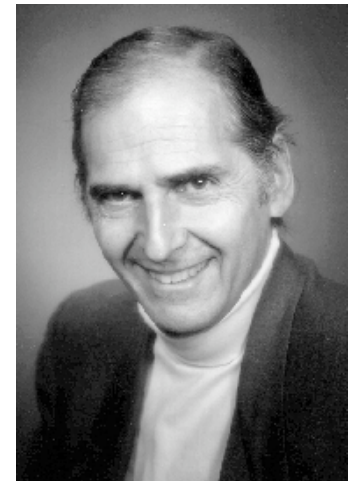
- Depends on the 4 semi-inclusive parameters
  - $b$ ,  $p$  of  $p_T$  distribution (Gamma),
  - $\langle n \rangle$ ,  $1/k$  of track multiplicity (NBD)
 derived from the quoted means and standard deviations of the semi-inclusive  $p_T$  and multiplicity distributions.
- The result is in excellent agreement with the [NA49 Pb+Pb central measurement PLB 459, 679 \(1999\)](#)

See M.J.Tannenbaum  
PLB 498, 29 (2001)

From one of Jeff Mitchell's talks: “Average  $p_T$  Fluctuations”

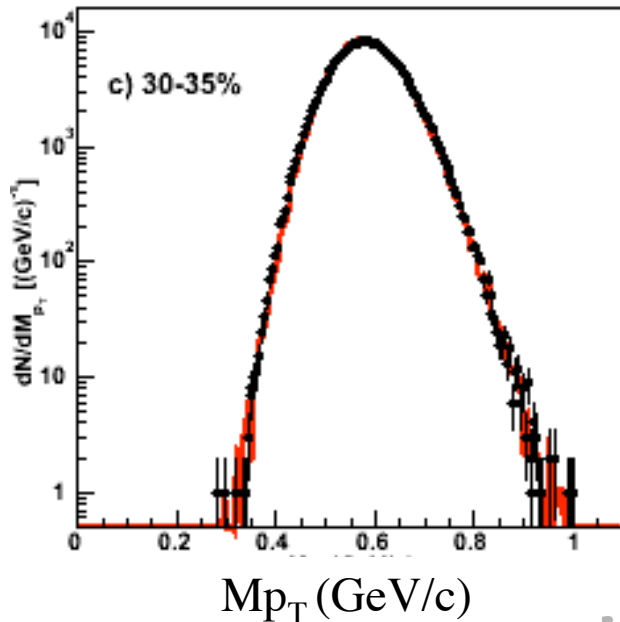
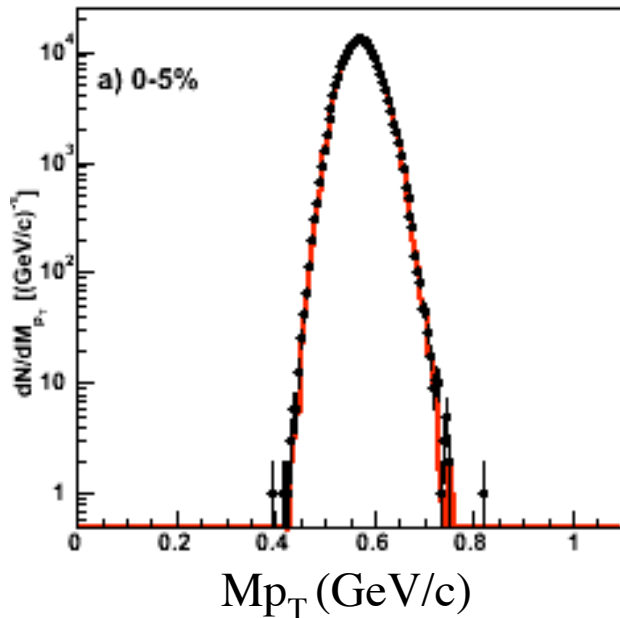


It's not a  
Gaussian...it's a  
Gamma distribution!



# PHENIX $M_{p_T}$ vs centrality

## 200 GeV Au+Au nucl-ex/0310005



- compare Data to **Mixed events** for **random**.

- Must use **exactly** the same  $n$  distribution for data and **mixed events** and **match** inclusive  $\langle p_T \rangle$  to  $\langle M_{p_T} \rangle$

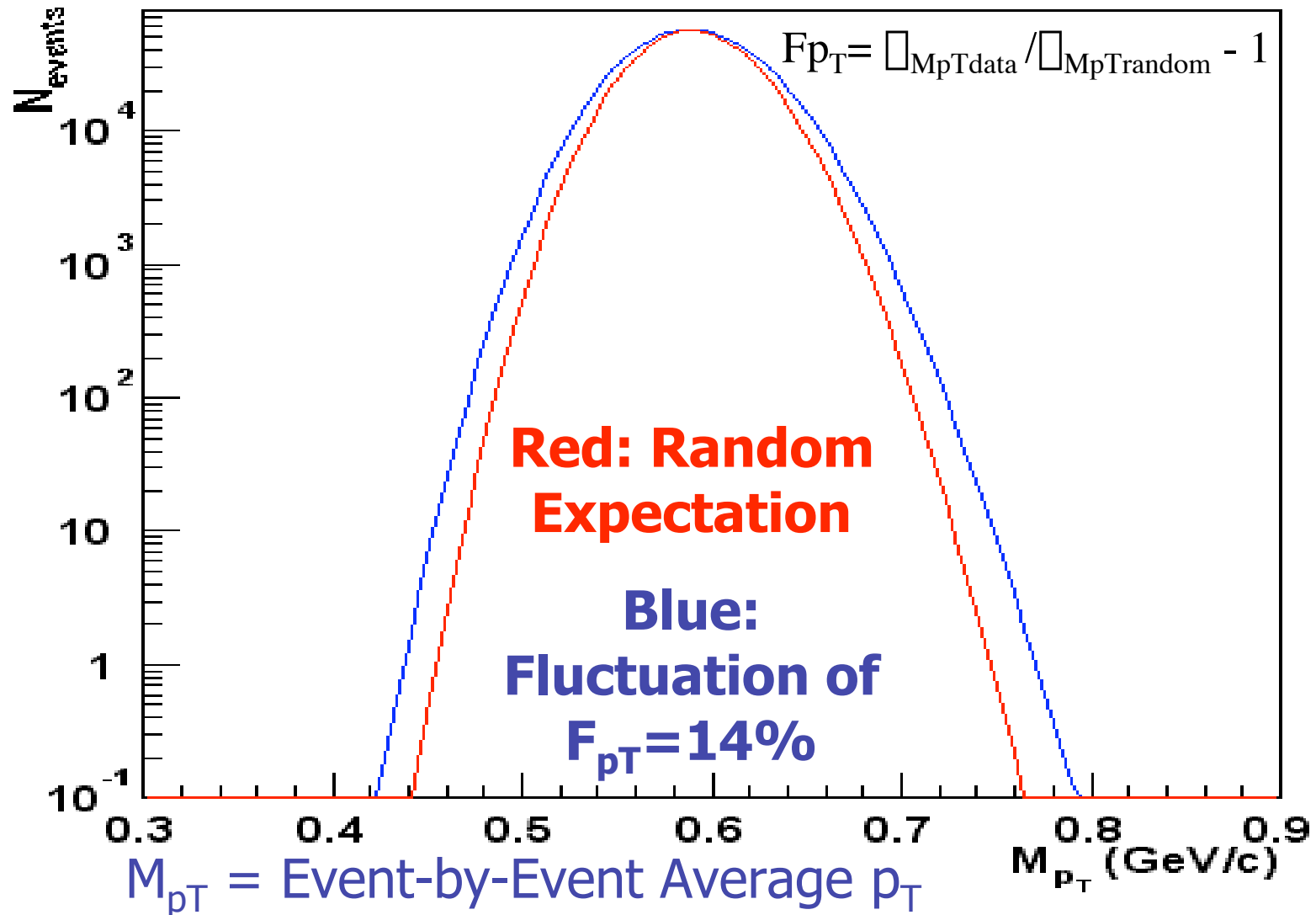
- best fit of real to **mixed** is statistically unacceptable

- deviation expressed as:

$$F_{p_T} = \frac{\square_{M_{p_T} \text{data}}}{\square_{M_{p_T} \text{mixed}}} - 1 \sim \text{few } \%$$

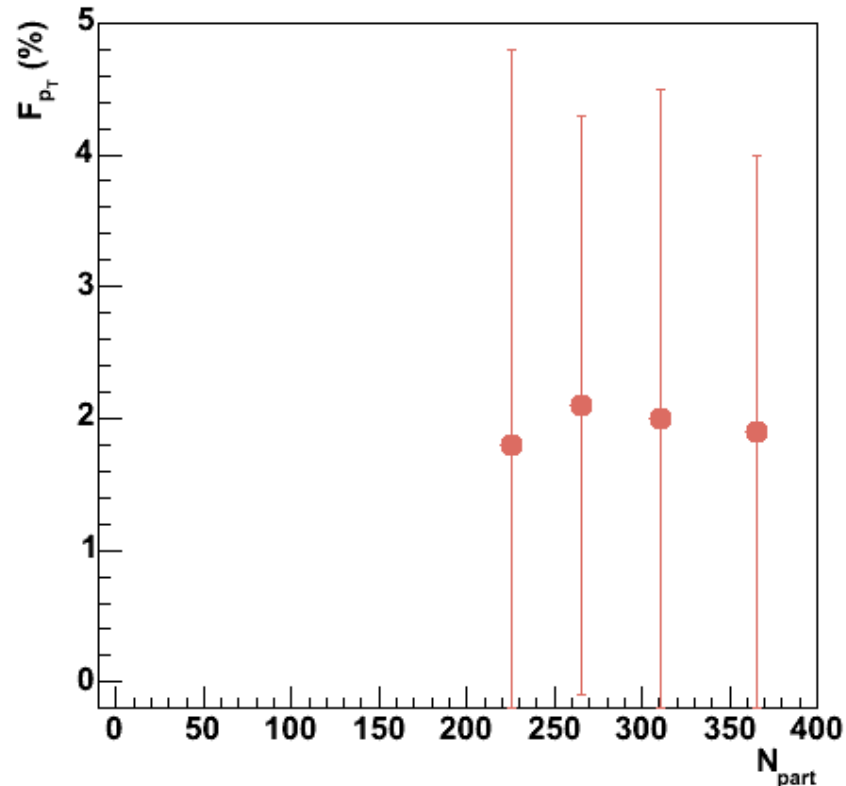
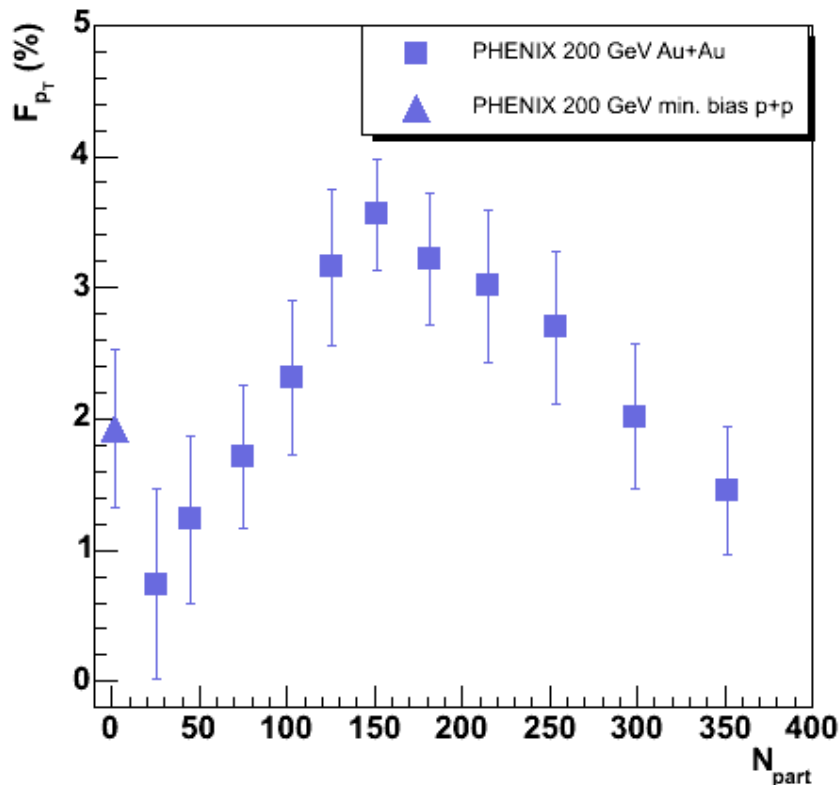
# How To Measure a Fluctuation

$\langle M_{p_T} \rangle$  must stay the same only  $\sigma_{M_{p_T}}$  varies



# Large Improvement at $s_{NN}=200$ GeV Compared to $s_{NN}=130$ GeV results

nucl-ex/0310005 subm. PRL

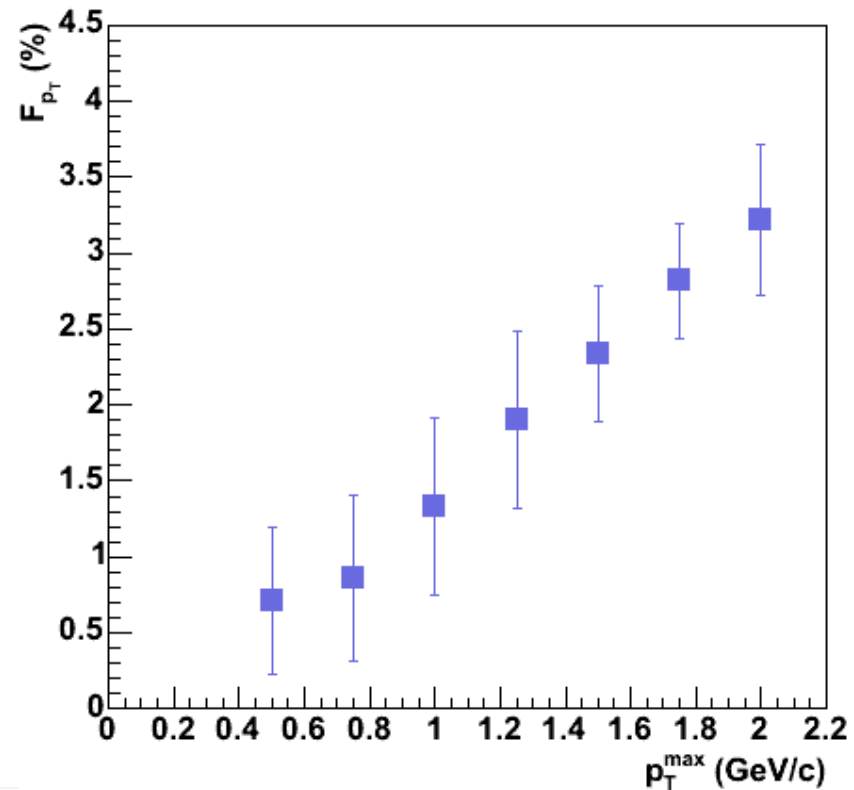
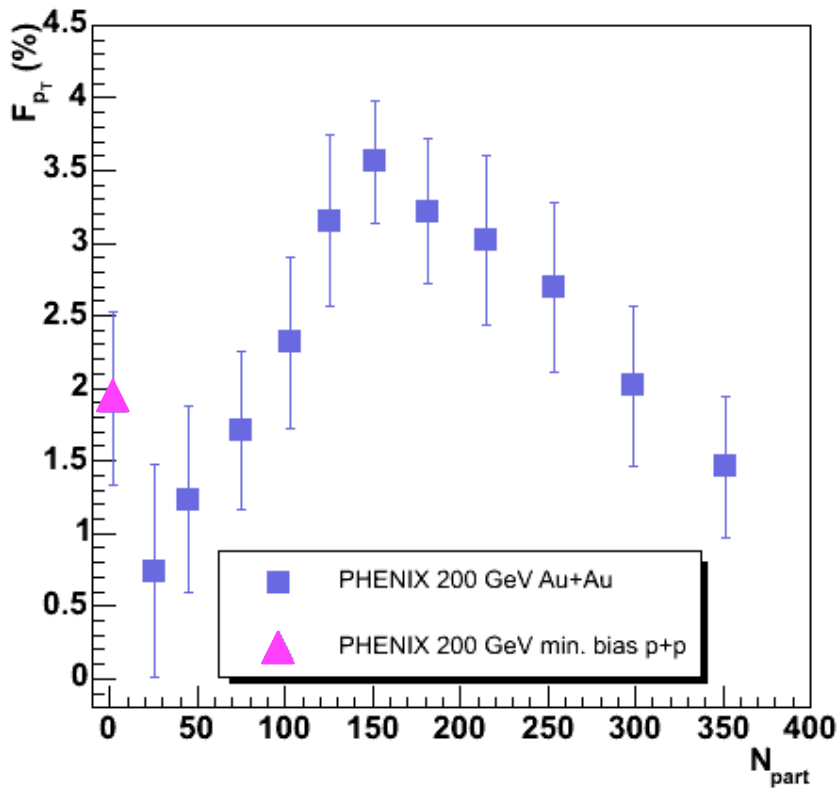


- 3 times larger solid angle
- better tracking
- more statistics

$s_{NN}=130$  GeV  
PRC 66 024901 (2002)

# Fluctuation is a few percent of $\langle \square_{MpT} \rangle$ : Interesting variation with $N_{part}$ and $p_{Tmax}$

Errors are totally systematic from run-run r.m.s variations



$n > 3$   $0.2 < p_T < 2.0$  GeV/c

$0.2$  GeV/c  $< p_T < p_T^{max}$

PHENIX nucl-ex/0310005 subm. PRL

# Simulate of Fluctuations: I-Baseline Simulation

A **data-driven** simulation designed to simulate **statistically independent particle production**:

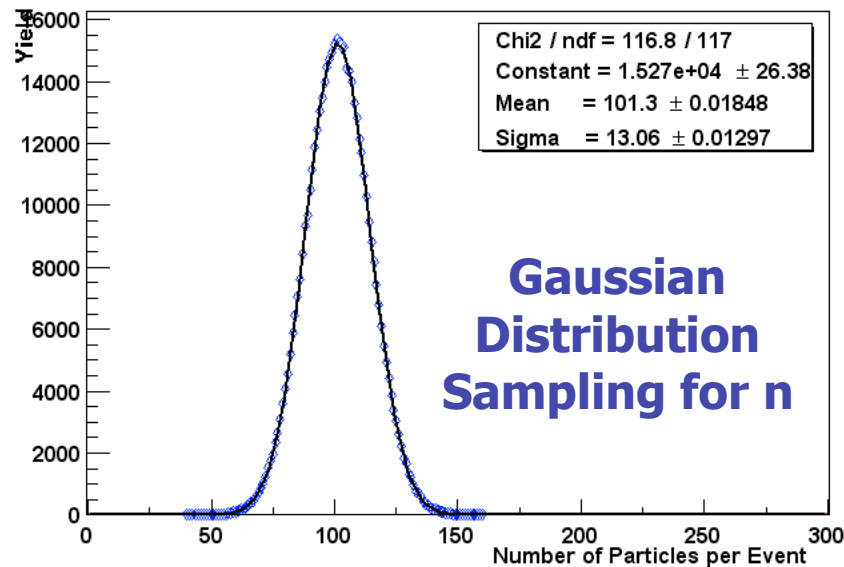
- Generate the number of particles in an event by sampling a Gaussian distribution fit to the data.
- Assign a  $p_T$  to each particle by sampling an  $m_T$  exponential distribution fit (or double exponential, or Gamma distribution) to the data inclusive  $p_T$  distribution.
- Calculates the event-by-event  $M_{pT}$ .
- Generates mixed events for calculation of fluctuation quantities.

**Input parameters include:  $\langle n \rangle$ ,  $\sigma_{\langle n \rangle}$ , inclusive  $p_T$  function parameters,  $p_T$  range for  $\langle p_T \rangle$  calculation.**



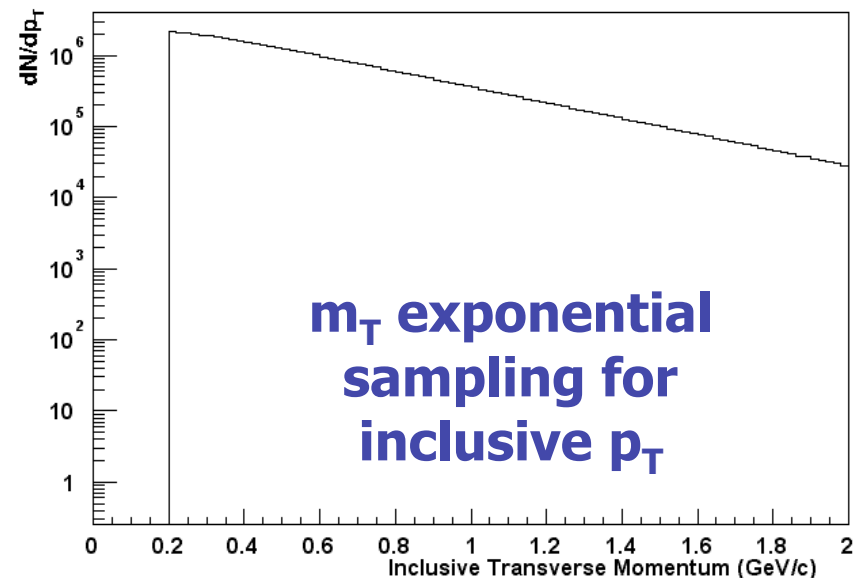


# Results from the Baseline Simulation with random $p_T$ and $n$ from measured distributions



Inclusive  $\langle p_T \rangle$ ,  $\sigma_{p_T}$ ,  
 $\langle n \rangle$ ,  $\sigma_{\langle n \rangle}$  matched to  
the data for each  
centrality class.

Sample: Using  
a match to  
PHENIX 0-5%  
centrality data

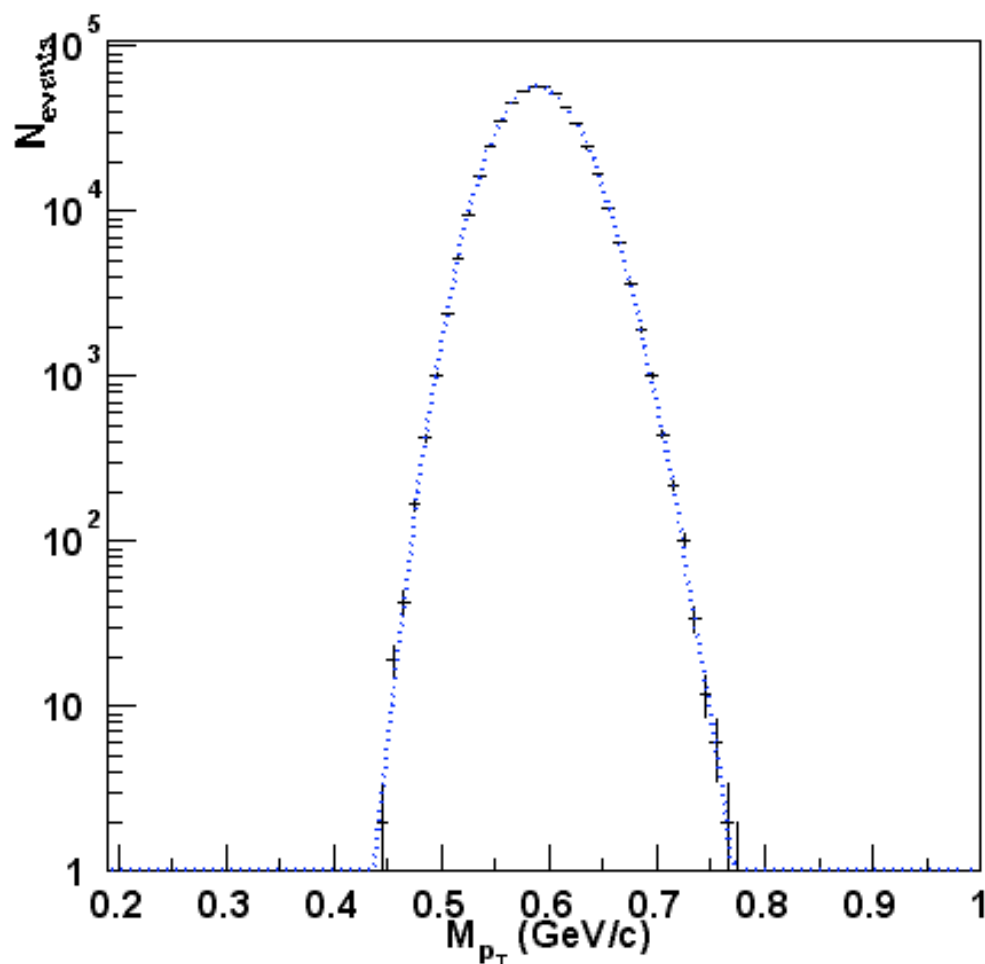


# I-Results from the Baseline Simulation

Black points: Simulation  
Output

Blue curve: Gamma  
distribution calculation  
for statistically  
independent particle  
emission with input  
parameters taken from  
the inclusive spectra.

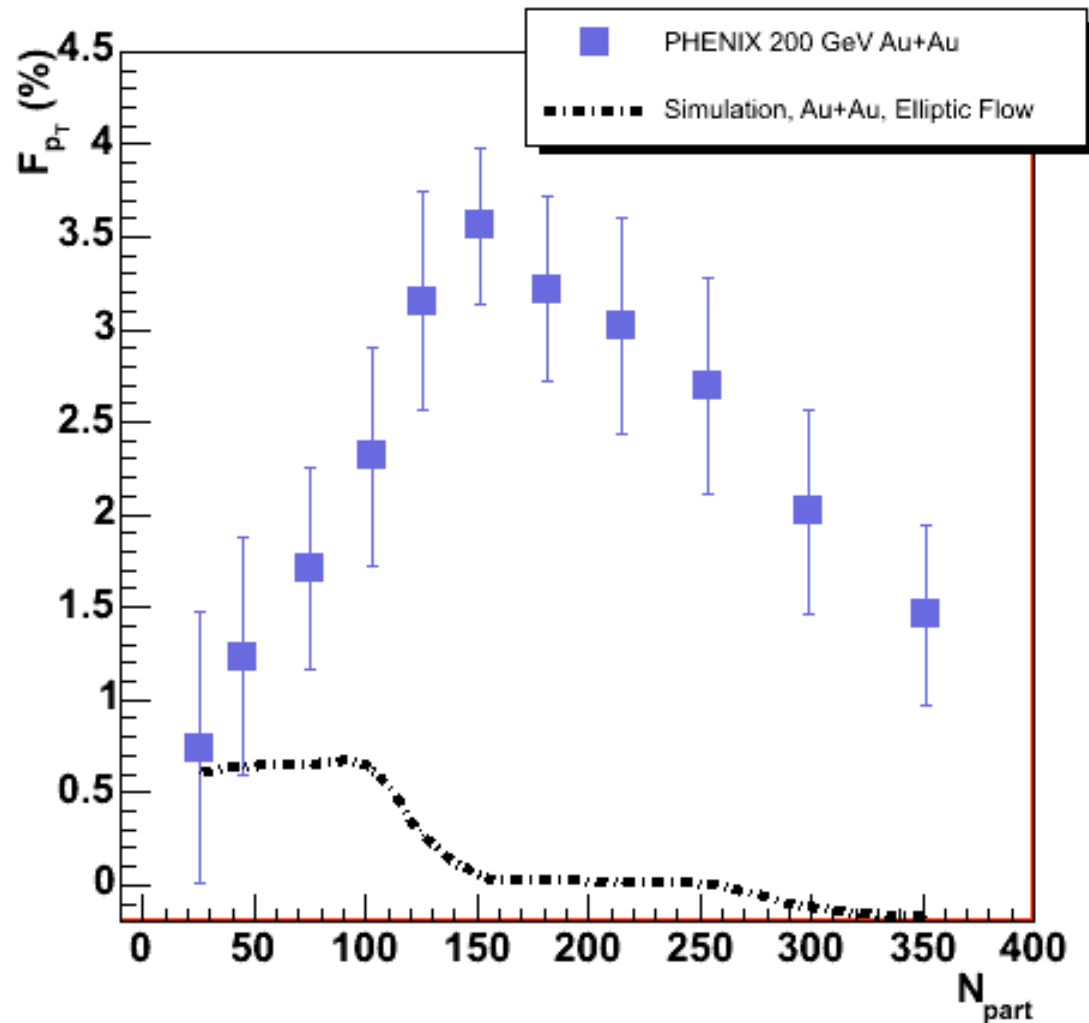
*My result (PLB498) is  
now a good check for  
statistical independence  
in the Monte Carlo or in  
the mixed events*



# II-Elliptic Flow Contribution Simulation

Algorithm: Particles are assigned an azimuthal coordinate based upon the PHENIX measurement of  $v_2$  (wrt the reaction plane) as a function of centrality and  $p_T$ . Only particles within the PHENIX acceptance are included in the calculation of  $M_{pT}$ .

With the exception of peripheral collisions, the elliptic flow contribution is a small fraction of the observed fluctuation.

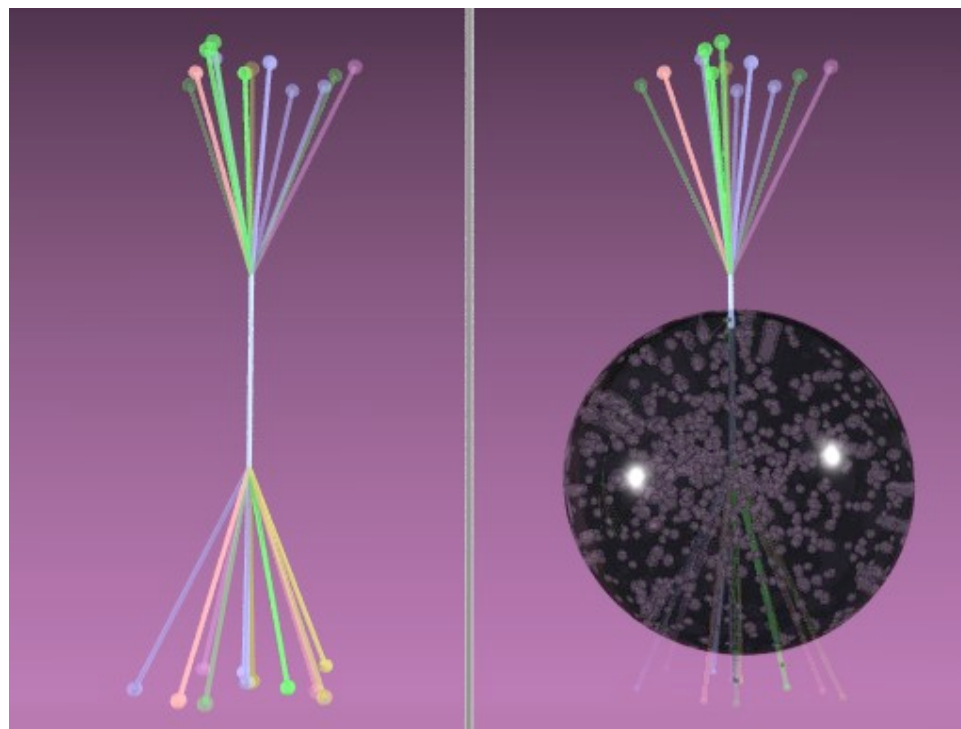


## III-A Jet Contribution?

Jets are simulated using a hybrid algorithm which embeds **Pythia** hard scattering events into Mean Max baseline events.

A single varying parameter is defined: A hard scattering probability factor,  $S_{\text{prob}}$ , is randomly tested for each thrown particle. If the test is true, a single PYTHIA event is embedded into the baseline event after applying experimental acceptance criteria.

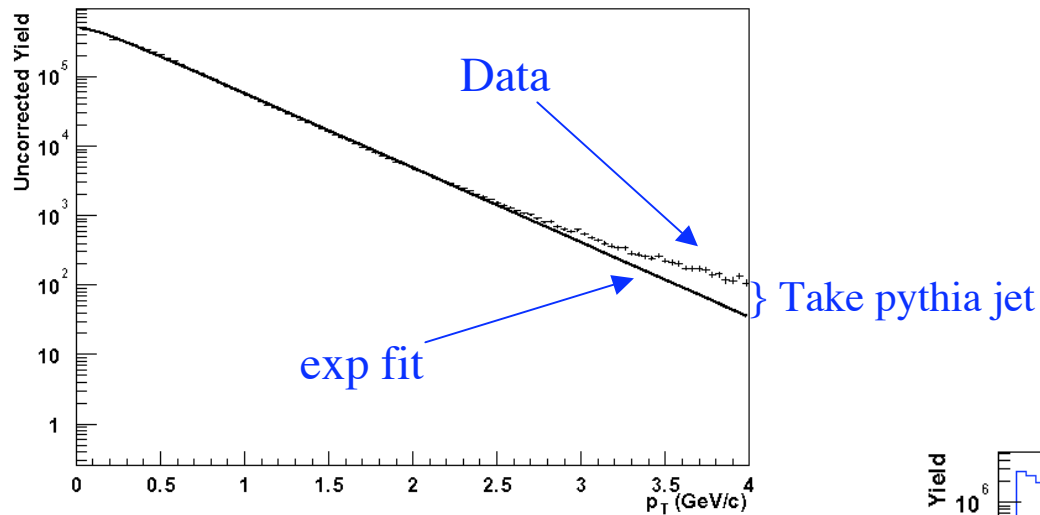
NOTE: The  $n$  distribution is preserved in this simulation. The inclusive  $\langle p_T \rangle$  and  $\sigma(p_T)$  are affected by less than 1%.



To mock up jet suppression,  $S_{\text{prob}}$  is scaled by the experimentally measured value of the nuclear modification factor,  $R_{AA}$ , as a function of centrality.

# How Jets are Inserted

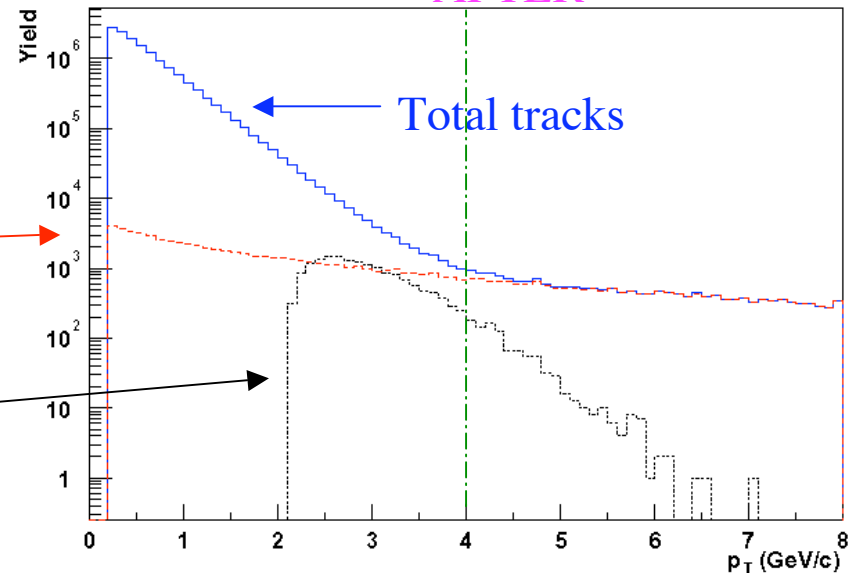
BEFORE



Tracks from pythia jets

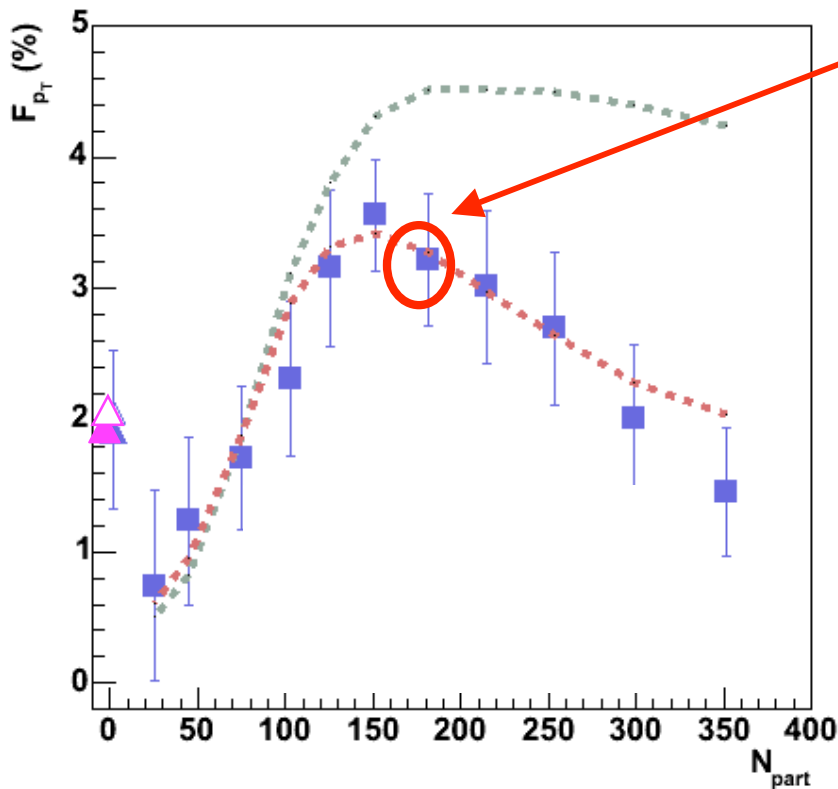
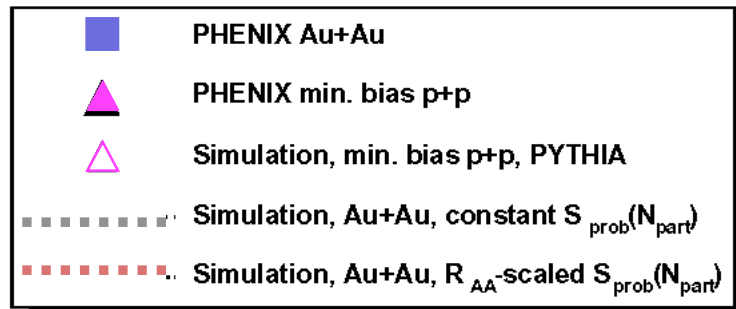
Tracks generated with original exp fit

AFTER

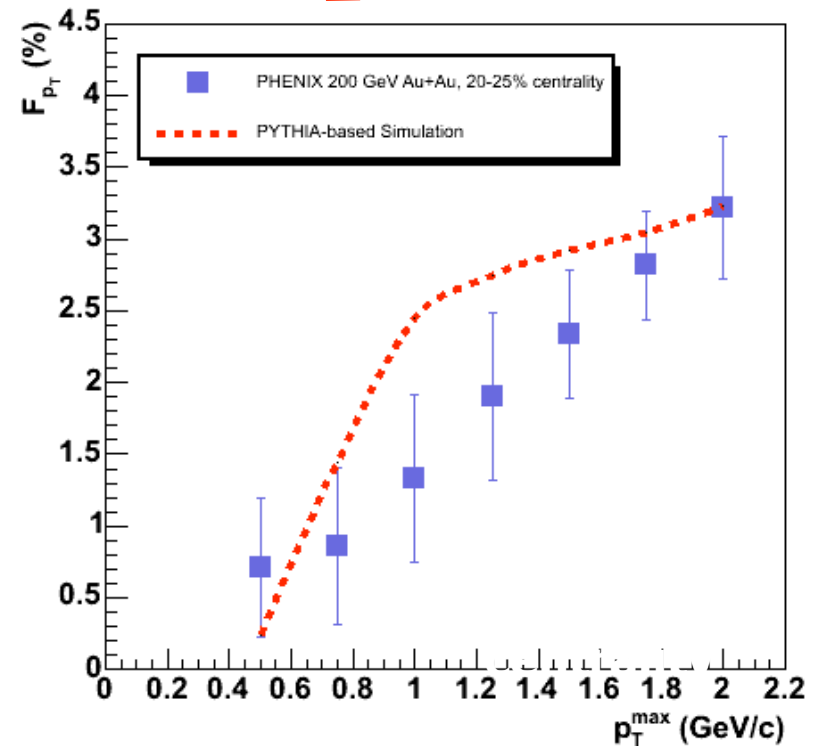


# III-Jet Simulation Results

## PHENIX at $s_{NN} = 200$ GeV



The  $S_{\text{prob}} \times R_{AA}$  parameter is initially adjusted so that  $F_{pT}$  from the simulation matches  $F_{pT}$  from the data for 20-25% centrality.



# IV-Estimate of the Magnitude of Event-by-Event Temperature Fluctuations

$$\frac{\sigma_T}{\langle T \rangle} = \sqrt{\frac{2F_{p_T}}{(p=0.8) \langle n \rangle + 1}}$$

R. Korus and S. Mrowczynski,  
Phys. Rev. C64 (2001) 054908.

Measurement	$s_{NN}$	$\sigma_T/\langle T \rangle$ Most central	$\sigma_T/\langle T \rangle$ , At the peak $F_{p_T}$
PHENIX	200	1.8%	3.7%
STAR	130	1.7%	3.8%
CERES	17	1.3%	2.2%
NA49	17	0.6%	2.6%

See Jeff Mitchell's talk for more detailed comparisons of Expt's

# Conclusions

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- PHENIX event-by-event  $M_{p_T}$  data at  $s_{NN}=200$  GeV show a significant positive non-random fluctuation---with striking variation with centrality and maximum  $p_T$  of tracks included.
- The increase of  $F_{p_T}$  with increasing  $p_T$  implies that the majority of the fluctuation is due to correlated high  $p_T$  particles.
- A hybrid simulation using PYTHIA events to simulate hard-scattering products can well reproduce the PHENIX fluctuation data at  $s_{NN}=200$  GeV when the measured jet suppression is included.
- Even if the entire fluctuation were due to event-by-event temperature fluctuations, these are less than 2 % for central collisions at both RHIC and CERN energies.
- Where are the critical-fluctuations that were expected ?