

Exploring the Proton Spin

Werner Vogelsang

RBRC & BNL Nuclear Theory

LBNL Berkeley, 12/01/2004

Spin

- invariants of Poincare group

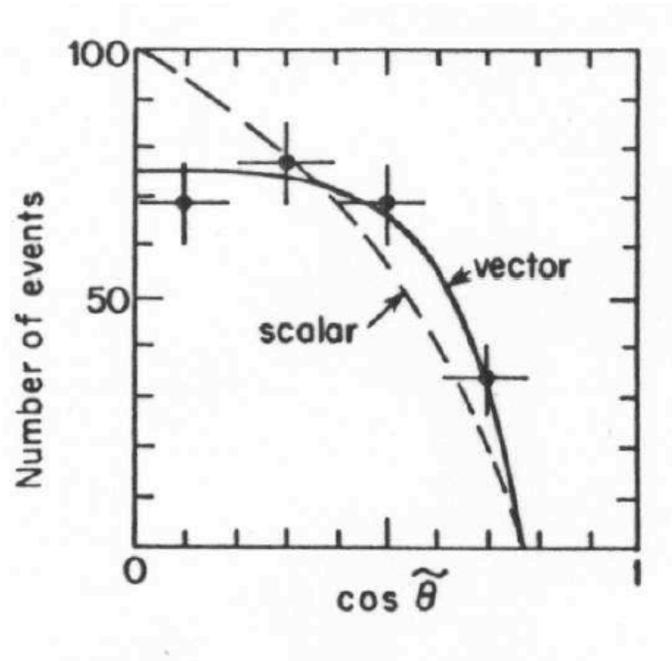
$$\mathcal{P}_\mu \mathcal{P}^\mu = m^2$$

$$\mathcal{W}_\mu \mathcal{W}^\mu = -m^2 S(S+1)$$

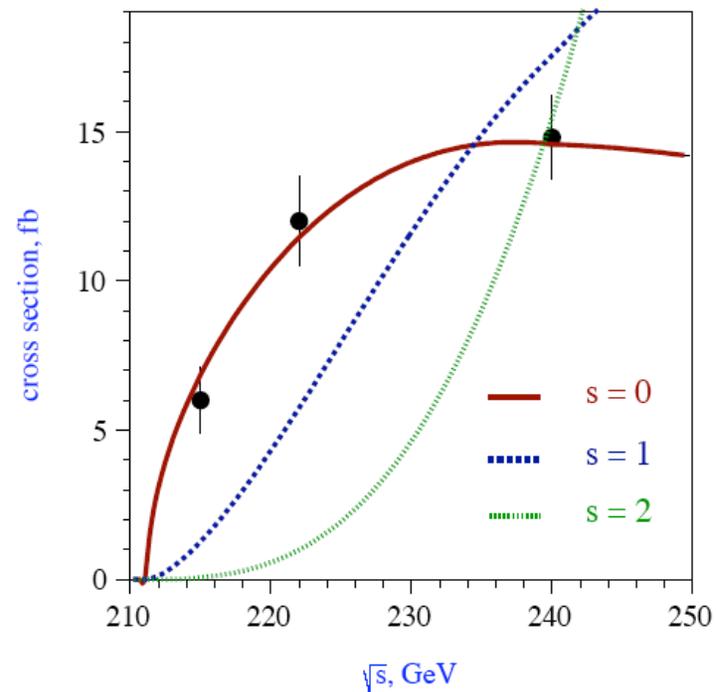
$$\mathcal{W}^\mu \sim \epsilon^{\mu\nu\rho\sigma} \mathcal{M}_{\nu\rho} \mathcal{P}_\sigma$$

- all particles that we believe to be elementary have Spin !
- gauge fields (W, Z, γ, g) : spin-1
- quarks and leptons : spin-1/2
- Higgs ?

- spin \leftrightarrow many phenomena in particle physics
 - * magnetic moments
 - * electric dipole moments
 - * angular (& other) distributions in particle reactions



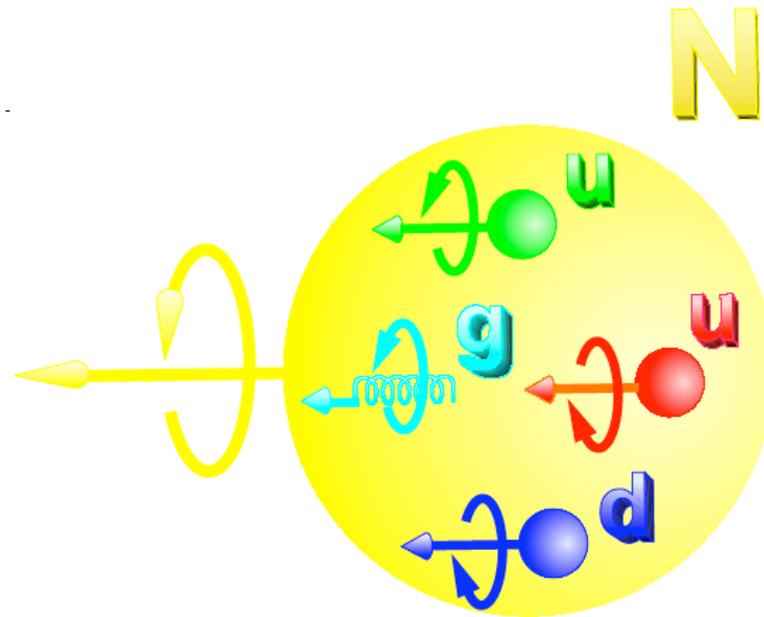
$e^+e^- \rightarrow q\bar{q}g$ TASSO



$e^+e^- \rightarrow HZ$ LC

- Today : let's look at spin in QCD

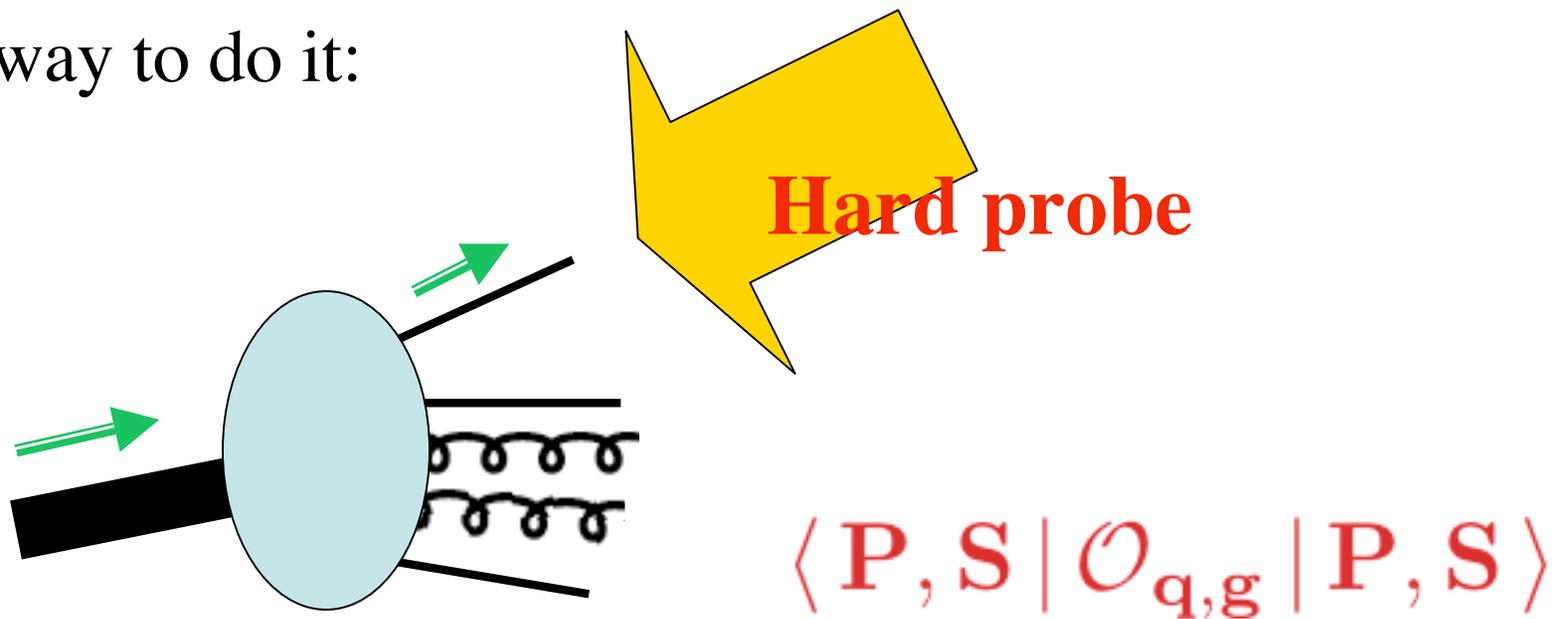
The nucleon, a composite particle with spin



- Main goal of QCD spin physics:

To understand the spin structure of hadrons in terms of quarks and gluons

- The way to do it:

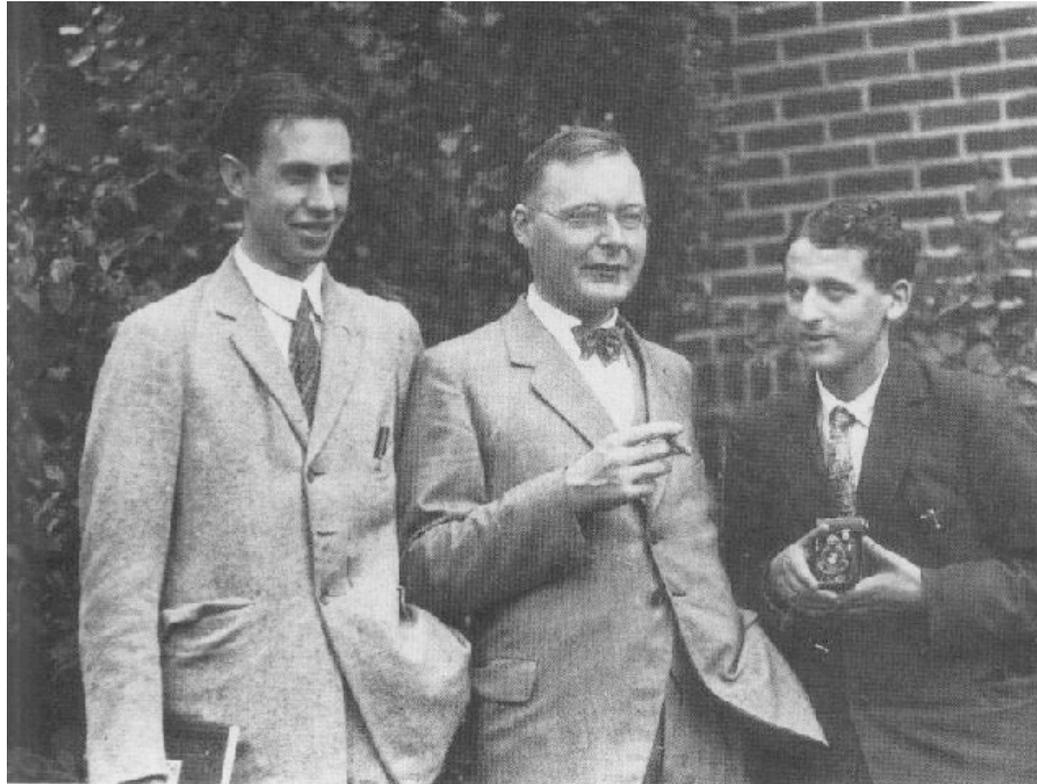


Outline:

- Early history of spin
- Early nucleon structure
- Deeply-inelastic scattering
- Polarized DIS
- Current goals in QCD spin physics
 - * quark & gluon polarization
 - * parton orbital angular momentum
 - * transverse polarization
- Conclusions & outlook

Early history of spin

Goudsmit & Uhlenbeck 1925: propose “self-rotating” electron



“This is a good idea. Your idea may be wrong, but since both of you are so young without any reputation, you would not lose anything by making a stupid mistake.”
(Ehrenfest)

1927: the proton spin is $1/2$

- Hund, Hori & Dennison's conclusion

A Note on the Specific Heat of the Hydrogen Molecule.

By DAVID M. DENNISON, Ph.D., University of Michigan.

(Communicated by R. H. Fowler, F.R.S.—Received June 3, 1927.)

In a recent article F. Hund* has treated the problem of the specific heat of the hydrogen molecule on the basis of the wave mechanics. The total number of rotational states are divided due to the homopolar character of the molecule into two groups, to the one of which belong wave functions symmetrical in the two nuclei, and to the other wave functions which are antisymmetrical in the nuclei. Hund has suggested that the presence of both groups in hydrogen may be accounted for by assuming that the nuclei possess a spin, in which case transitions between symmetrical or between antisymmetrical states will have their usual intensity but transitions between symmetrical and antisymmetrical states

a time long compared with the time of the experiment, we obtain a specific heat curve which follows the observed curve to within the errors of observation, and that moreover the constants ρ and I are in good agreement with the values of these constants as found in the band spectrum of H_2 .

[*Added June 16, 1927.*—It may be pointed out that the ratio of 3 to 1 of the antisymmetrical and symmetrical modifications of hydrogen, as regards the rotation of the molecule, is just what is to be expected from a consideration of the equilibrium at ordinary temperatures if the nuclear spin is taken equal to that of the electron, and only the complete antisymmetrical solution of the Schrödinger wave equation allowed.*

I wish to express my thanks to Mr. R. H. Fowler for much helpful criticism and to Prof. T. Hori for the opportunity of seeing the results of his work before their publication. I wish also to acknowledge with gratitude a stipend from the University of Michigan.

* W. Heisenberg, 'Z. f. Physik,' vol. 41, p. 239 (1927), in particular see p. 264.

- Heisenberg had previously entertained this idea

Early structure of the Nucleon

Structure of the nucleon in 1933:

$$\vec{\mu}_p = \frac{e\hbar}{mc} 2.79 \vec{s}_p$$

JULY 29, 1933

NATURE

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Magnetic Moment of the Proton

THE spin of the electron has the value $\frac{1}{2} \cdot \frac{h}{2\pi}$, and its magnetic moment has the value $2 \frac{e}{m_e c} \cdot \frac{1}{2} \cdot \frac{h}{2\pi}$, or 1 Bohr magneton. The spin of the proton has the same value, $\frac{1}{2} \cdot \frac{h}{2\pi}$, as that of the electron. Thus for the magnetic moment of the proton the value $2 \frac{e}{m_p c} \cdot \frac{1}{2} \cdot \frac{h}{2\pi} = 1/1840$ Bohr magneton = 1 nuclear magneton is to be expected.

So far as we know, the only method at present available for the determination of this moment is the deflection of a beam of hydrogen molecules in an inhomogeneous magnetic field (Stern-Gerlach experiment). In the hydrogen molecule, the spins of the two electrons are anti-parallel and cancel out. Thus the magnetic moment of the molecule has two sources: (1) the rotation of the molecule as a whole, which is equivalent to the rotation of charged particles, and leads therefore to a magnetic moment as arising from a circular current; and (2) the magnetic moments of the two protons.

fore, even at the lowest temperatures, the rotational magnetic moment is superimposed on that due to the two protons with parallel spin. Since, however, the rotational moment is known from the experiments with pure para-hydrogen, the moment of the protons can be determined from deflection experiments with ortho-hydrogen, or with ordinary hydrogen consisting of 75 per cent ortho- and 25 per cent para-hydrogen. The value obtained is 5 nuclear magnetons for the two protons in the ortho-hydrogen molecule, that is, 2.5 (and not 1) nuclear magnetons for the proton.

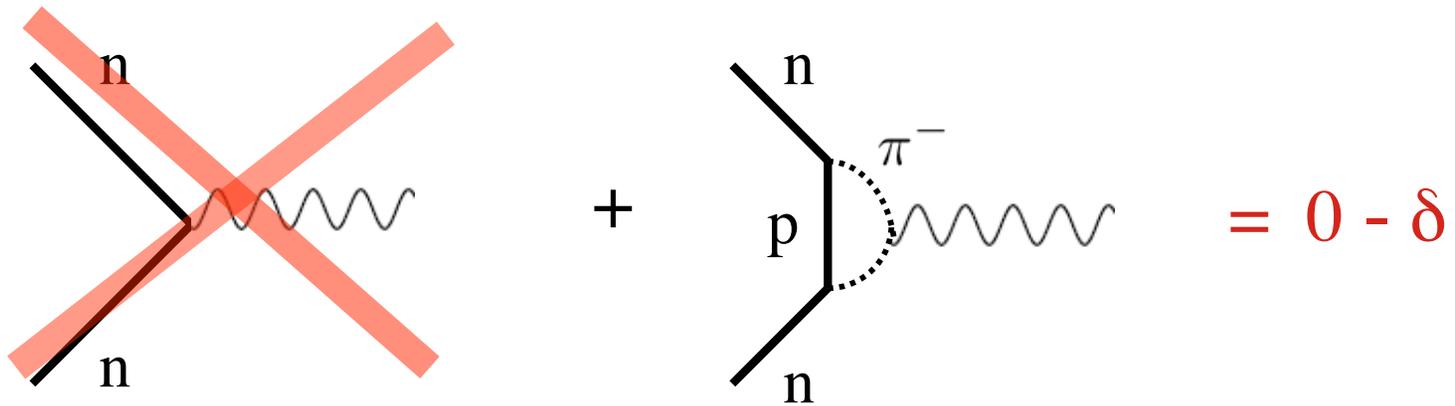
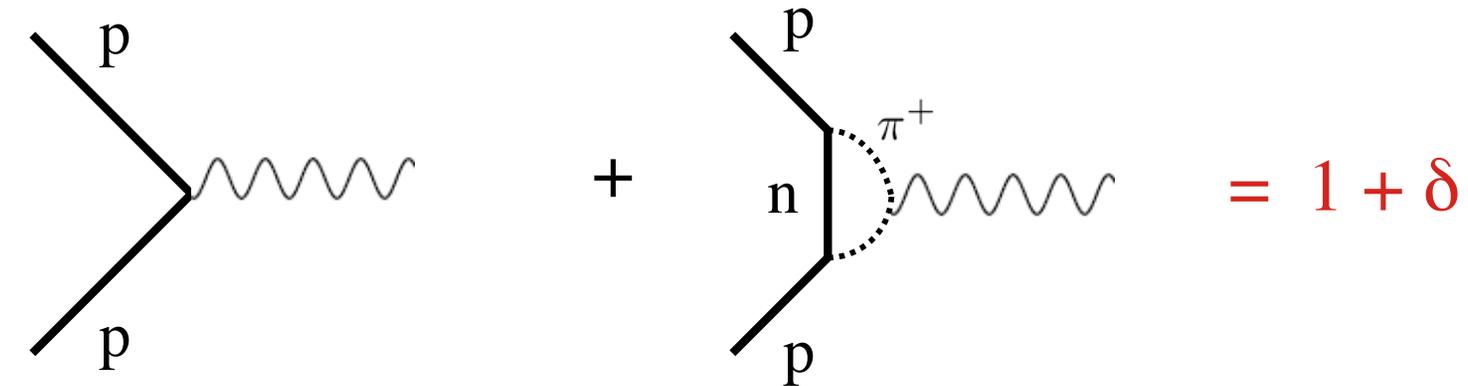
This is a very striking result, but further experiments carried out with increased accuracy and over a wide range of experimental conditions (such as temperature, width of beam, etc.) have shown that it is correct within a limit of less than 10 per cent.

A more detailed account of these experiments will appear in the *Zeitschrift für Physik*.

I. ESTERMANN.
R. FRISCH.
O. STERN.

Institut für physikalische Chemie,
Hamburgischer Universität.
June 19.

- early attempts by Yukawa's theory:



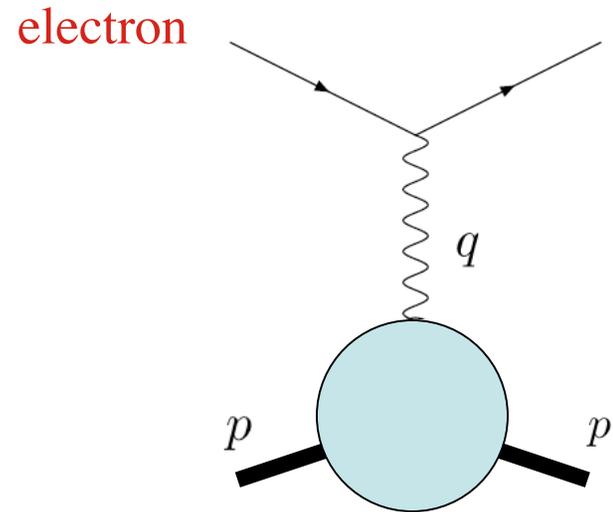
$$2.79 = 1 + 1.79$$

$$-1.91 = 0 - 1.91$$

- heavier mesons ? divergencies ?

How to get deeper insight ?

- Basic idea: scatter off nucleon with simple probe



$$Q \equiv \sqrt{-q^2}$$

$$\frac{\hbar}{Q} = \frac{2 \times 10^{-16} \text{ m}}{Q/\text{GeV}}$$

$$\frac{d\sigma}{d\Omega} = \left(\frac{d\sigma}{d\Omega} \right)_{\text{point}} |F(q)|^2$$

$$F(\vec{q}) = \int d^3x \rho(\vec{r}) e^{i\vec{q}\cdot\vec{r}}$$

form factor

- for spin-1/2 proton:

$$\bar{u}(p', s') \Gamma^\mu u(p, s) = \chi_{s'}^\dagger \left(G_E(Q^2), \frac{i\vec{\sigma} \times \vec{q}}{2m_p} G_M(Q^2) \right) \chi_s$$

where $G_E(0) = 1$ $G_M(0) = 2.79$

- cross section:

$$\tau \equiv Q^2/4M^2$$

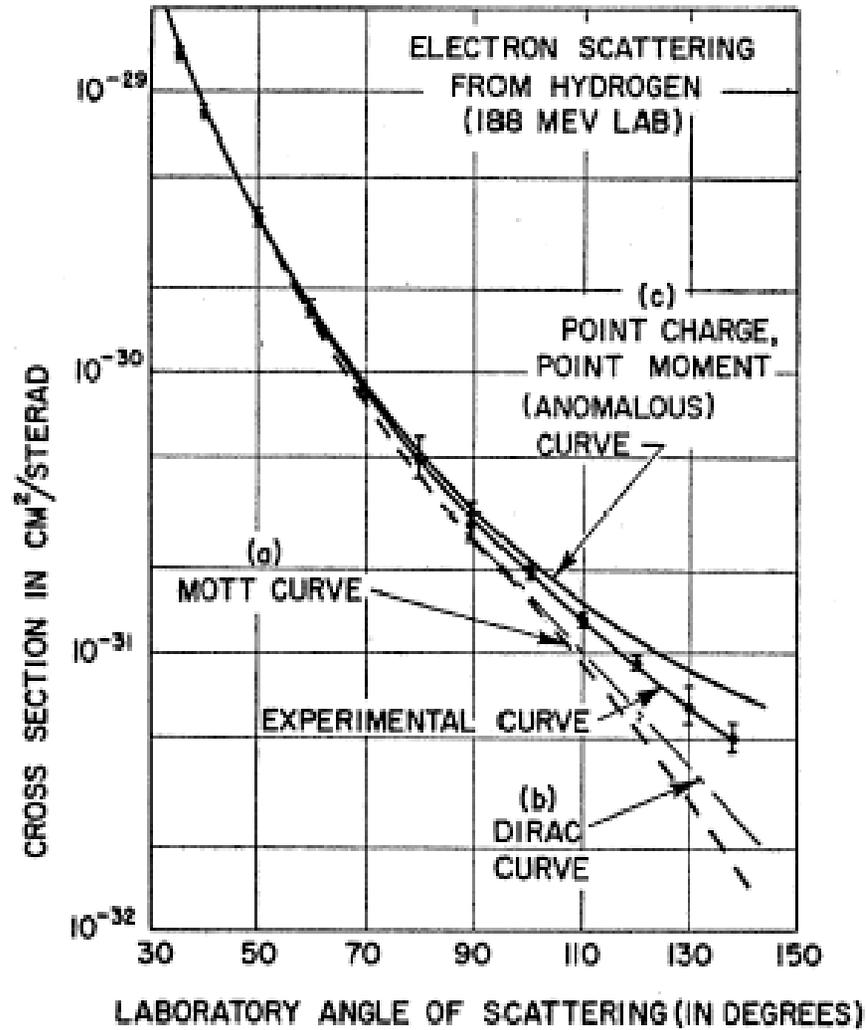
$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2}{4E^2 \sin^4\left(\frac{\theta}{2}\right)} \frac{E'}{E} \left[\frac{G_E^2 + \tau G_M^2}{1 + \tau} \cos^2\left(\frac{\theta}{2}\right) + 2\tau G_M^2 \sin^2\left(\frac{\theta}{2}\right) \right]$$

- compare point-like, but with anomalous magnetic moment:

$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2}{4E^2 \sin^4\left(\frac{\theta}{2}\right)} \frac{E'}{E} \left[\frac{1 + 7.78\tau}{1 + \tau} \cos^2\left(\frac{\theta}{2}\right) + 5.58\tau \sin^2\left(\frac{\theta}{2}\right) \right]$$

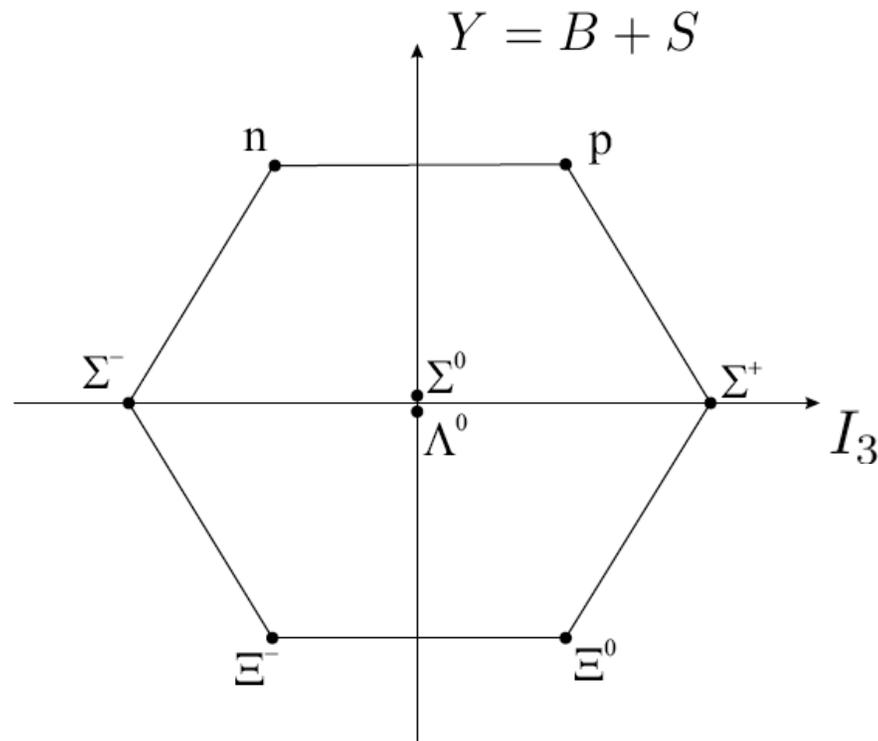
Structure of the nucleon in the '50s

McAllister, Hofstadter



$$\Rightarrow \langle r^2 \rangle \sim 10^{-15} \text{ m}$$

- fit hadrons with similar properties into SU(3) multiplets:
Gell-Mann; Ne'eman; Nishijima



- fundamental representation of SU(3): triplet \rightarrow u d s quarks

Gell-Mann; Zweig

$$|\text{baryon}\rangle = |qqq\rangle \quad |\text{meson}\rangle = |q\bar{q}\rangle$$

- the proton wave function is:

$$|P, \uparrow\rangle = \frac{1}{\sqrt{18}} [2u^\uparrow u^\uparrow d^\downarrow - u^\uparrow u^\downarrow d^\uparrow - u^\downarrow u^\uparrow d^\uparrow + \text{perm.}]$$

- from this, magnetic moments: $\sim \langle P, \uparrow | \mu_i (\sigma_3)_i | P, \uparrow \rangle$

$$\mu_p = \frac{1}{3} [4\mu_u - \mu_d] \quad \mu_n = \frac{1}{3} [4\mu_d - \mu_u] \quad \mu_i = \frac{e_i \hbar}{2m_i c}$$

$$\frac{\mu_n}{\mu_p} = -\frac{2}{3} \quad \text{exp.} = -0.685 \quad \checkmark$$

- quarks carry the proton spin - **entirely**:

$$\mathcal{N}(u^\uparrow) - \mathcal{N}(u^\downarrow) = \frac{4}{3} \quad \mathcal{N}(d^\uparrow) - \mathcal{N}(d^\downarrow) = -\frac{1}{3}$$

$$\frac{1}{2} \left(\frac{4}{3} - \frac{1}{3} \right) = \frac{1}{2}$$

- from now on:

$$\mathcal{N}(u^\uparrow) - \mathcal{N}(u^\downarrow) \equiv \Delta U$$

- $\mathbf{q}^\dagger \sigma_{\mathbf{k}} \mathbf{q}$ becomes $\bar{\mathbf{q}} \gamma^\mu \gamma^5 \mathbf{q}$ in rel. theory
- simple quark model has limitations: predicts

$$g_A = \Delta U - \Delta D = \frac{5}{3} \quad \text{exp.} = 1.257 \quad \times$$

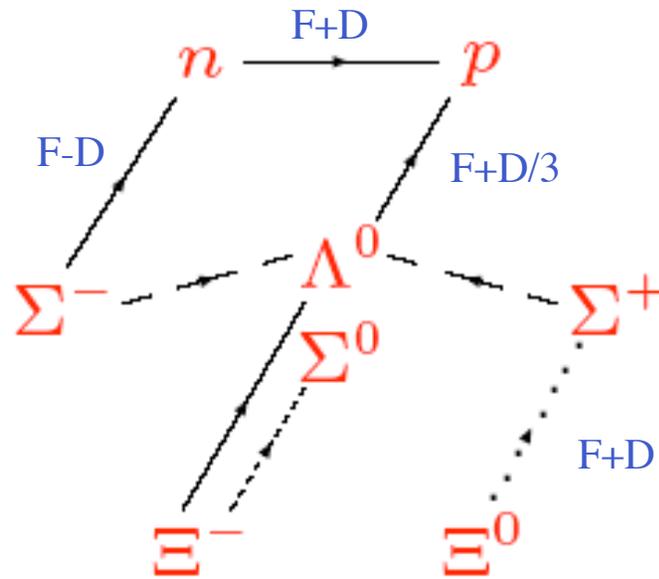
β decay $n \rightarrow p e^- \bar{\nu}_e$



- also, expect higher Fock states in nucleon:

$$|u, u, d\rangle + |u, u, d, (u\bar{u})\rangle + |u, u, d, (s\bar{s})\rangle + \dots$$

- what can be said in terms of SU(3) symmetry alone?



- find:

Bjorken; Ellis, Jaffe

$$\Delta U + \Delta \bar{U} - (\Delta D + \Delta \bar{D}) = F + D = 1.257 \pm 0.003$$

$$\Delta U + \Delta \bar{U} + \Delta D + \Delta \bar{D} - 2(\Delta S + \Delta \bar{S}) = 3F - D = 0.575 \pm 0.05$$

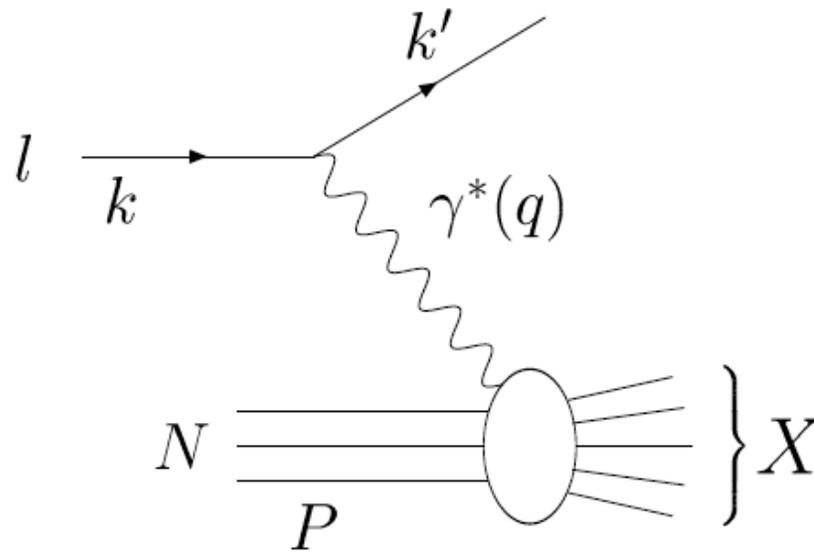
- no prediction for total quark spin contribution:

$$\Delta \Sigma = \Delta U + \Delta \bar{U} + \Delta D + \Delta \bar{D} + \Delta S + \Delta \bar{S} = ?$$

Measure in deeply-inelastic processes!

Structure of the Nucleon from
the late '60s: the inelastic era

- Deeply-inelastic scattering : $ep \rightarrow eX$



$$Q^2 = -q^2 \gg m_N^2$$

“inelasticity”

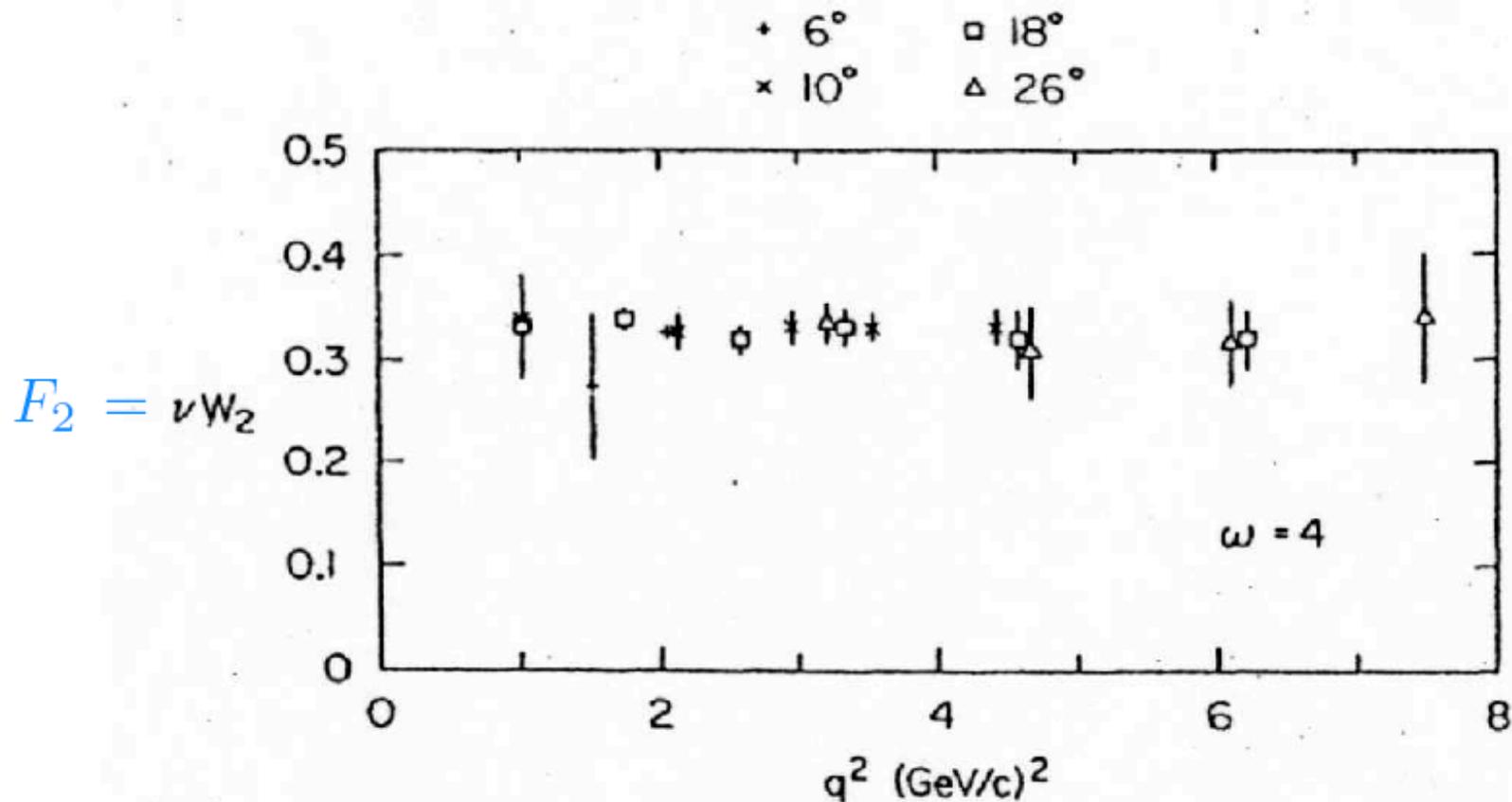
$$x \equiv \frac{Q^2}{2P \cdot q} = \frac{Q^2}{Q^2 + M_X^2 - m_N^2}$$

Bjorken var.

- spin-averaged cross section : $(y = 1 - \frac{P \cdot k'}{P \cdot k})$

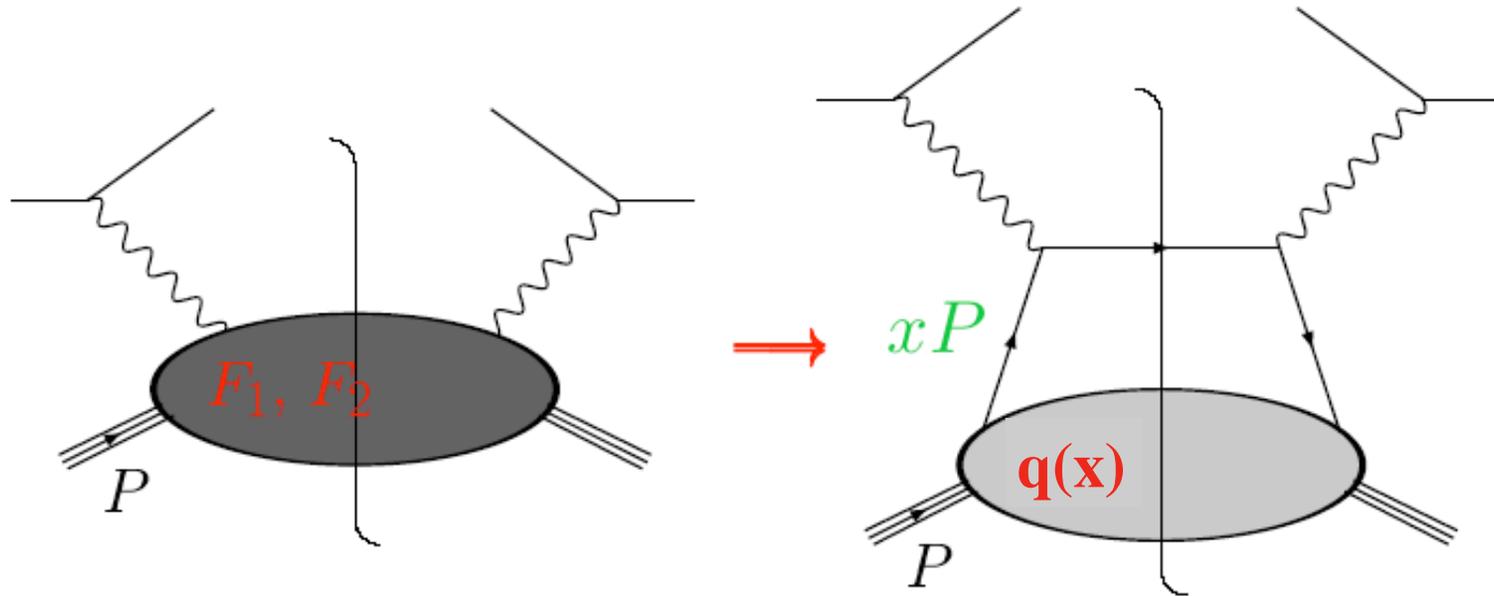
$$\frac{d^2\sigma}{dx dQ^2} = \frac{4\pi\alpha^2}{Q^4 x} \left[xy^2 F_1(x, Q^2) + (1-y) F_2(x, Q^2) \right]$$

- early results from SLAC : "scaling"



Parton Model :

Feynman; Bjorken, Paschos



$$F_1(x) = \frac{1}{2} \sum_q e_q^2 [q(x) + \bar{q}(x)]$$

$$F_2(x) = 2x F_1(x)$$

(spin 1/2 !)

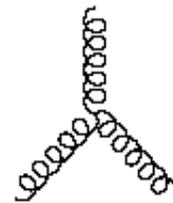
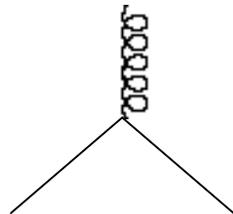
- this opened the door to the development of a comprehensive theory of quarks and gluons and their interactions:

Quantum Chromo-Dynamics (QCD)

- * quarks come in 3 colors

$$u = \begin{pmatrix} u \\ u \\ u \end{pmatrix}$$

- * \mathcal{L}_{QCD} invariant under local SU(3) phase transformations
- * color charge couples to 8 generalized “photons”: gluons
- * non-abelian gauge group \Rightarrow gluons carry color



Ultraviolet Behavior of Non-Abelian Gauge Theories*

David J. Gross[†] and Frank Wilczek

Joseph Henry Laboratories, Princeton University, Princeton, New Jersey 08540

(Received 27 April 1973)

It is shown that a wide class of non-Abelian gauge theories have, up to calculable logarithmic corrections, free-field-theory asymptotic behavior. It is suggested that Bjorken scaling may be obtained from strong-interaction dynamics based on non-Abelian gauge symmetry.

Non-Abelian gauge theories have received much attention recently as a means of constructing unified and renormalizable theories of the weak and electromagnetic interactions.¹ In this note we report on an investigation of the ultraviolet (UV) asymptotic behavior of such theories. We have found that they possess the remarkable feature, perhaps unique among renormalizable theories, of asymptotically approaching free-field theory. Such asymptotically free theories will exhibit, for matrix elements of currents between on-mass-shell states, Bjorken scaling. We therefore suggest that one should look to a non-Abelian gauge theory of the strong interactions to provide the explanation for Bjorken scaling, which has so far eluded field-theoretic understanding.

Reliable Perturbative Results for Strong Interactions?*

H. David Politzer

Jefferson Physical Laboratories, Harvard University, Cambridge, Massachusetts 02138

(Received 3 May 1973)

An explicit calculation shows perturbation theory to be arbitrarily good for the deep

- crucial success for QCD : Christ, Haslacher, Mueller; Georgi, Politzer; DGLAP

quantitative prediction of scaling violations in DIS

- why dependence on Q^2 after all ?

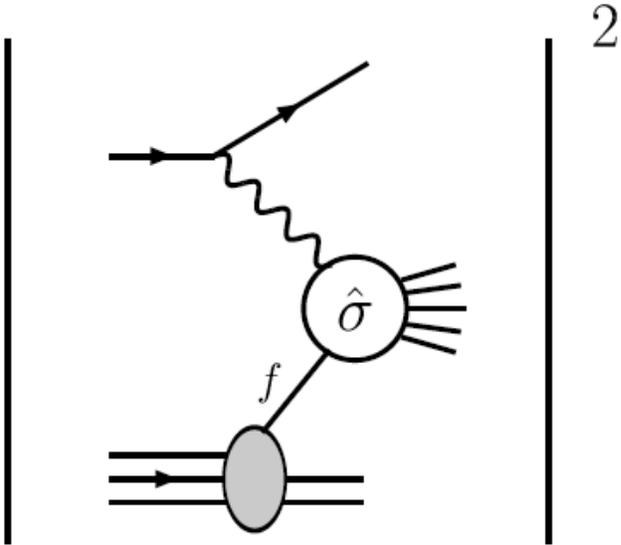
Parton states not truly frozen. Some fluctuate on scales $\sim 1/Q$



$$Q^2 \frac{d}{dQ^2} \begin{pmatrix} q(x, Q^2) \\ g(x, Q^2) \end{pmatrix} = \int_x^1 \frac{dz}{z} \begin{pmatrix} \mathcal{P}_{qq} & \mathcal{P}_{qg} \\ \mathcal{P}_{gq} & \mathcal{P}_{gg} \end{pmatrix}_{(z, \alpha_s(Q^2))} \cdot \begin{pmatrix} q \\ g \end{pmatrix} \left(\frac{x}{z}, Q^2 \right)$$

“DGLAP” evolution

The essence: DIS “factorizes”



$$\sigma = \sum_f f(x, Q) \times \hat{\sigma}^{\gamma^* f}(x, \alpha_s(Q)) + \underbrace{\mathcal{O}\left(\frac{\lambda^2}{Q^2}\right)}_{\text{“small”}}$$

parton distrib.

$$\langle P | \mathcal{O}_q | P \rangle$$

parton- γ^*

cross sec.
perturbative

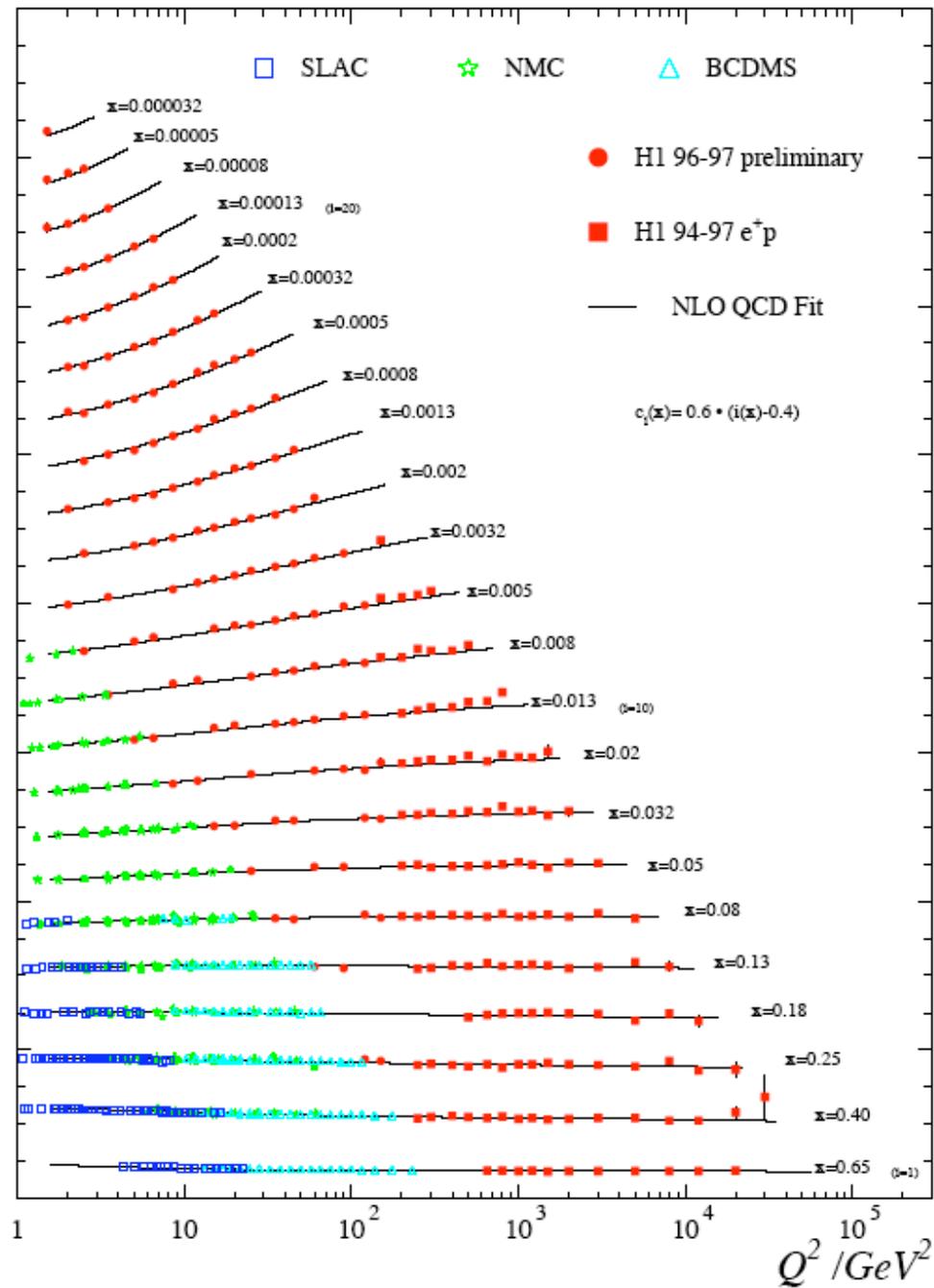
$$\hat{\sigma}^{\gamma^* q} \sim \left| \begin{array}{c} \text{LO diagram} \end{array} \right|^2 + \left| \begin{array}{c} \text{NLO diagram} + \dots \end{array} \right|^2 + \dots$$

LO

NLO

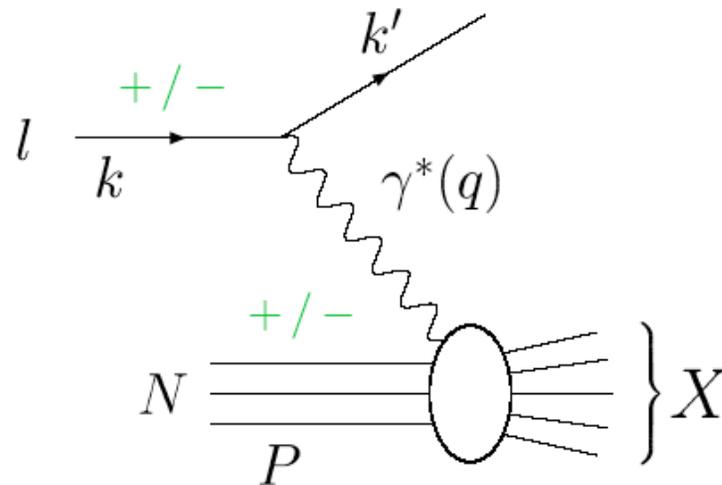
$$\hat{\sigma}^{\gamma^* g} \sim \left| \begin{array}{c} \text{NLO diagram} + \dots \end{array} \right|^2 + \dots$$

$F_2 + c_i(x)$



Polarized deeply-inelastic scattering

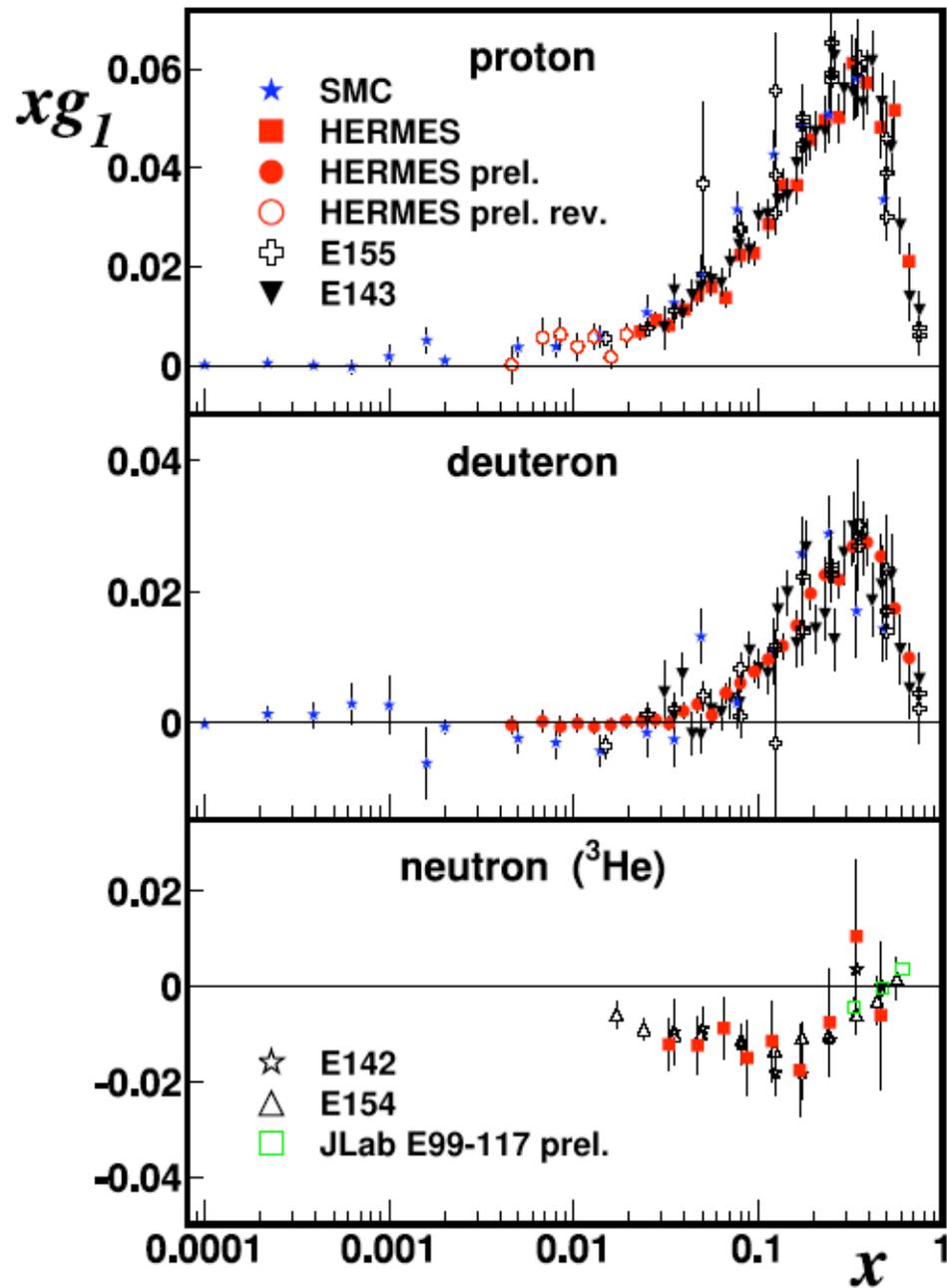
- advent of polarized electron beams 1972
- first polarized DIS (SLAC E-80) 1976



$$\frac{d^2\sigma}{dx dy} \approx \frac{4\pi\alpha^2}{Q^2} \left[y F_1(x, Q^2) + \frac{1-y}{yx} F_2(x, Q^2) + \lambda_l \lambda_N (2-y) g_1(x, Q^2) \right]$$

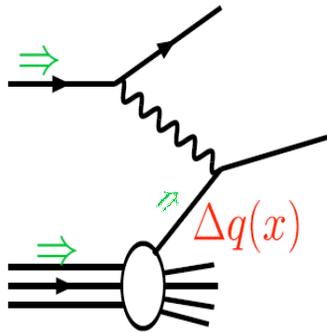
$$\sigma(++)-\sigma(+-) \quad \text{gives} \quad g_1(x, Q^2)$$

- so far “fixed-target” experiments (p, n, d)
SLAC (E80,130,142,143,155), CERN (EMC,SMC), DESY (HERMES)



(U. Stösslein / HERMES)

in the parton model :



$$F_1(x) = \frac{1}{2} \sum_q e_q^2 [q(x) + \bar{q}(x)]$$

$$g_1(x) = \frac{1}{2} \sum_q e_q^2 [\Delta q(x) + \Delta \bar{q}(x)]$$

$$\Delta q(x) = \text{[red circle with right arrow]} - \text{[red circle with left arrow]}$$

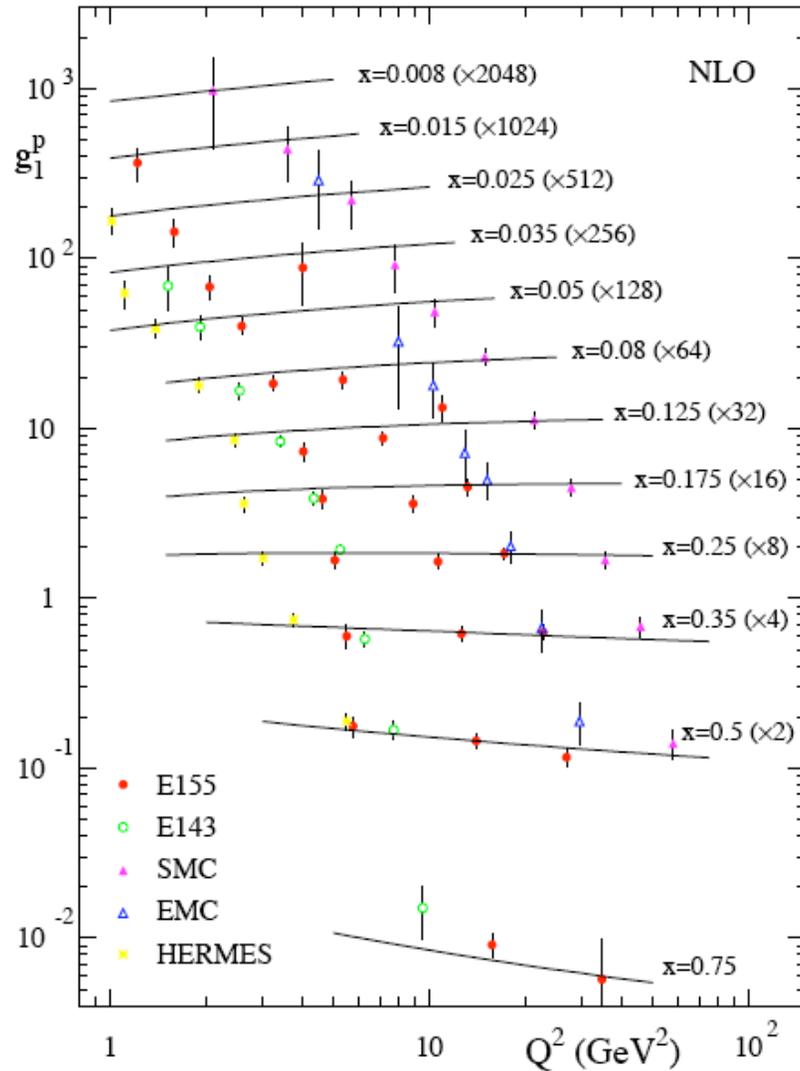
$$q(x) = \text{[red circle with right arrow]} + \text{[red circle with left arrow]}$$

- also for g_1 scaling violations predicted in QCD:

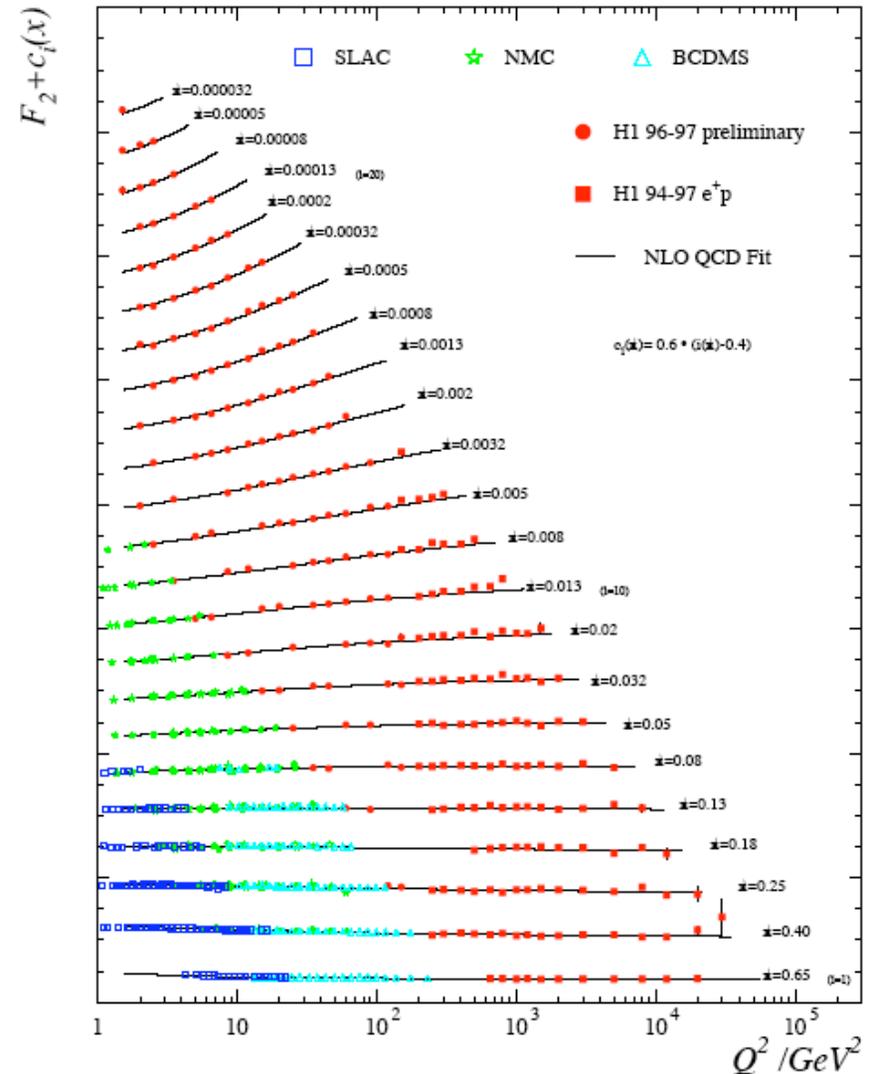
$$g_1(x) \longrightarrow g_1(x, Q^2)$$

World data on pol. and unpol. deep-inelastic scattering

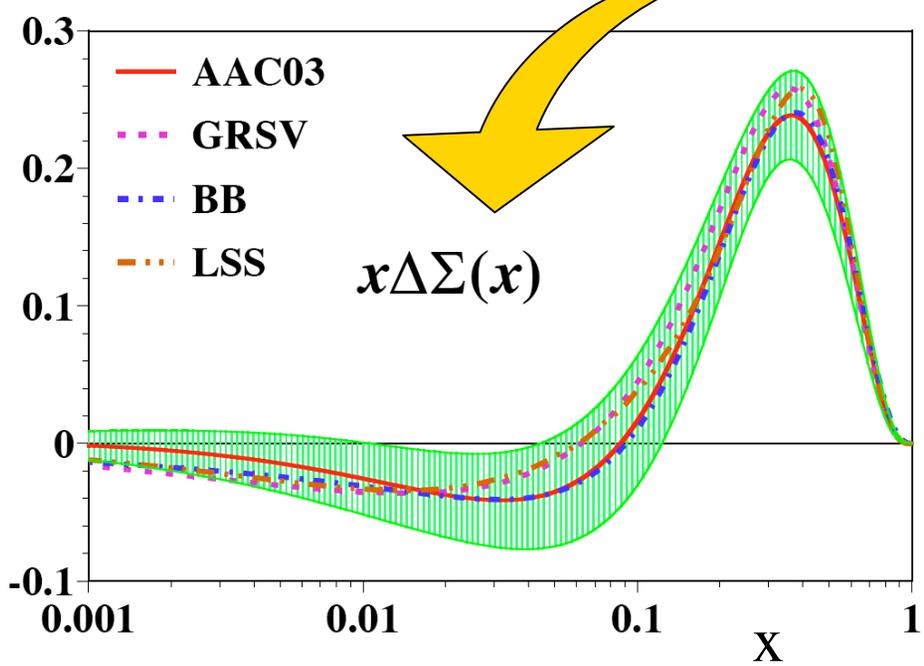
polarized



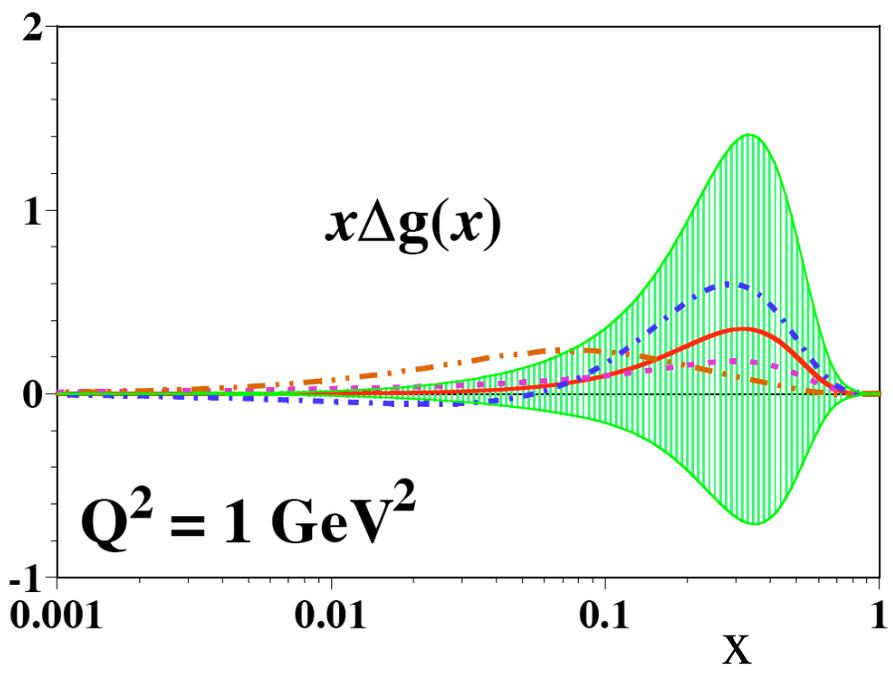
unpolarized



Hirai, Kumano, Saito



$$\Delta\Sigma = \Delta u + \Delta\bar{u} + \Delta d + \Delta\bar{d} + \Delta s + \Delta\bar{s}$$



gluon polarization ?

$$\Delta g(x) = \text{[Diagram: gluon with right arrow]} - \text{[Diagram: gluon with left arrow]}$$

very weak constraint from scaling violations

- experiments have determined

$$\Gamma_1(Q^2) \equiv \int_0^1 dx g_1(x, Q^2)$$

- have

$$2\Gamma_1 = \frac{4}{9} (\Delta U + \Delta \bar{U}) + \frac{1}{9} (\Delta D + \Delta \bar{D}) + \frac{1}{9} (\Delta S + \Delta \bar{S})$$

- recall

$$\Delta U + \Delta \bar{U} - (\Delta D + \Delta \bar{D}) = F + D$$

$$\Delta U + \Delta \bar{U} + \Delta D + \Delta \bar{D} - 2(\Delta S + \Delta \bar{S}) = 3F - D$$

$$\Delta\Sigma \equiv \Delta U + \Delta \bar{U} + \Delta D + \Delta \bar{D} + \Delta S + \Delta \bar{S} \approx 0.2 \ll 1$$

So, what carries the proton spin ?

$$\frac{1}{2} = \langle \mathbf{P}, \frac{1}{2} | \mathbf{J}_3 | \mathbf{P}, \frac{1}{2} \rangle$$

$$\mathbf{J}_i = -\frac{1}{2} \epsilon_{ijk} M^{jk} = \int d^3x \left[\vec{x} \times \vec{T}_{\text{QCD}} \right]_i$$

In QCD:

$$J_3 = \int d^3x \left[\underbrace{\bar{\psi} \gamma^3 \gamma_5 \psi}_{\sim \text{quark spin}} + \underbrace{\psi^\dagger \left(\vec{x} \times (-i\vec{D}) \right)_3 \psi}_{\sim \text{quark OAM}} + \underbrace{\left[\vec{x} \times \left(\vec{E}(\vec{x}) \times \vec{B}(\vec{x}) \right) \right]_3}_{\sim \text{total gluon ang. mom.}} \right]$$

↓
spin + OAM

-
- spin sum rule :

$$\frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta G + L_q + L_g$$

where

- * $\Delta G(Q^2) = \int_0^1 dx \Delta g(x, Q^2)$

$$\Delta g(x) = \text{[Diagram: quark with right-pointing red arrow]} - \text{[Diagram: quark with left-pointing red arrow]}$$

The diagram shows two circular nodes containing a wavy line representing a gluon. The left node has a red arrow pointing to the right, and the right node has a red arrow pointing to the left. A green arrow points to the right from the right side of each node. A minus sign is placed between the two nodes.

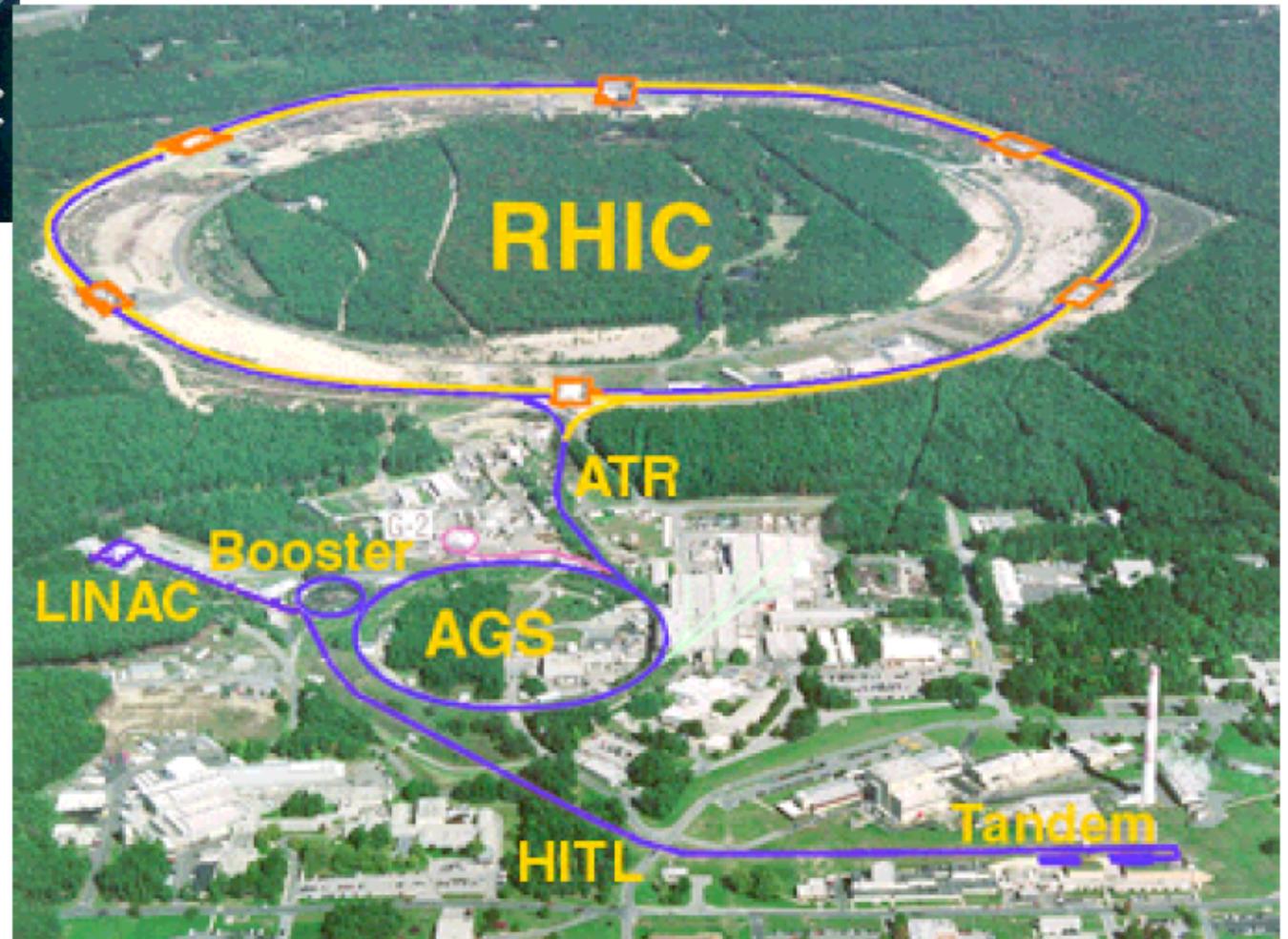
- * $L_{q,g}$ quark, gluon orbital angular momenta

→ How to measure ?

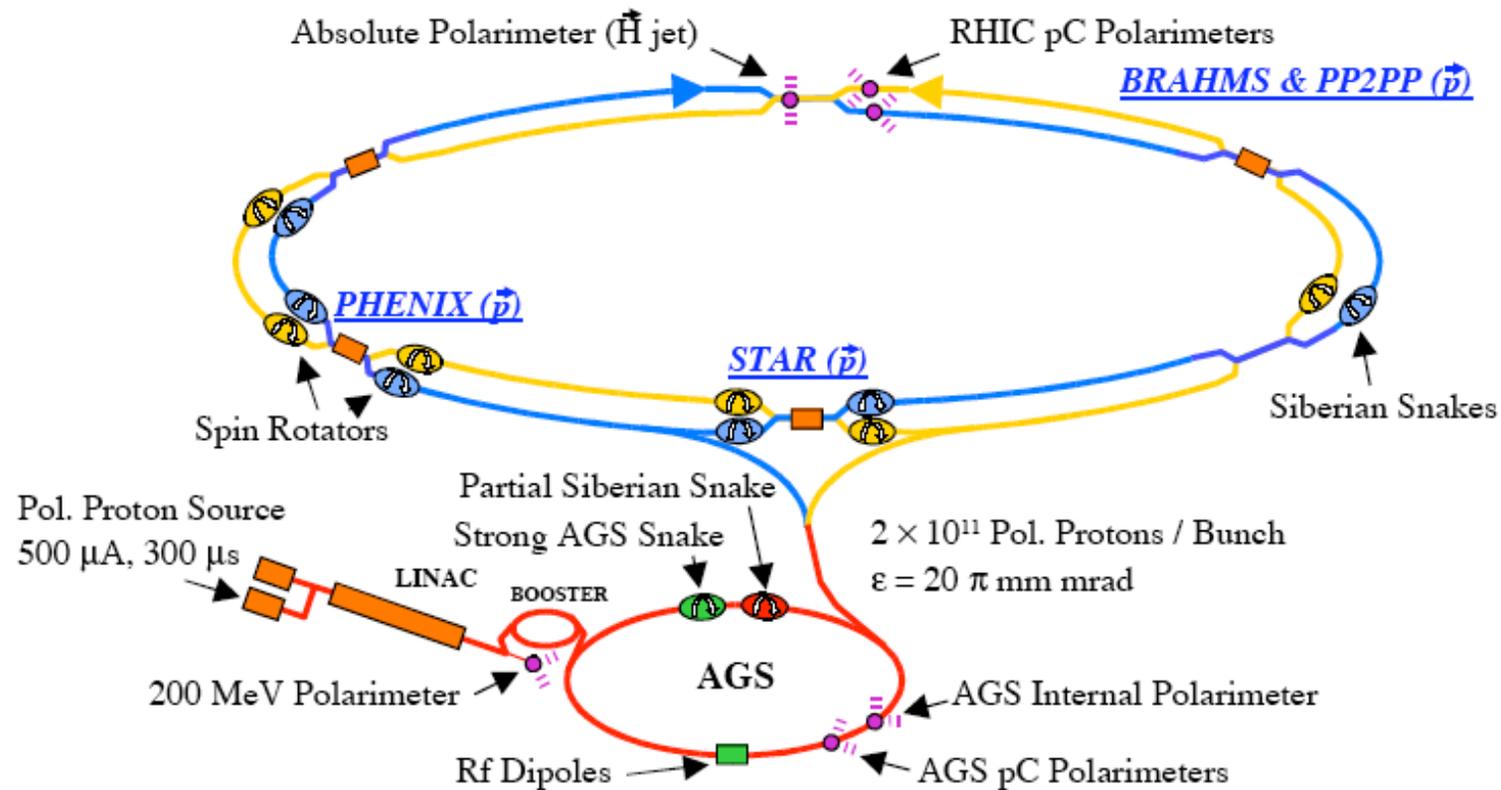
Current goals in QCD spin physics

- results from polarized DIS have motivated
 - * new generation of facilities to explore the nucleon spin structure
 - * large theoretical activity
- today, have a number of new experiments / facilities
 - * lepton-nucleon scattering HERMES, COMPASS, JLab
 - * polarized proton-proton collisions at RHIC
- key goals :
 - * gluon polarization Δg in nucleon
 - * more information on $\Delta q, \Delta \bar{q}$ (e.g., by flavor)
 - * orbital angular momentum
 - * phenomena in QCD with transverse polarization

A new milestone : polarized pp collider RHIC

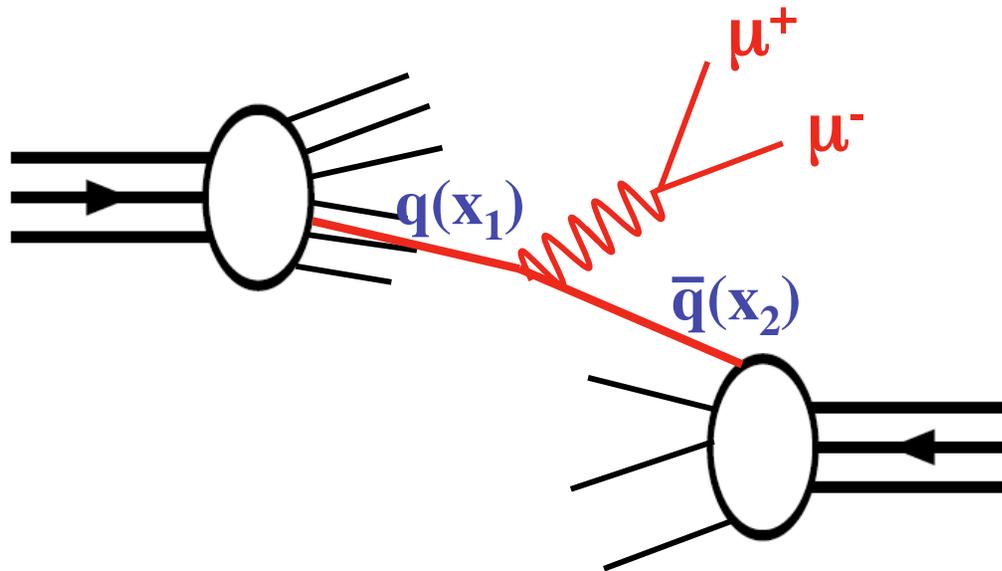


Polarized Proton Collisions in RHIC



Soon after DIS & parton model :

Drell, Yan



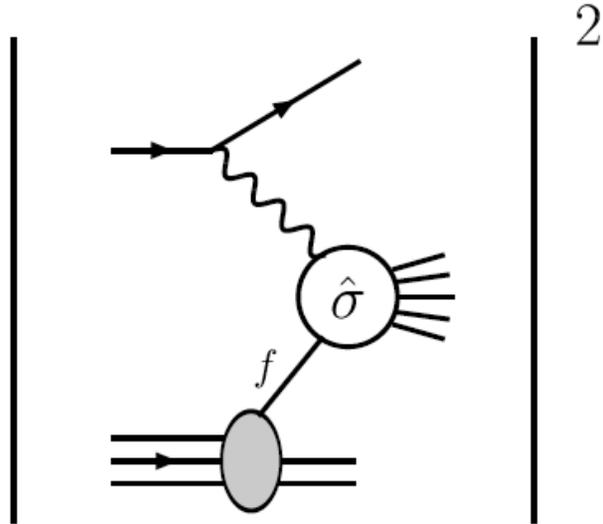
Then extension to many other reactions :

$$pp \rightarrow \text{jet } X, \quad pp \rightarrow \pi X, \quad pp \rightarrow \gamma X, \quad pp \rightarrow Q\bar{Q} X, \dots$$

Feynman; Berman, Jacob; Berman, Bjorken, Kogut; Feynman, Field, Fox; . . .

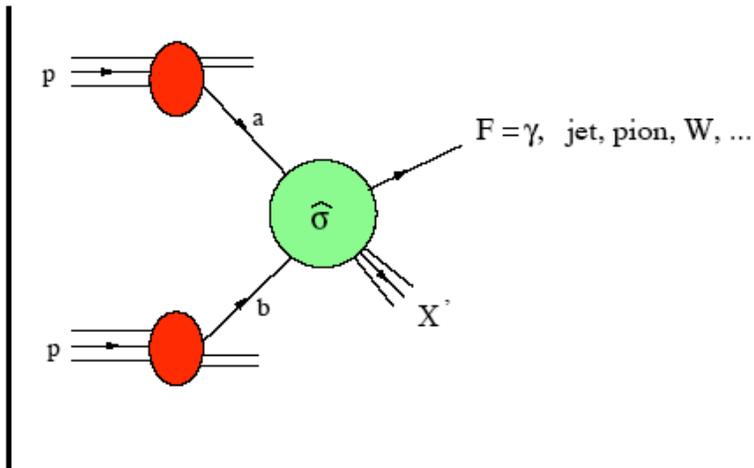
- this is formalized in “factorization theorems”

Sterman,Libby; Ellis et al.; Collins,Soper,Sterman



$$\sigma = \sum_f f(x, Q) \times \hat{\sigma}^{\gamma^* f}(x, \alpha_s(Q)) + \mathcal{O}\left(\frac{\lambda^2}{Q^2}\right)$$

universal pdf's



2

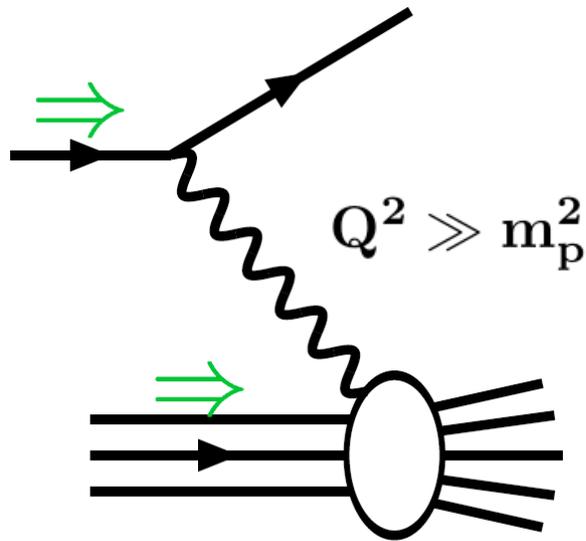
$$\sigma = \sum_{a,b} f_a(x_a, p_T) \times f_b(x_b, p_T) \times \hat{\sigma}^{ab \rightarrow F}(x_a, x_b, \alpha_s(p_T)) + \mathcal{O}\left(\frac{\lambda}{p_T}\right)$$

perturbation theory

$$\hat{\sigma} = \underbrace{\hat{\sigma}^0}_{\text{LO}} + \underbrace{\alpha_s \hat{\sigma}^1}_{\text{NLO}} + \dots$$

Compare the probes :

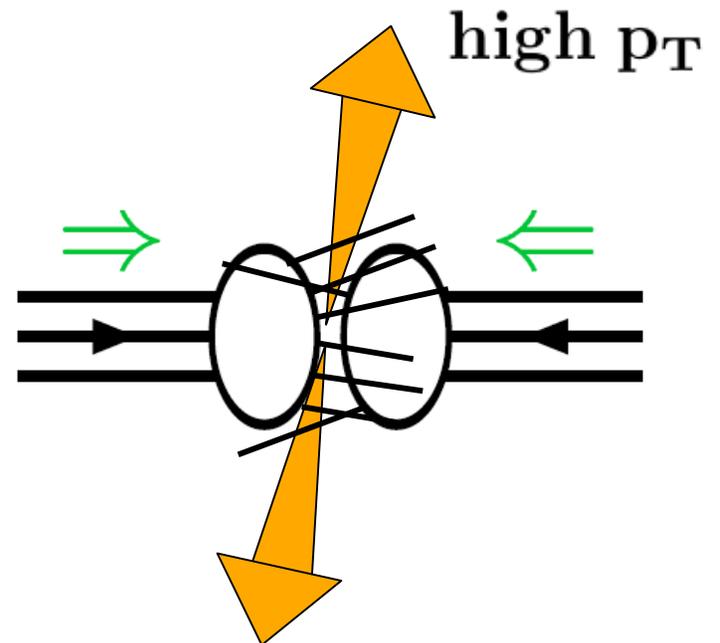
Polarized DIS



SLAC, CERN, DESY, Jlab, eRHIC

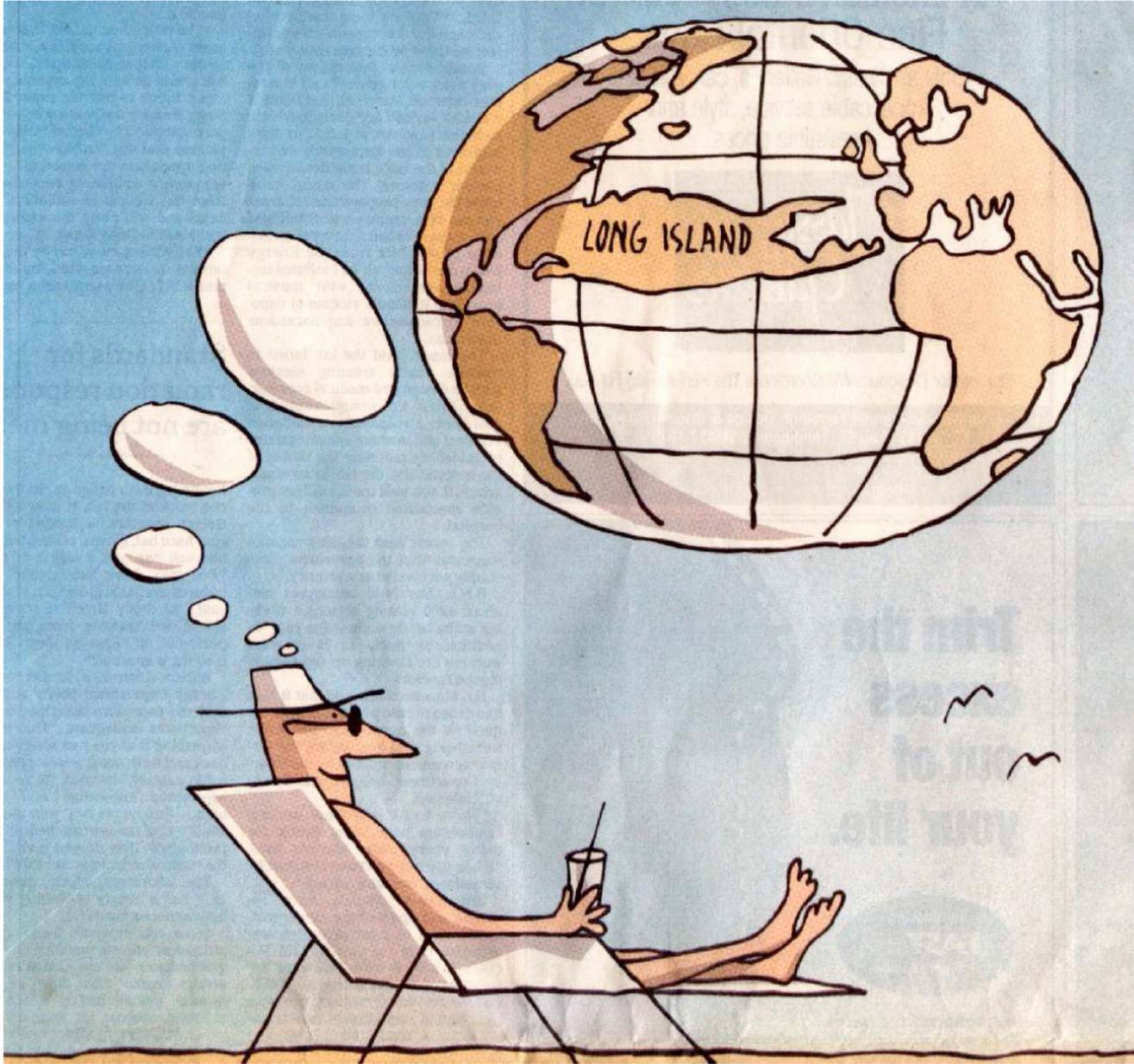
a powerful probe of quarks
(but sees gluons, too!)

pp scattering

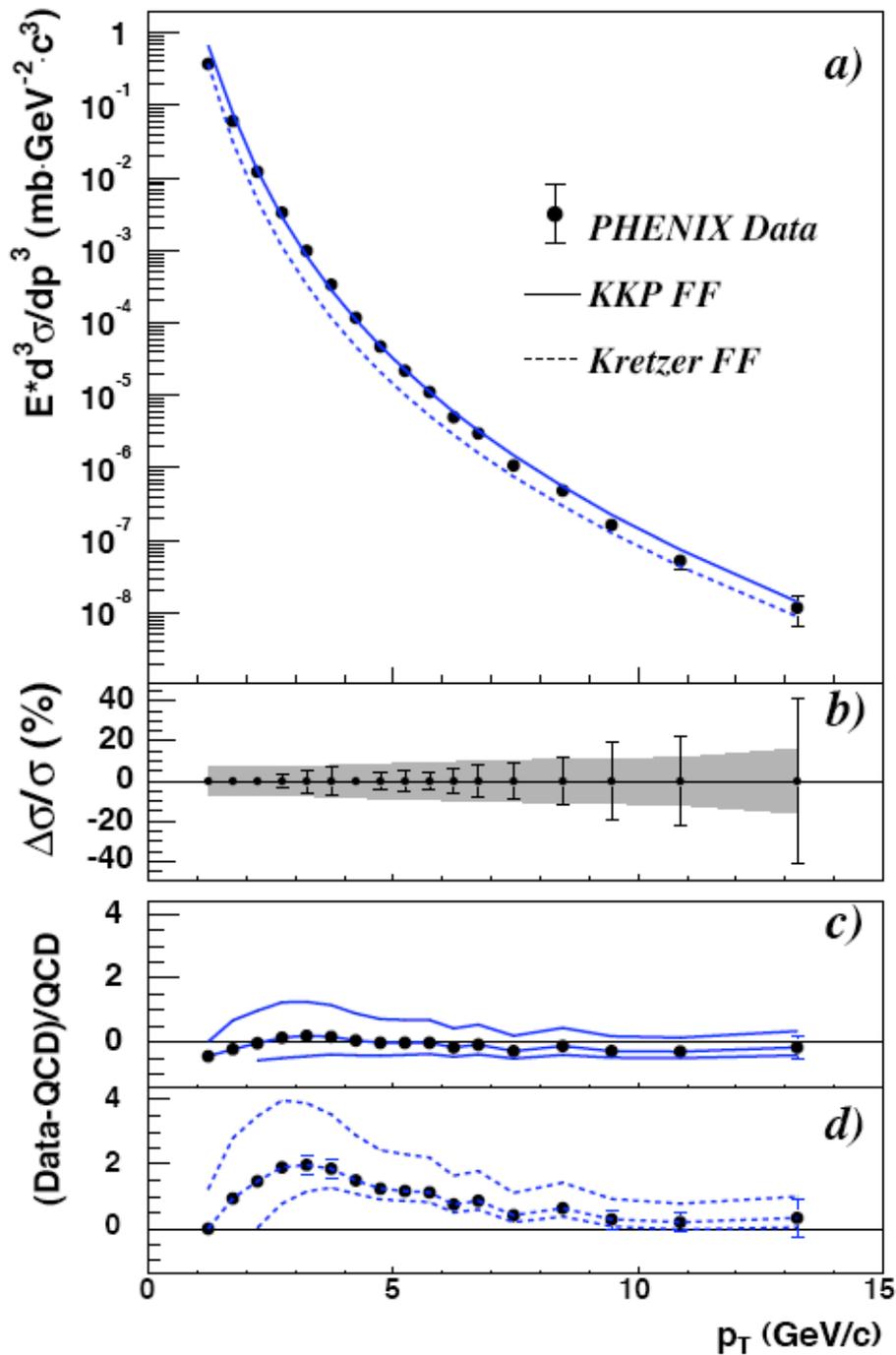


RHIC

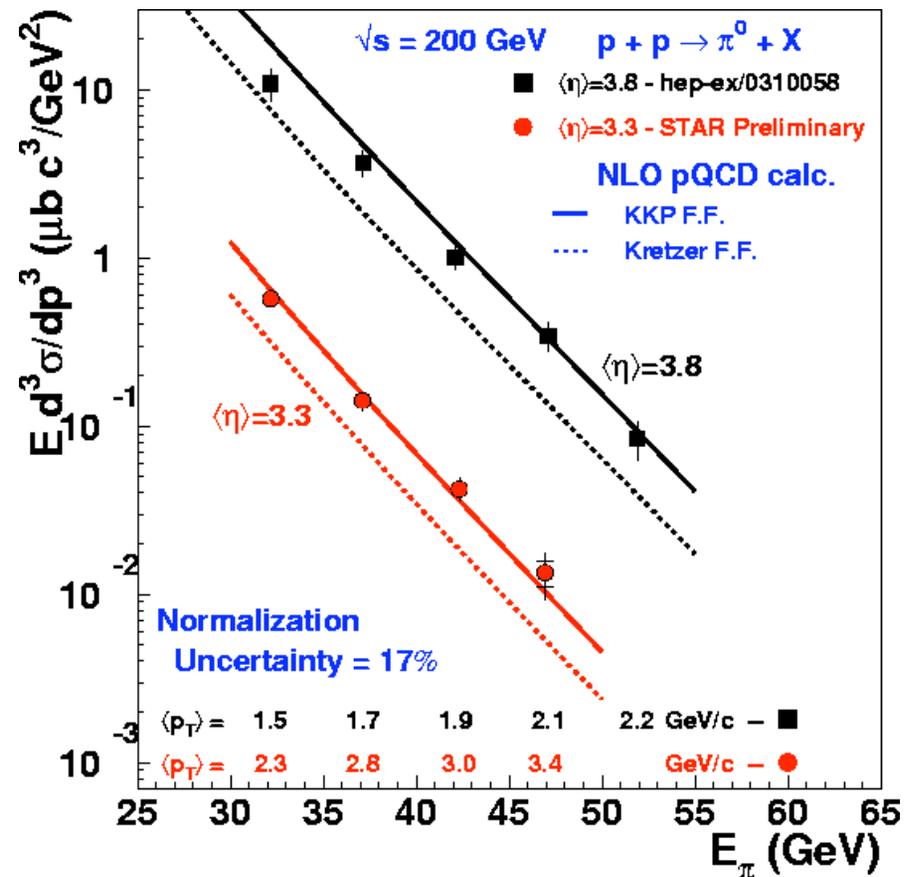
a powerful probe of gluons
(but sees quarks, too!)



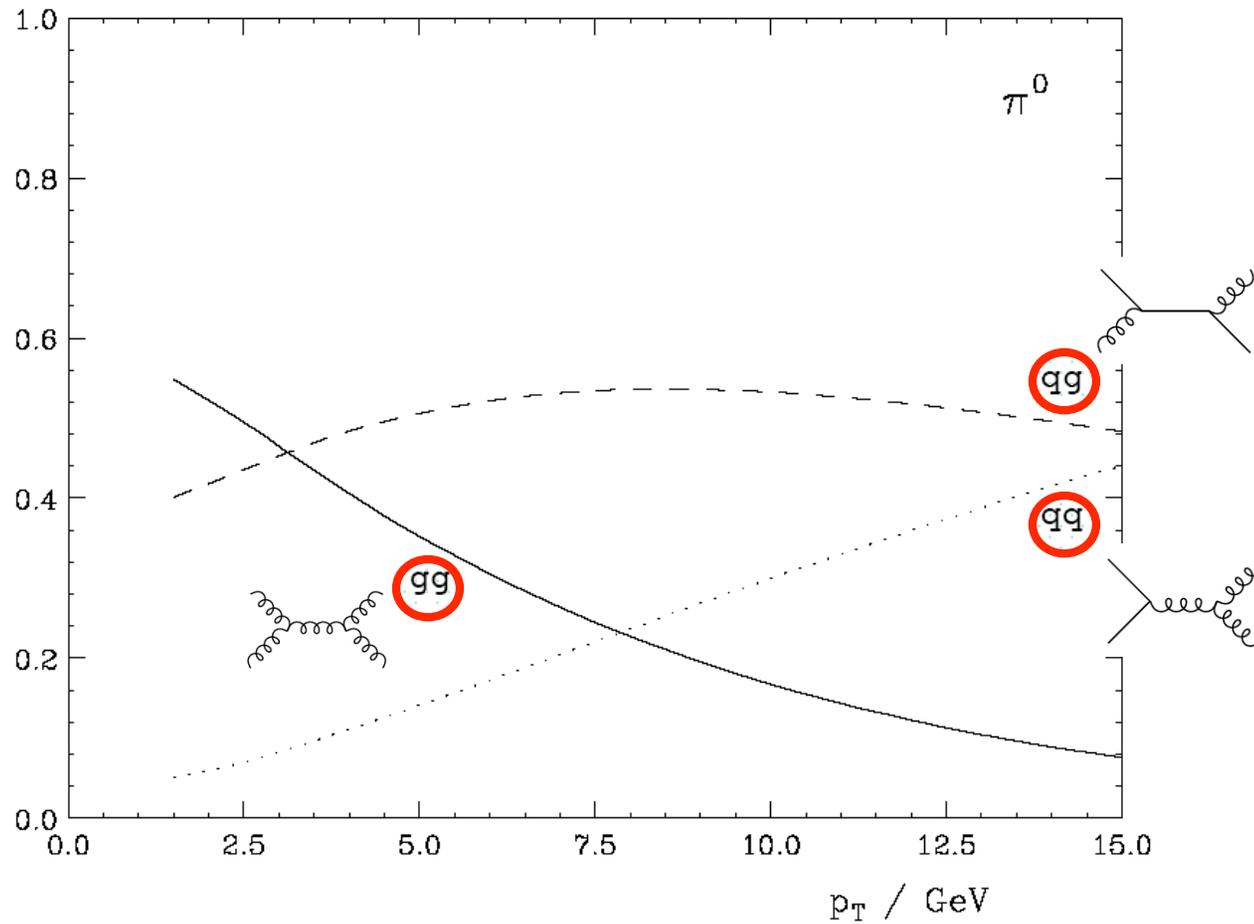
Probing gluon polarization Δg



$pp \rightarrow \pi^0 X$ at RHIC

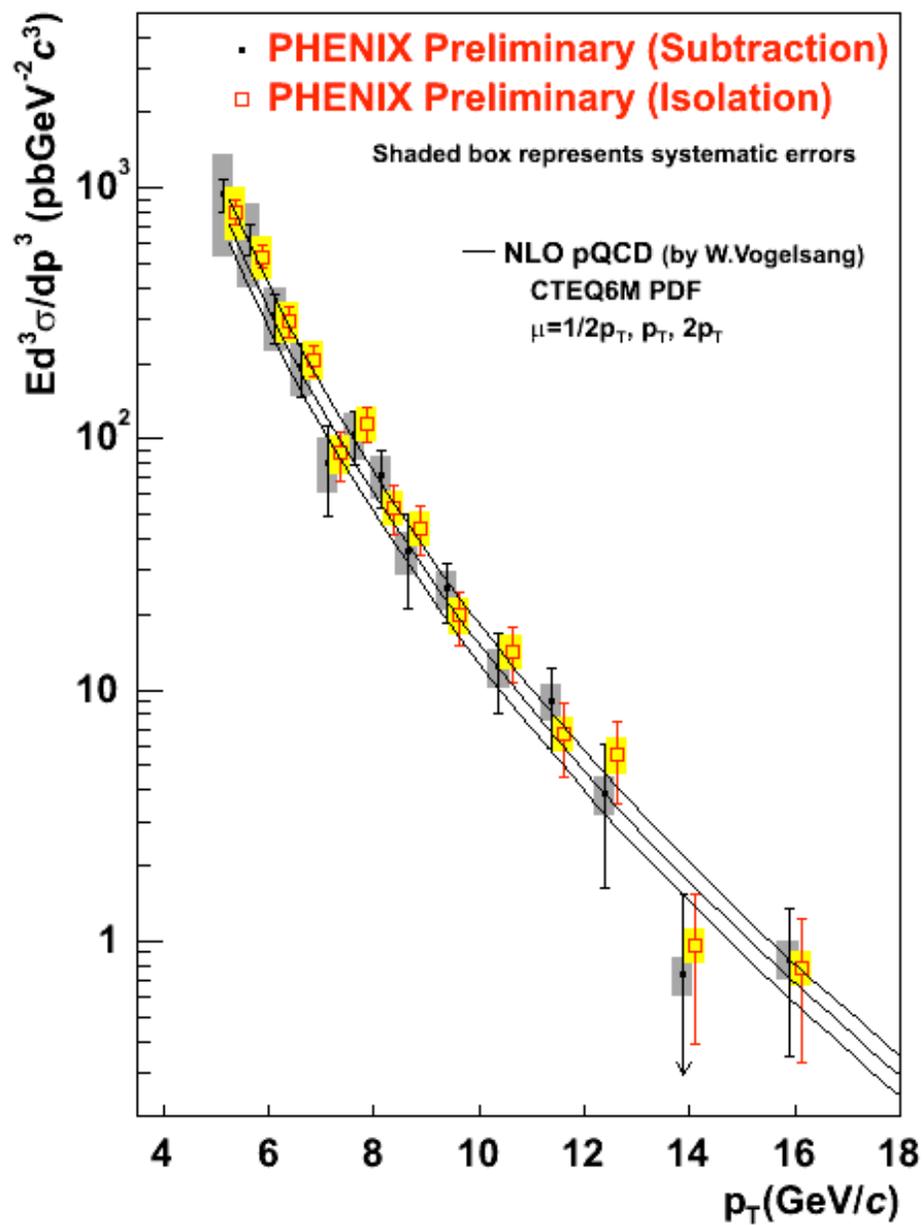
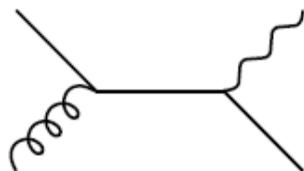


- contributions by partonic scatterings :

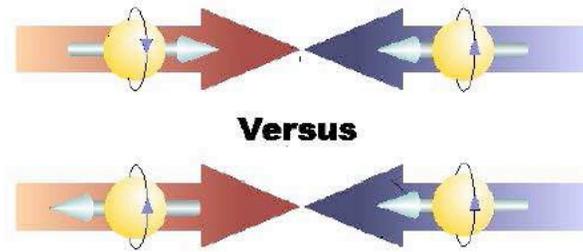


→ A good probe of gluons !

$$pp \rightarrow \gamma X$$



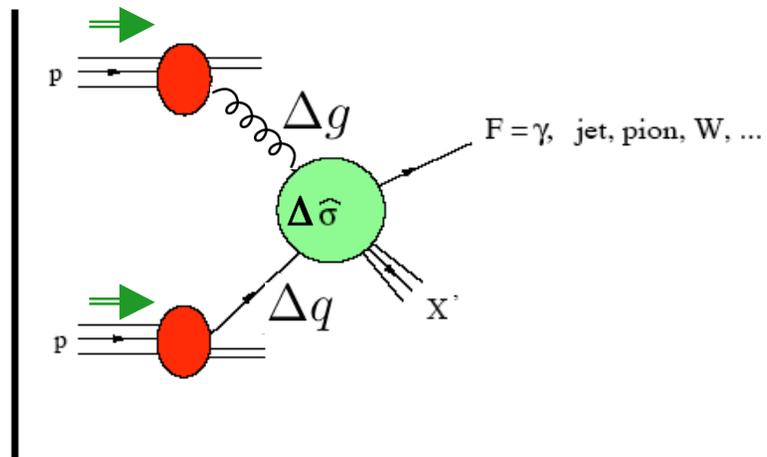
Polarized hadron collisions



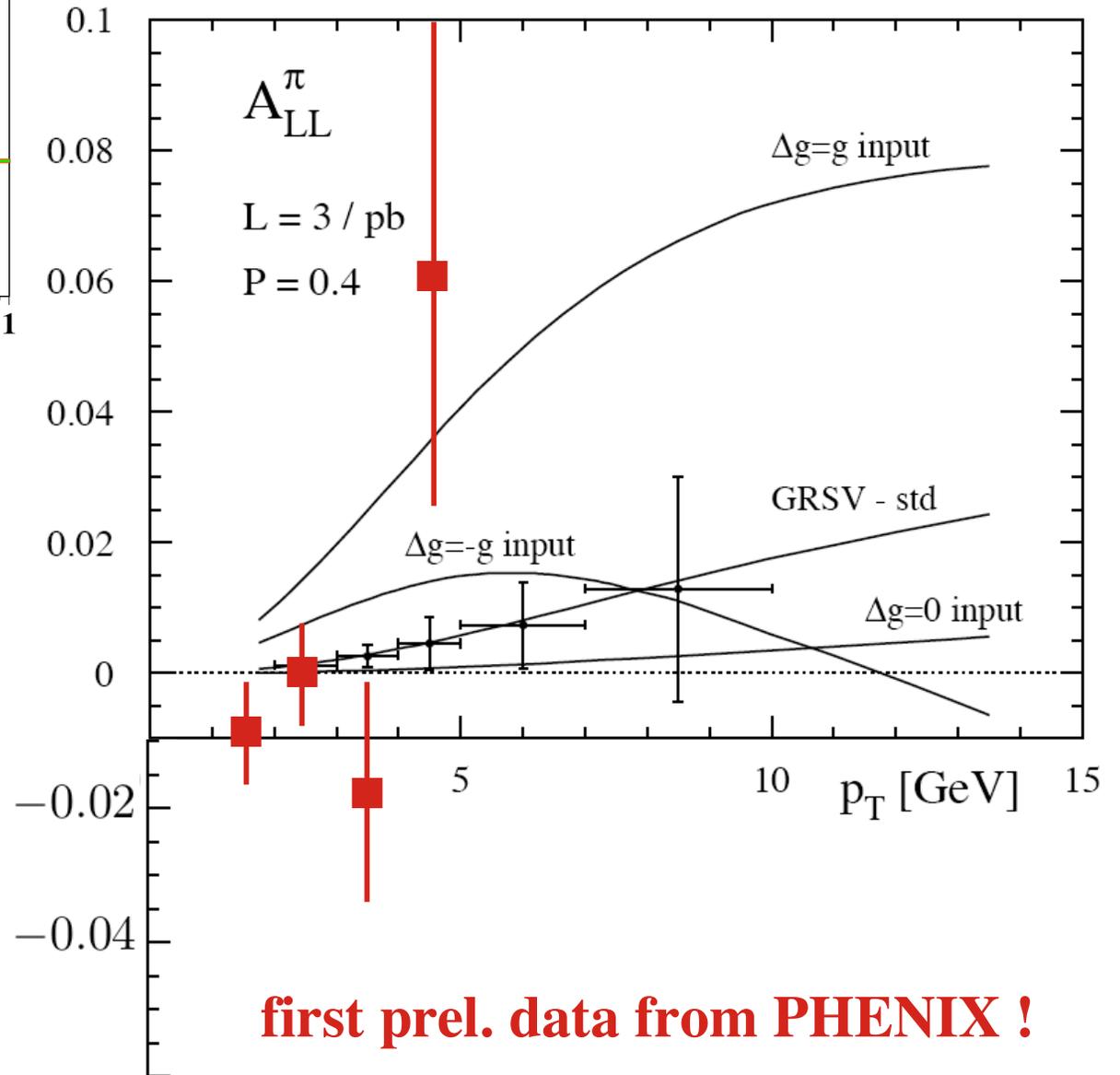
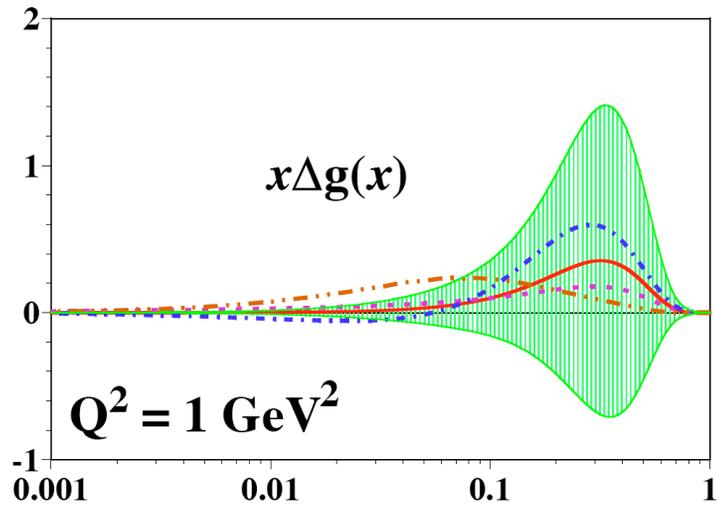
Spin asymmetry

$$A_{LL} \equiv \frac{\sigma_{++} - \sigma_{+-}}{\sigma_{++} + \sigma_{+-}} \equiv \frac{\Delta\sigma}{\sigma}$$

$$\Delta\sigma \sim$$

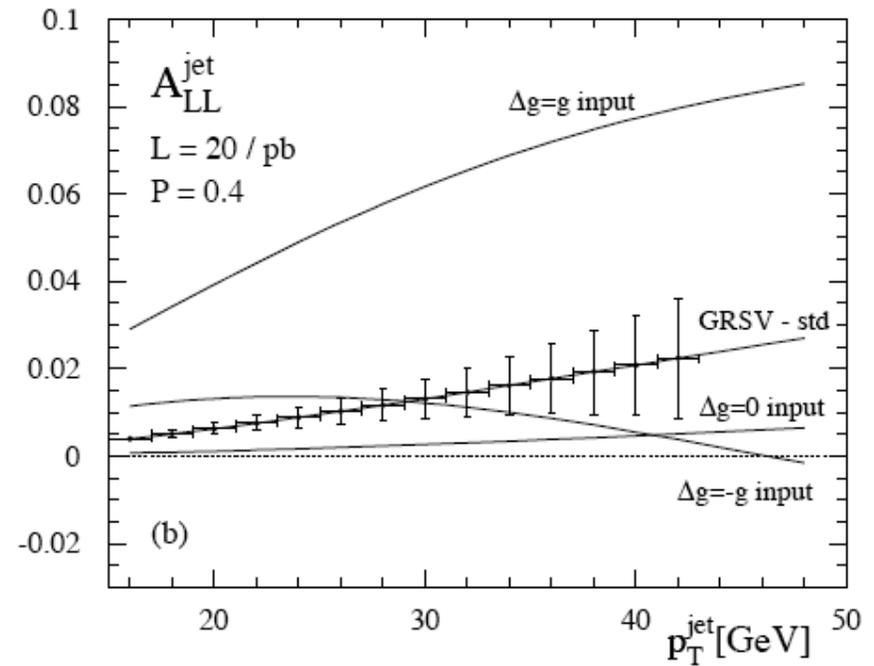
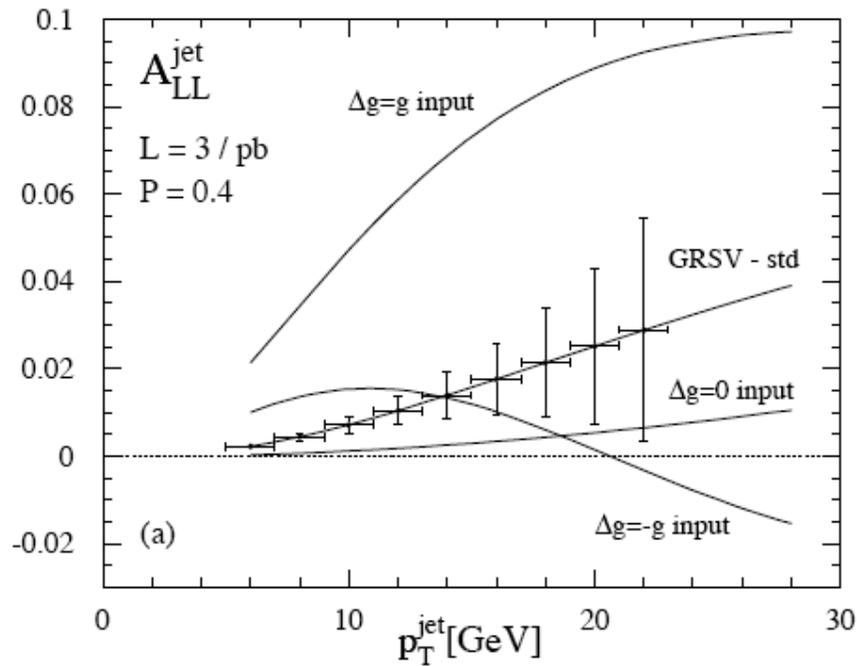


Example : $pp \rightarrow \pi^0 X$



first prel. data from PHENIX !

Spin asymmetry for jet production at STAR:



Jäger, Stratmann, WV

(de Florian, Frixione, Signer, WV)

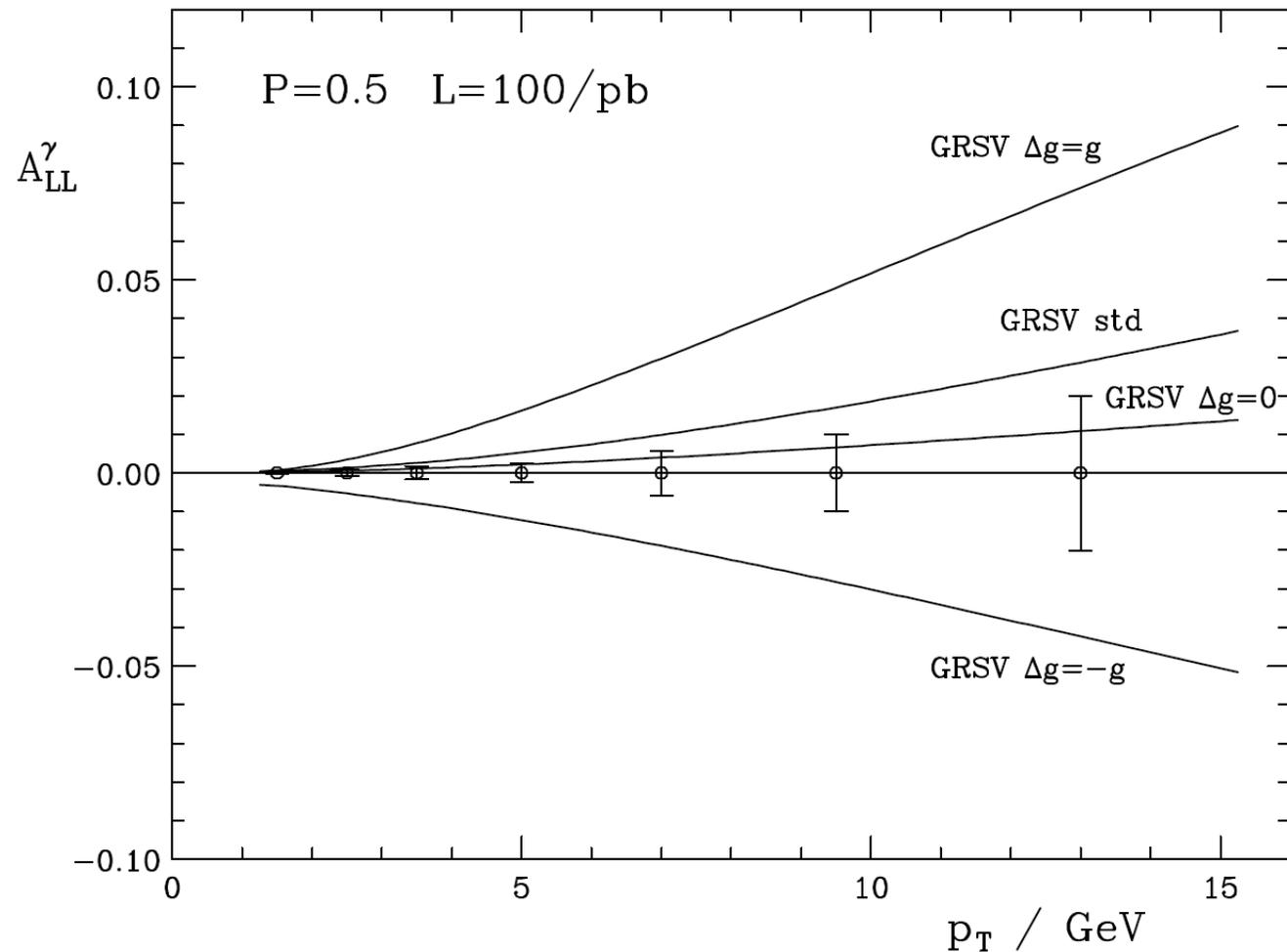
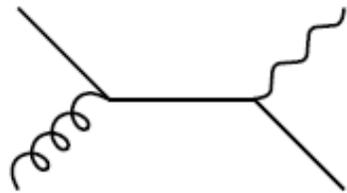
Mid / long-term at RHIC:

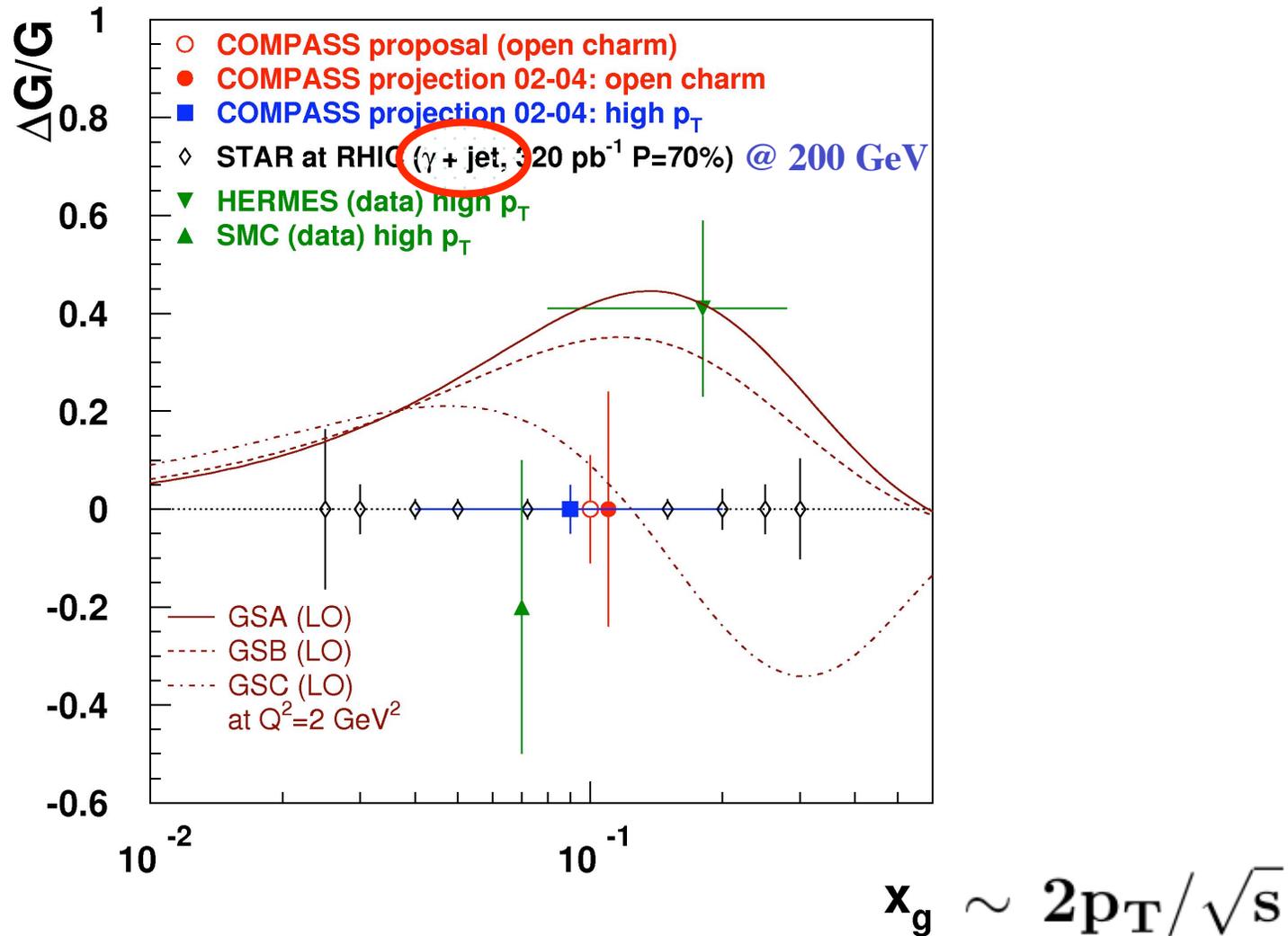
“rare probes”

- gluon polarization from $pp \rightarrow \gamma X$

$L=100/\text{pb}$

Frixione, WV



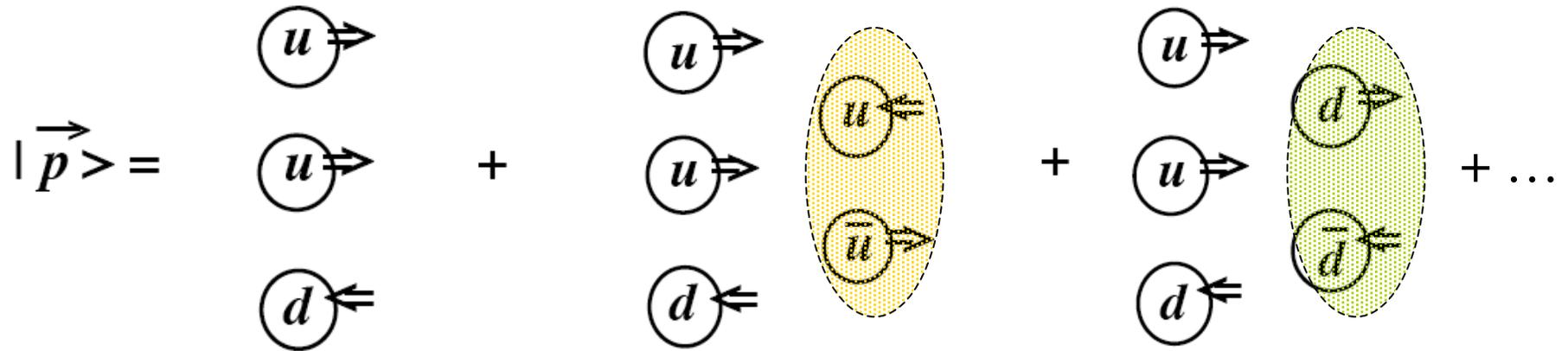


typically, $0.025 < x_g < 0.3$ @ $\sqrt{s} = 200 \text{ GeV}$

$0.01 < x_g < 0.1$ @ $\sqrt{s} = 500 \text{ GeV}$

Further information

on quark distributions



most models predict $\Delta\bar{u} > 0$ $\Delta\bar{d} < 0$

$$\Delta\bar{u} - \Delta\bar{d} \begin{matrix} > \\ < \\ = \end{matrix} 0 ?$$

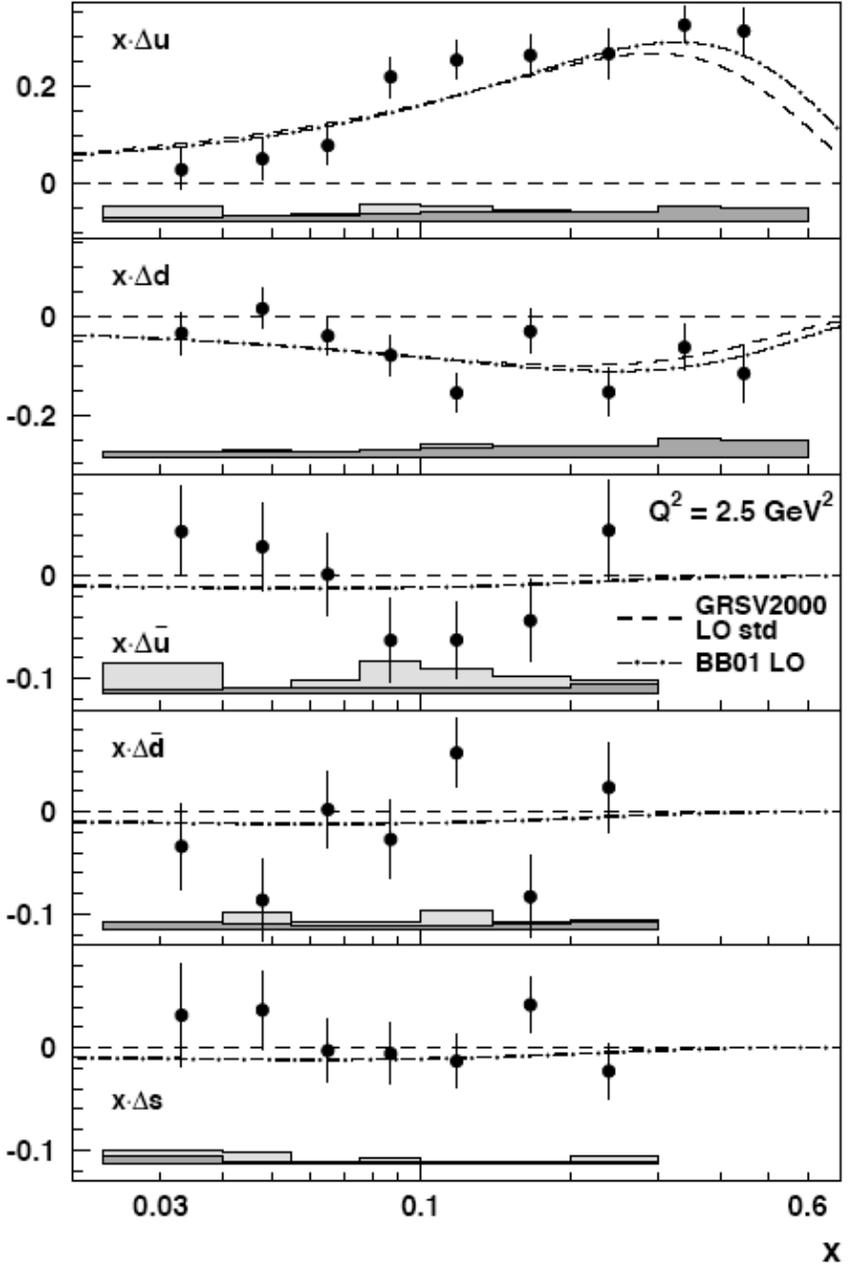
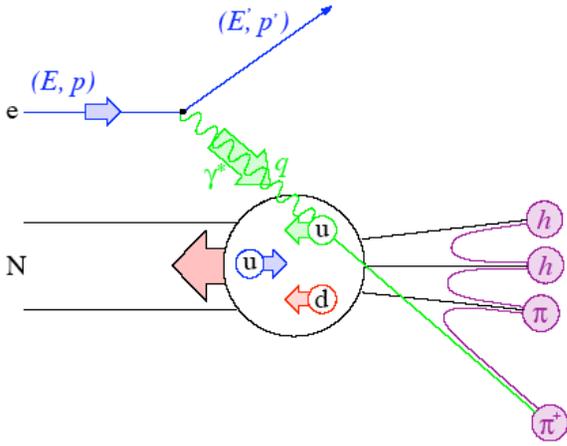
• considerable interest :

* SU(2) breaking in sea (meson cloud models, Pauli exclusion, . . .)
 (Thomas,Signal,Cao; Diakonov,Goeke,Polyakov,Weiss; Glück,Reya; Schäfer,Fries; Kumano; Wakamatsu)

* strange quark polarization

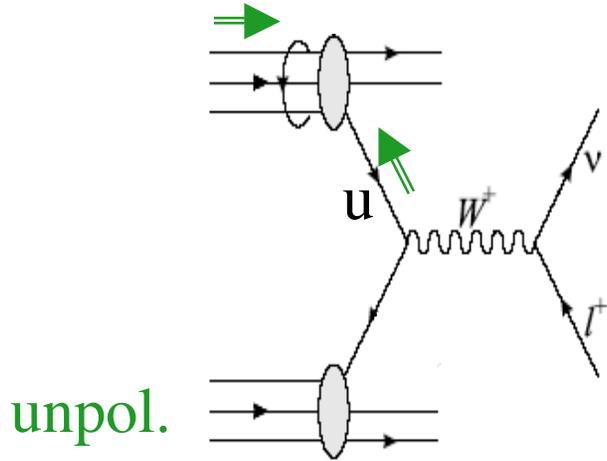
(Ellis,Karliner et al.; Brodsky,Ma Bo-Qiang et al; . . .)

HERMES



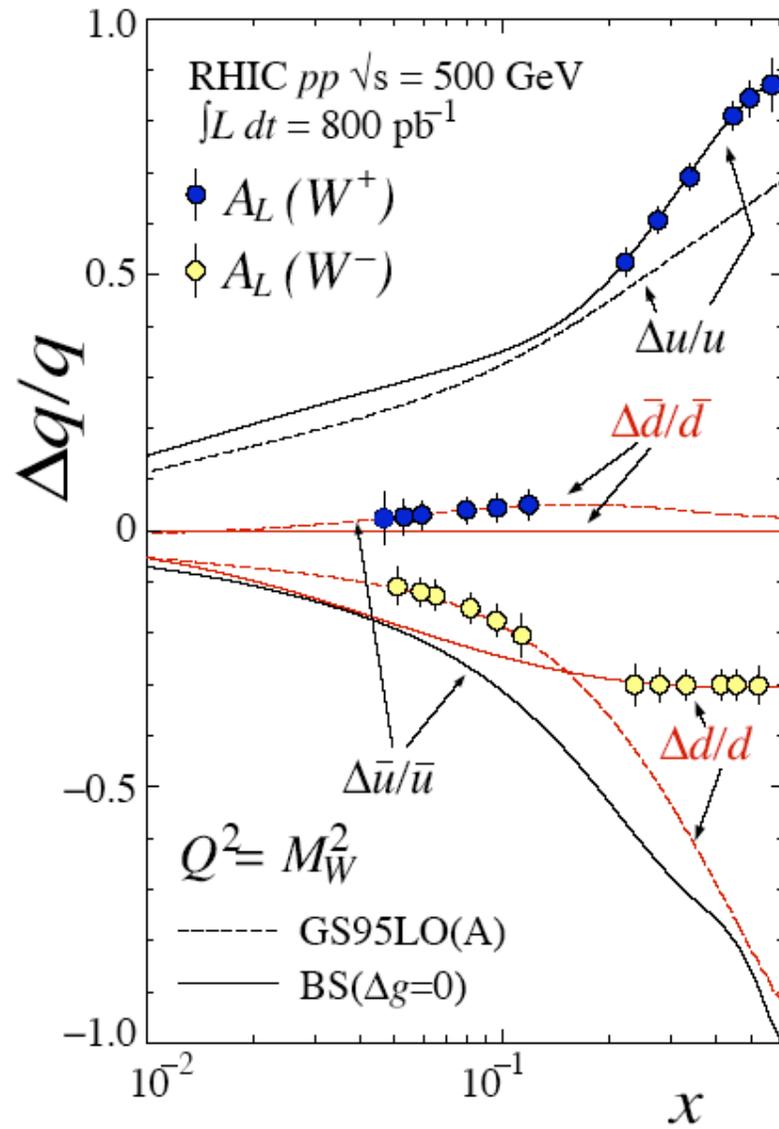
at RHIC:

W boson production



$$A_L = \frac{\sigma_+ - \sigma_-}{\sigma_+ + \sigma_-}$$

parity violating



Access to orbital angular momentum ?

- recall, in elastic scattering we had

$$\langle P' | J^\mu | P \rangle \sim \chi_{s'}^\dagger \left(G_E(Q^2), \frac{i\vec{\sigma} \times \vec{q}}{2m_p} G_M(Q^2) \right) \chi_s$$

where $G_E(0) = 1$ $G_M(0) = 2.79$

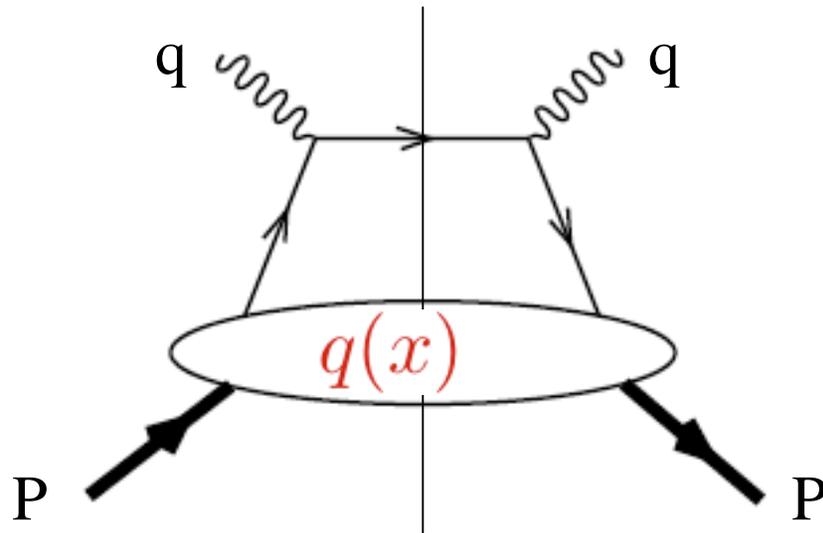
- measurement of $G_M(0)$ requires non-zero momentum transfer
- on the other hand, magnetic moment is

$$G_M(0) \sim \int d^3x \langle P | \frac{1}{2} \vec{x} \times \vec{J} | P \rangle$$

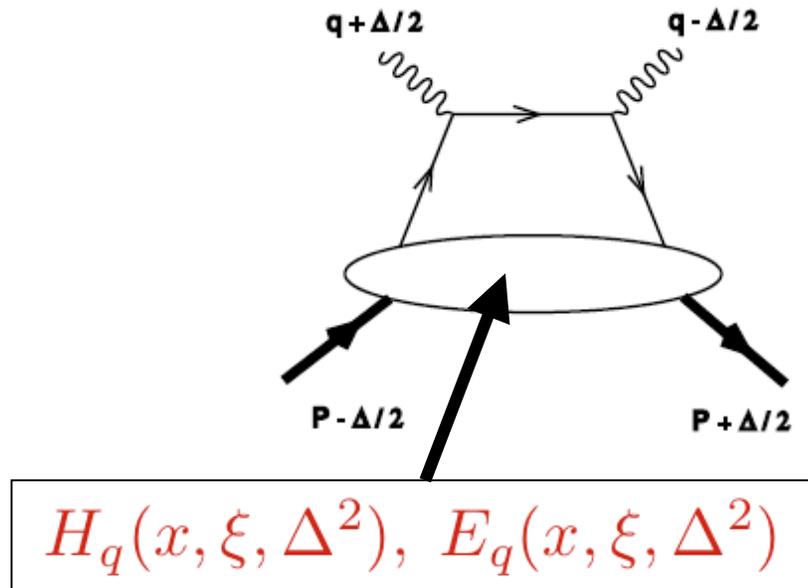

- operators for angular momentum involve explicit factor \vec{x}

$$L_q = \int d^3x \langle P, \frac{1}{2} | \psi_q^\dagger \left[\vec{x} \times \left(-i \vec{\nabla} \right) \right]_3 \psi_q | P, \frac{1}{2} \rangle$$

- \rightarrow need an **off-forward** process!
- DIS isn't like that:



- X. Ji: “Deeply-virtual Compton scattering”



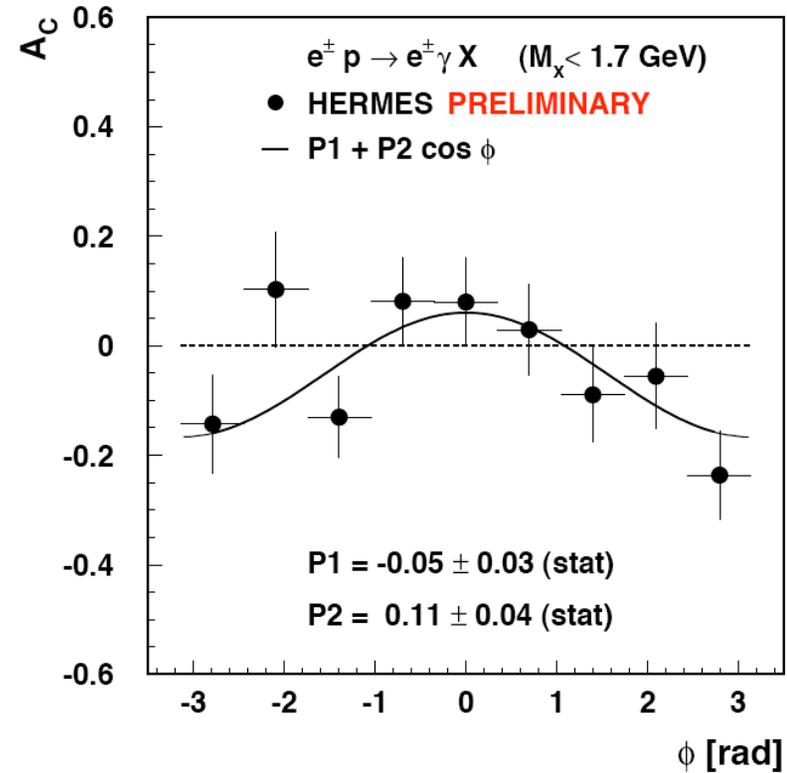
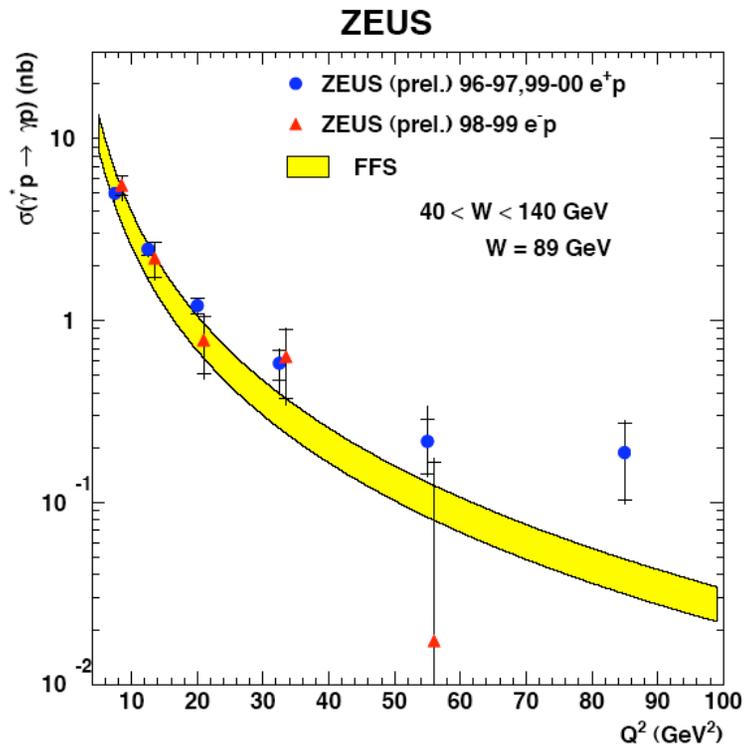
- $H_q(x, \xi, \Delta^2)$ and $E_q(x, \xi, \Delta^2)$ are related to both ordinary pdf's and to form factors:

“Generalized parton distributions”

$$J_q = \frac{1}{2} \lim_{\Delta^2 \rightarrow 0} \int dx x [H_q(x, \xi, \Delta^2) + E_q(x, \xi, \Delta^2)]$$

- measurements have begun:

HERMES, H1, ZEUS, CLAS

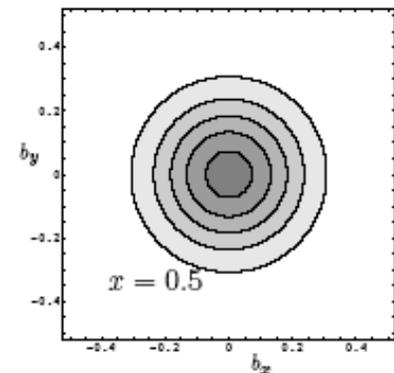
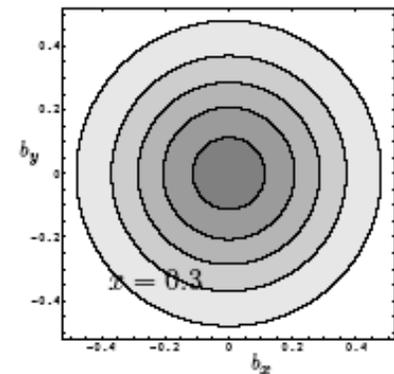
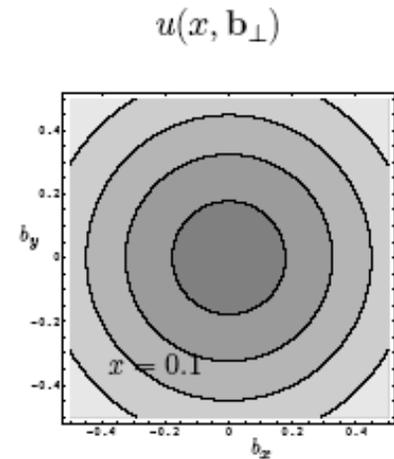
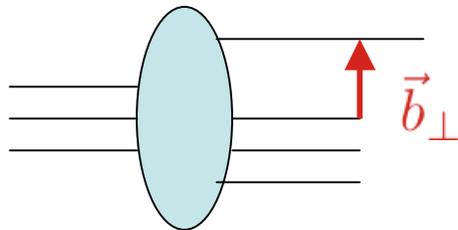


- theory: Belitsky, Müller; Frankfurt, Freund, Strikman; Ji, Osborne ...

- orbital angular momentum
- exclusive processes in QCD
- spatial distributions of partons in proton

$$q(x, \vec{b}_\perp) = \int d^2 \Delta_\perp e^{-i\vec{b}_\perp \cdot \vec{\Delta}_\perp} H_q(x, 0, -\Delta_\perp^2)$$

Burkardt; Ralston, Pire; Diehl; Belitsky, Ji, Yuan



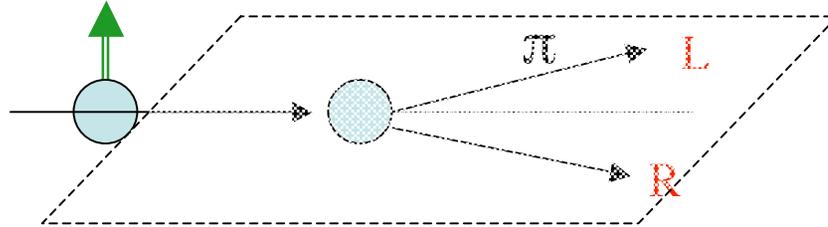
Transverse polarization



- hadronic single-spin asymmetries, e.g. in $\vec{p}p \rightarrow \pi X$

$$A_L \equiv \frac{\sigma_{+-} - \sigma_{-+}}{\sigma_{++} + \sigma_{--}} = 0 \quad \text{in QCD}$$

$$A_N \equiv \frac{\sigma_{\uparrow-} - \sigma_{\downarrow+}}{\sigma_{\uparrow+} + \sigma_{\downarrow-}} \neq 0 \quad \text{allowed}$$



$$A_N = \frac{L - R}{L + R}$$

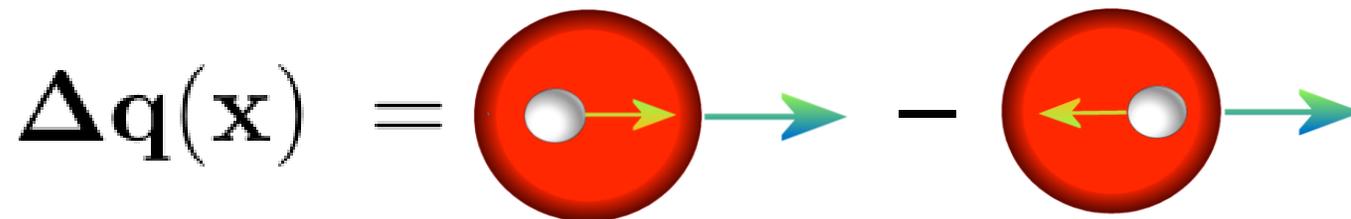
- in helicity basis :

$$|\uparrow\rangle = \frac{1}{\sqrt{2}} (|+\rangle + i|-\rangle) \quad |\downarrow\rangle = \frac{1}{\sqrt{2}} (|+\rangle - i|-\rangle)$$

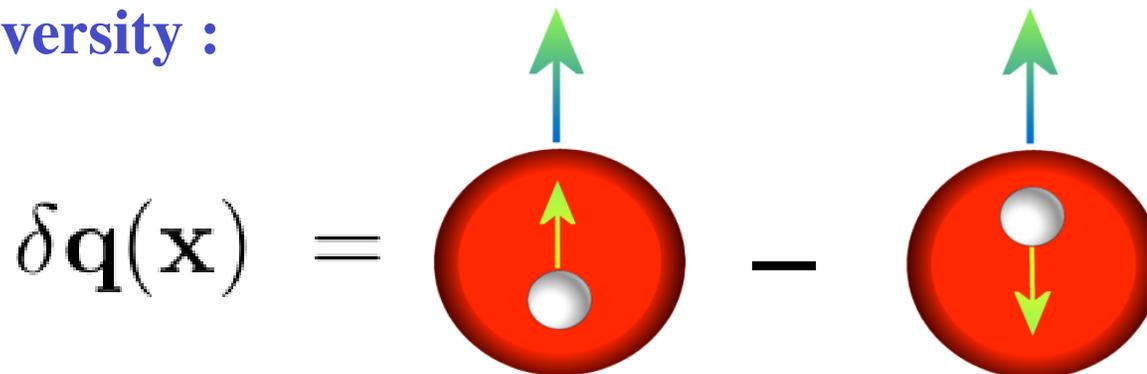
$$A_N \sim \text{Im} \left\{ \begin{array}{c} \text{Diagram of a red oval with a vertical dashed line through its center. Two blue lines extend from the top-left and top-right corners, and two blue lines extend from the bottom-left and bottom-right corners. The bottom-left line is labeled } p_R \text{ and the bottom-right line is labeled } p_L. \end{array} \right\}$$

- the simplest idea: transverse nucleon polarization carried by quark

Helicity :



Transversity :



Ralston,Soper; Jaffe, Ji; ...

- a little more precisely ...

$$\Delta q(x) = \text{[Diagram 1]} - \text{[Diagram 2]}$$

The diagram shows two gray ellipses representing a cross-section of a cylinder. Each ellipse has a vertical line through its center. Four lines extend from the top and bottom edges of each ellipse. In the first diagram, all four lines have a red '+' sign. In the second diagram, the top two lines have red '-' signs, and the bottom two lines have red '+' signs.

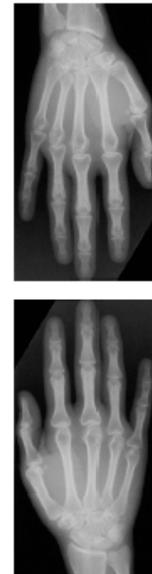
$$\delta q(x) = \text{[Diagram 3]} - \text{[Diagram 4]}$$

The diagram shows two gray ellipses. In the first diagram, all four lines extending from the top and bottom edges have red '+' signs. In the second diagram, the top two lines have red '+' signs, and the bottom two lines have red '-' signs.

- in helicity basis:

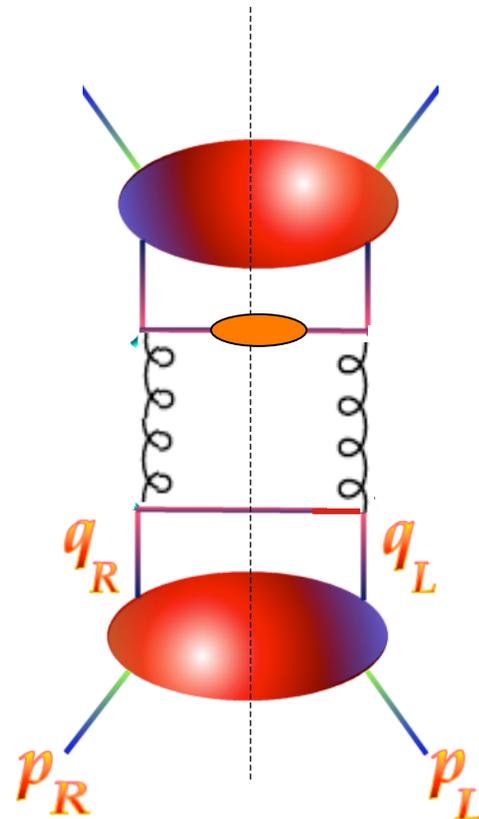
$$\delta q(x) \sim \text{[Diagram 5]}$$

The diagram shows a single gray ellipse with a vertical line through its center. Four lines extend from the top and bottom edges. The top-left and bottom-left lines have red '+' signs, while the top-right and bottom-right lines have red '-' signs.



helicity-flip,
 χ_{SB}, \dots

- back to single-spin asymmetry:



← transversity

- may arise only as

$$\frac{m_q}{p_T} \alpha_s \ll 1$$

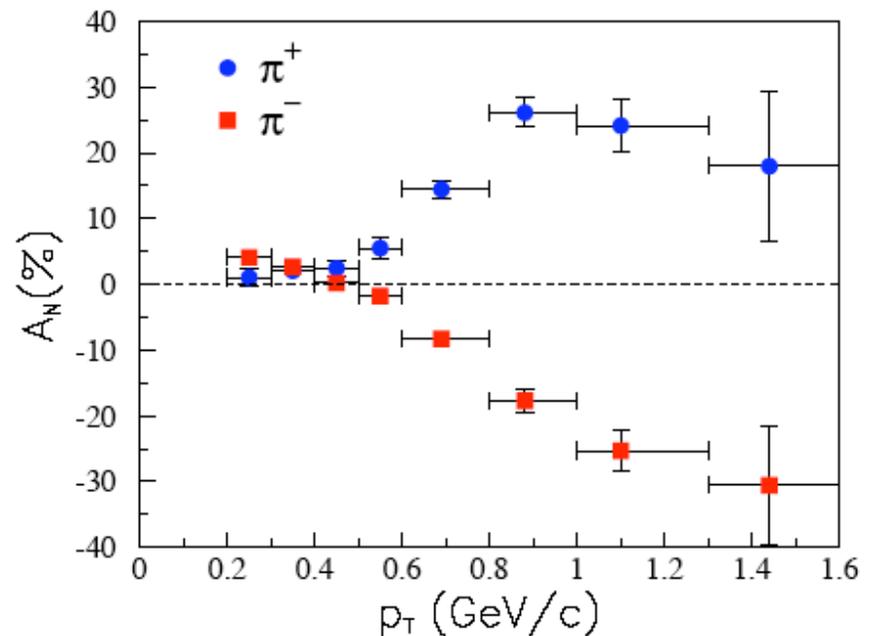
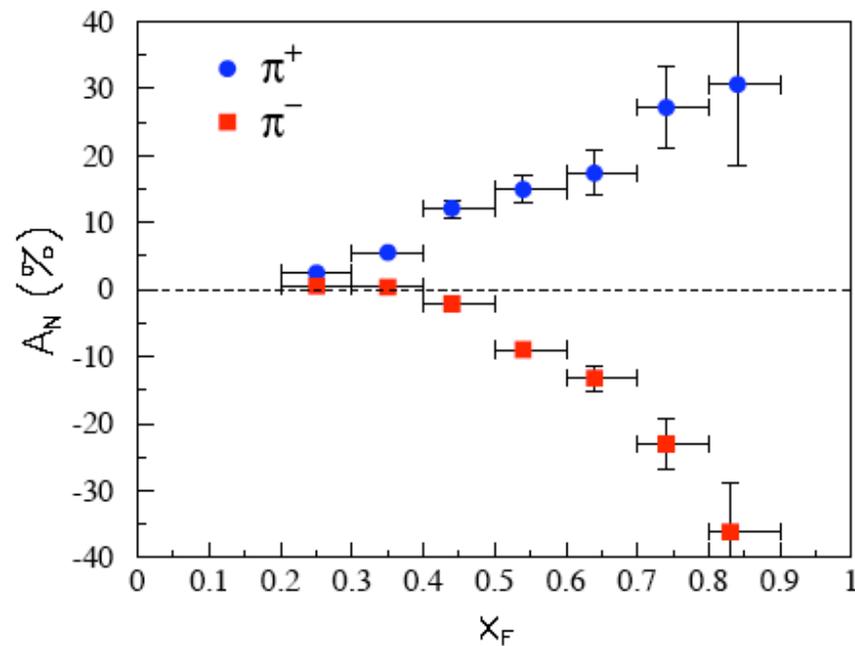
(Kane, Pumplin, Repko)

- the lesson : A_N is power-suppressed as $1/p_T \dots$
- \dots and is therefore small ?

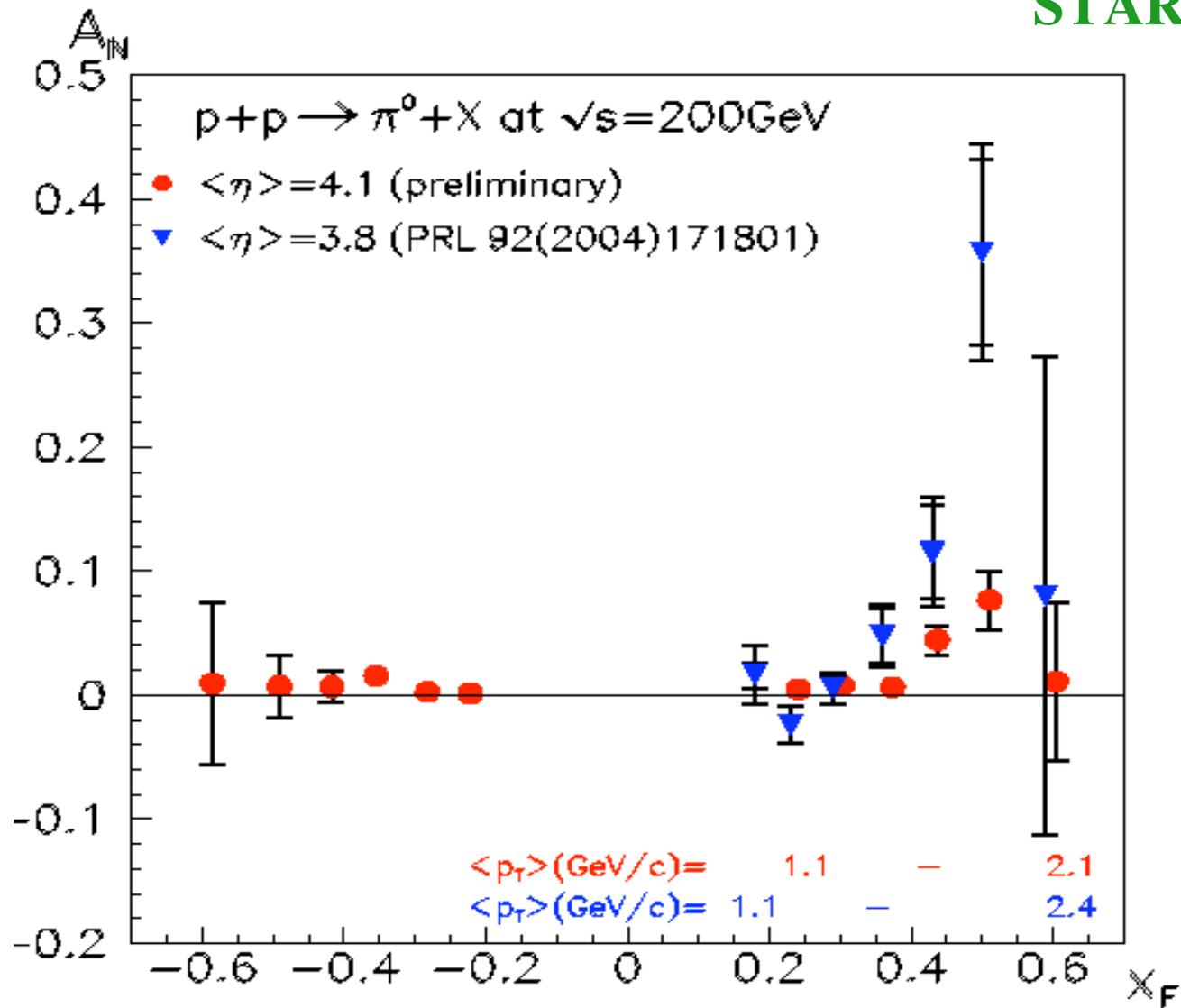
- in striking contrast :

- * large A_N seen in fixed-target experiments at
BNL,ANL,Fermilab,Serpukhov

- * E704 ('96) :

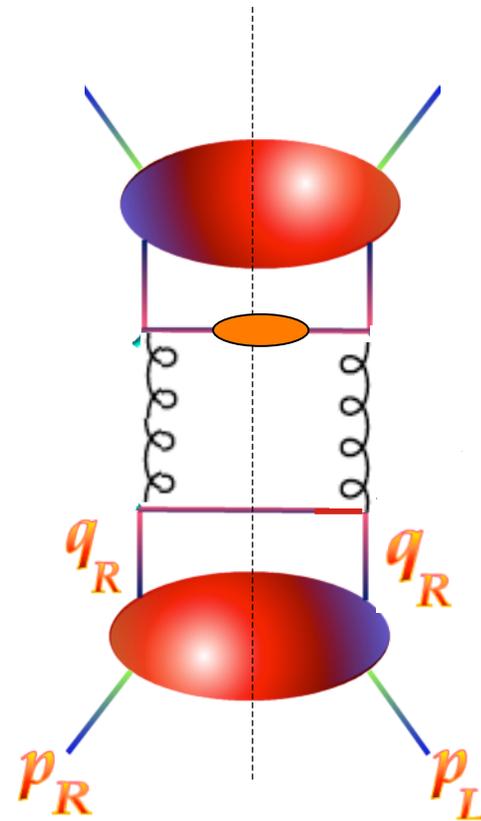


STAR



Much theoretical activity:

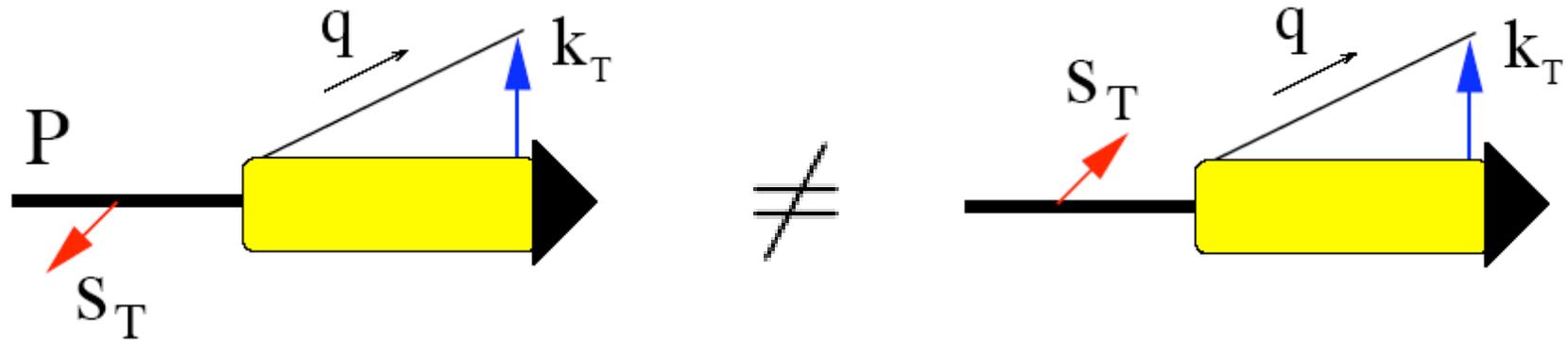
- how to avoid quark helicity flip ?



- requires transverse momentum k_T for quark
- interference of $J_z^p = +\frac{1}{2}$ and $J_z^p = -\frac{1}{2}$ amplitudes
- involves quark orbital angular momentum

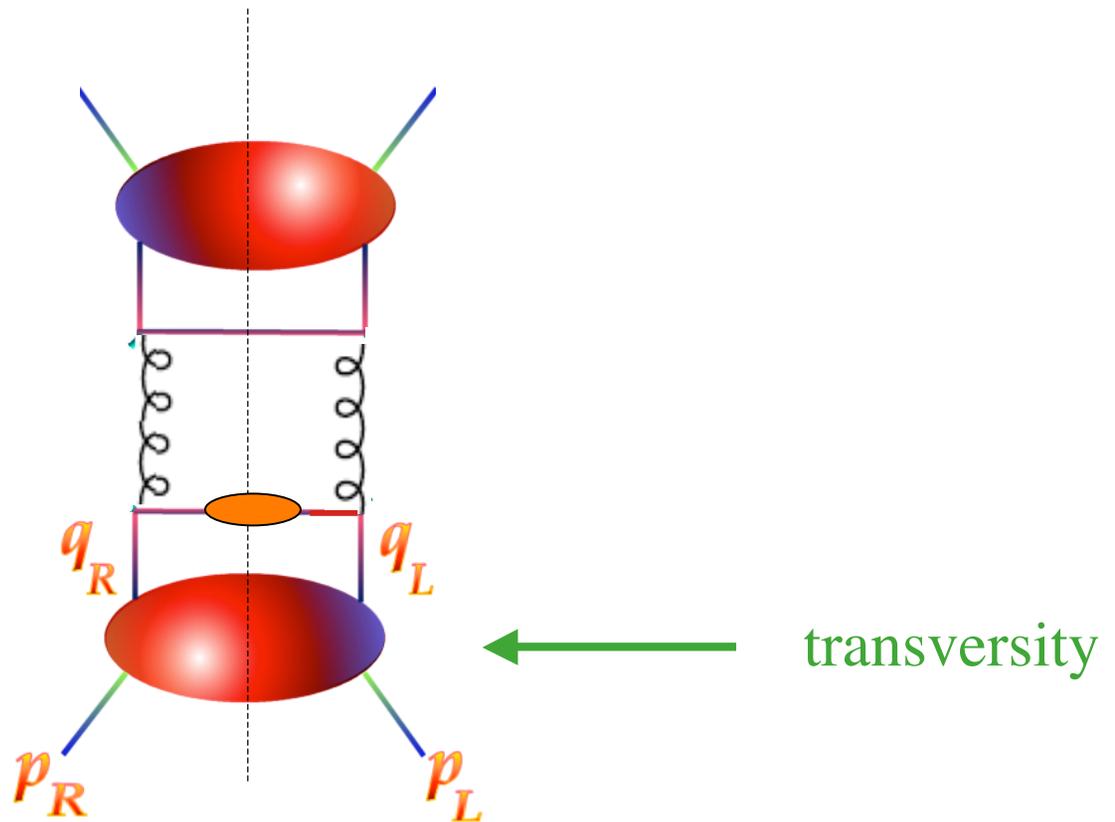
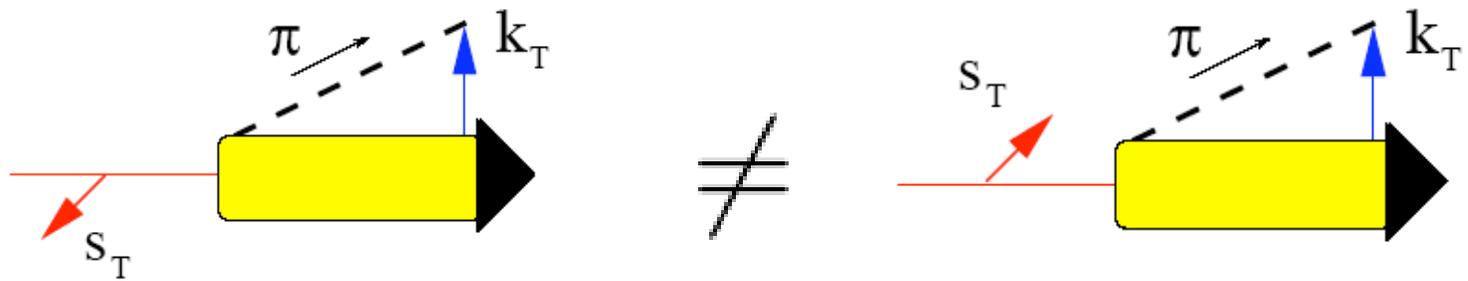
“Sivers effect”

- realized if



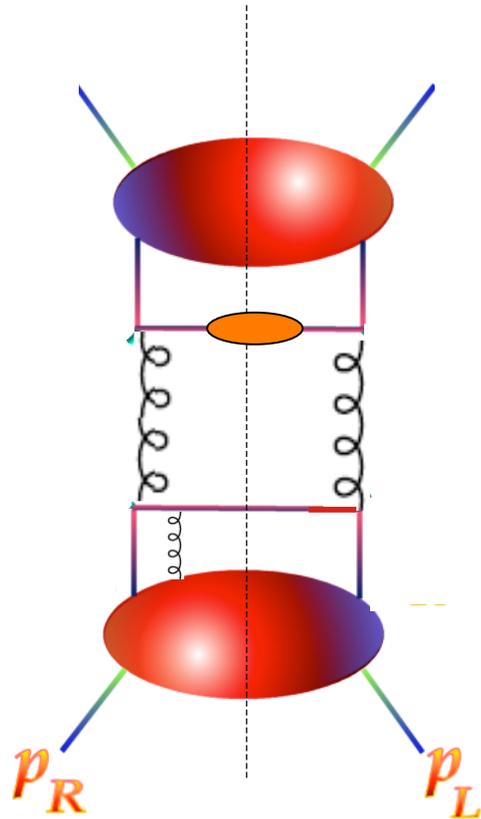
- correlation $\sim \vec{S}_T \cdot (\vec{P} \times \vec{k}_T)$
- thought of as arising from interaction of struck quark with gluon field (Brodsky,Hwang,Schmidt; Collins; Belitsky,Ji,Yuan; Boer,Mulders,Pijlman)
- steeply falling cross sections \rightarrow large effects possible

- Collins '93 : related effect in fragmentation



- yet another possibility :
“quark-gluon correlation functions”

Qiu, Sterman; Efremov, Teryaev; Koike ...

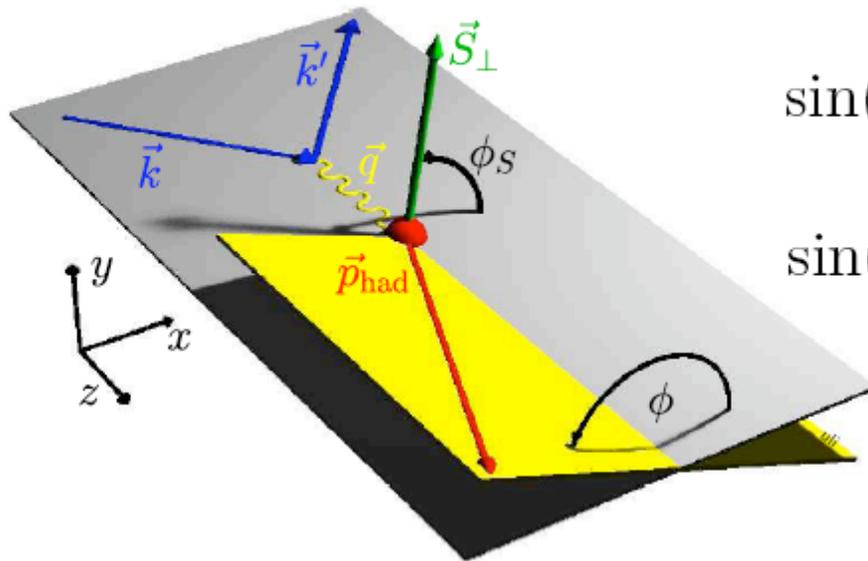


- nonperturbative models : Boros, Liang, Meng; Ostrovsky, Shuryak; ...
- still a lot to learn about the origins of single-spin asymmetries !

Some observables are directly sensitive to \vec{k}_T :

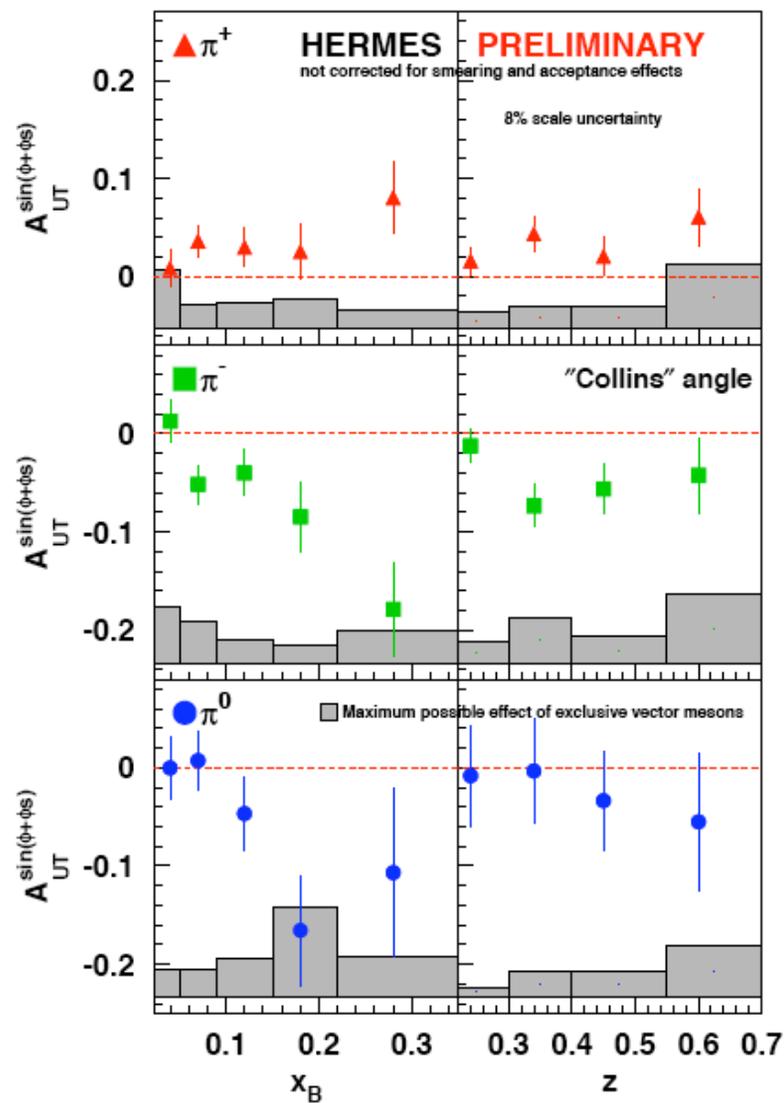
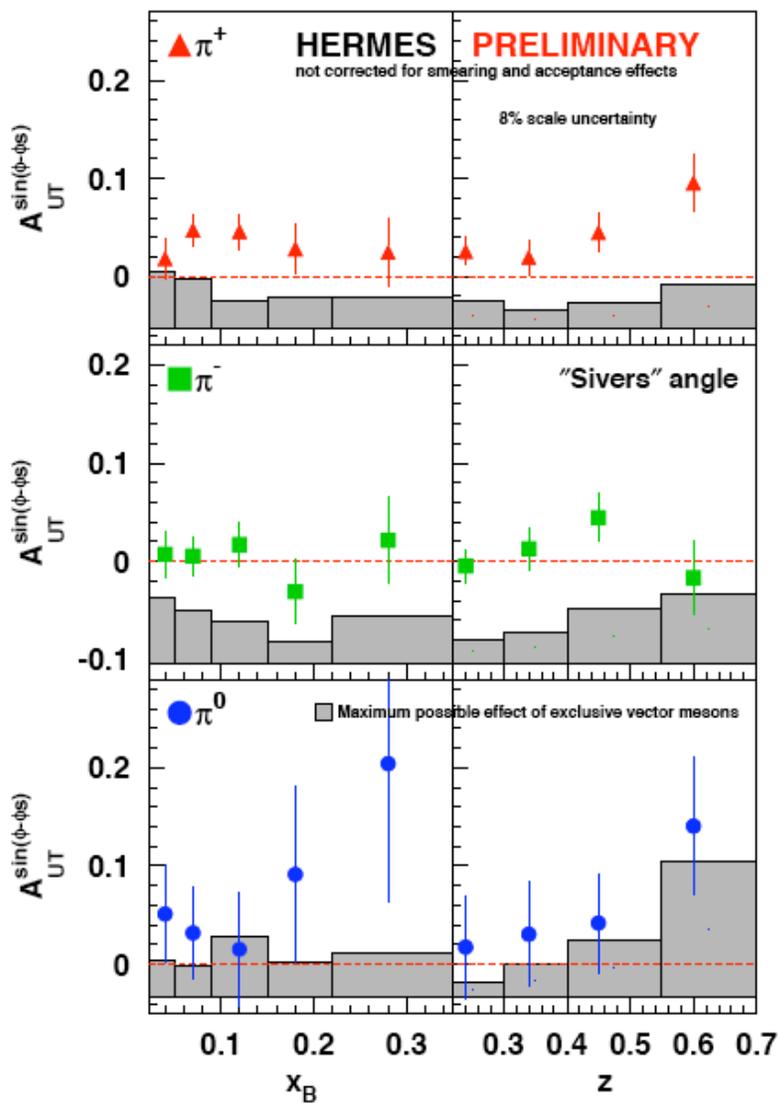
- example : $ep^\uparrow \rightarrow e\pi X$

Collins



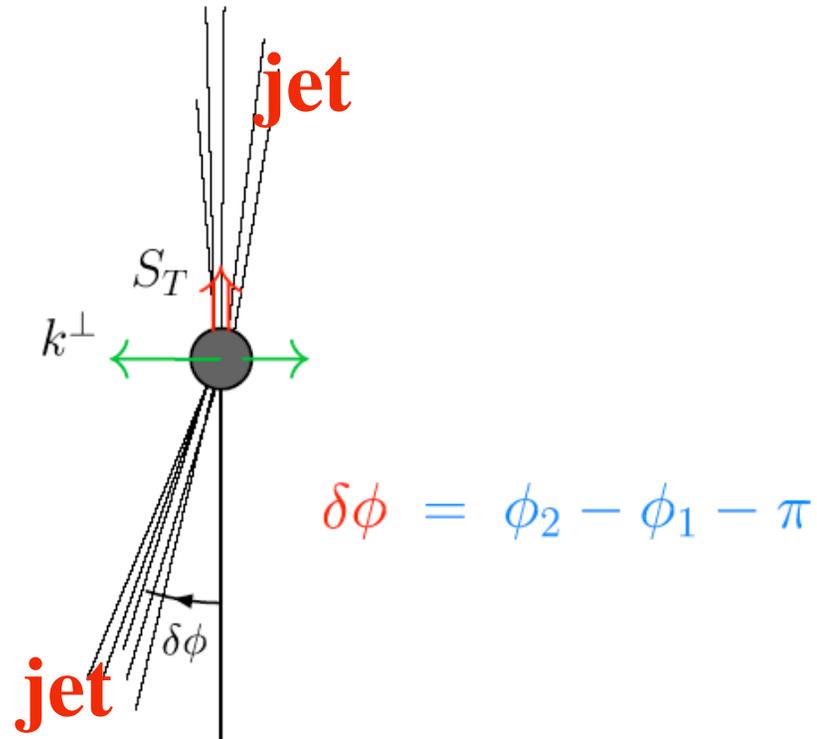
$$\sin(\phi - \phi_S) \sum_q e_q^2 f_{1T}^{\perp,q}(x) D_q(z)$$

$$\sin(\phi + \phi_S) \sum_q e_q^2 \delta q(x) H_1^{\perp,q}(z)$$



at RHIC:

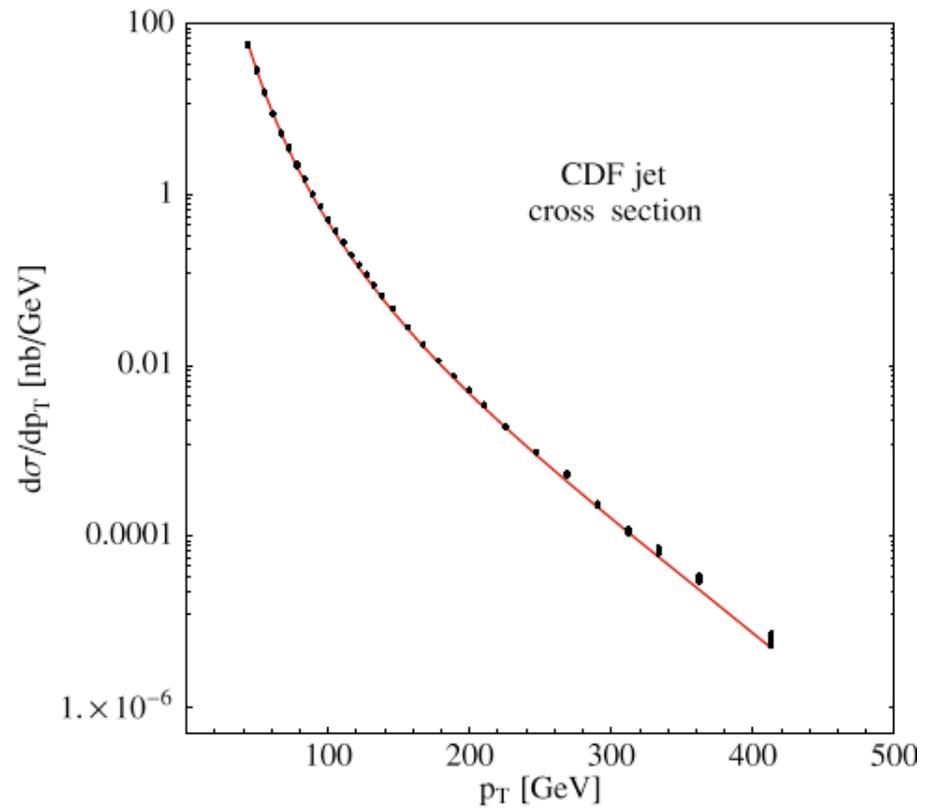
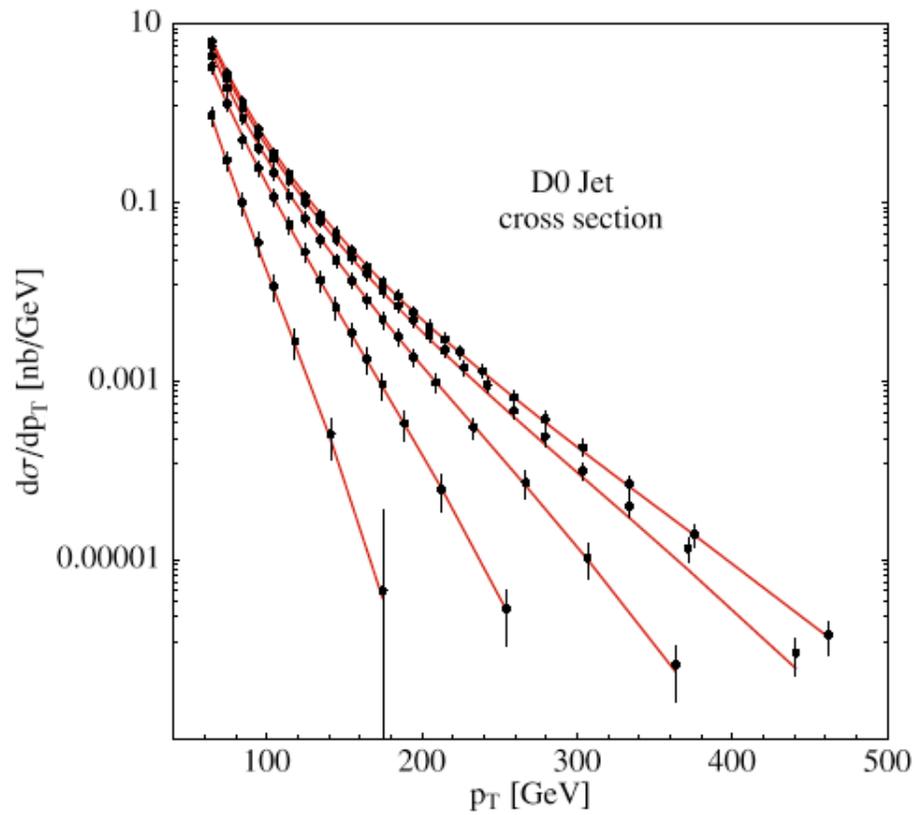
- consider $p^\uparrow p \rightarrow \text{jet jet } X$



Conclusions & Outlook:

- one can address & answer the question
“What carries the proton spin?”
- future promises to be as exciting as past was:
lepton-nucleon expt. and RHIC provide a wealth of information
 - * gluon polarization
 - * single-spin asymmetries
 - * quark polarizations by flavor
 - * orbital angular momenta
 - * . . .
- spin will continue to provide challenges to theory and experiment

High- p_T jets at the Tevatron :



Gluon polarization

- a key contributor to the proton spin ?

- $\langle S_g \rangle = \int_0^1 dx \Delta g(x, Q^2) \propto \frac{1}{\alpha_s(Q^2)}$ in QCD

- some model predictions ($Q \approx 0.5$ GeV) :

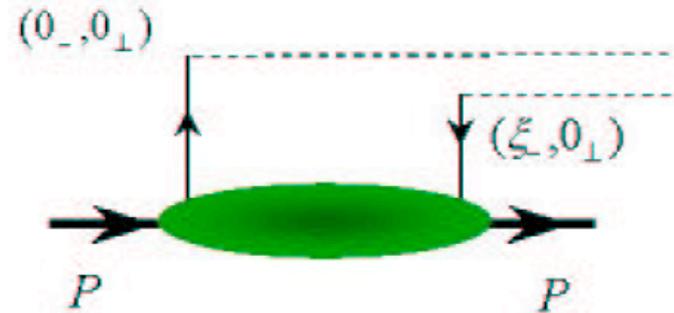
$$\langle S_g \rangle = -0.4 \quad (\text{Jaffe, bag model})$$

$$\langle S_g \rangle = +0.25 \quad (\text{Barone et al., Isgur - Karl})$$

$$\langle S_g \rangle = +0.3 \quad (\text{Rho et al., chiral bag})$$

...

- gauge-invariant parton distributions :

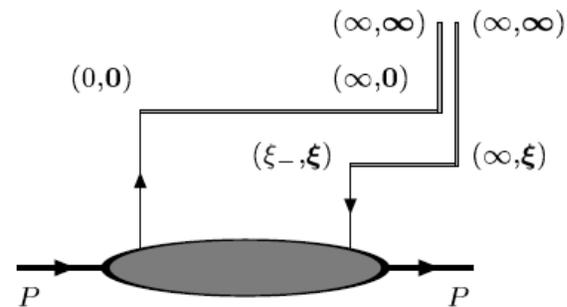


$$q(x) \sim \int d\xi^- e^{i\xi^- x} \langle P | \bar{\psi}_+(\xi^-) U_{[\infty, \xi^-]} U_{[0, \infty]} \psi_+(0) | P \rangle$$

$$U_{[a, \xi^-]} \equiv \mathcal{P} \exp \left(-ig \int_a^{\xi^-} d\lambda A^+(\lambda) \right)$$

- with k_T dependence

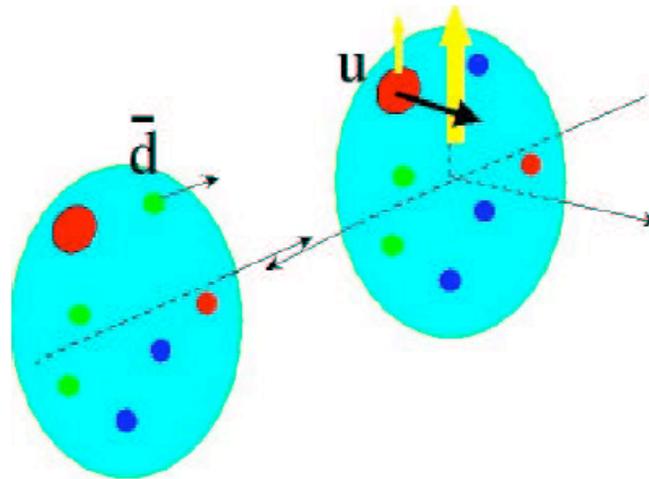
$$q(x, \vec{k}_T) \sim \int d\xi^- d^2\xi_T e^{i\xi^- x + i\vec{k}_T \cdot \vec{\xi}_T} \times \langle P | \bar{\psi}_+(\xi^-, \vec{\xi}_T) \tilde{U}_{[\infty, \xi^-]} \tilde{U}_{[0, \infty]} \psi_+(0) | P \rangle$$



- gauge link survives even in $A^+ = 0$ gauge

(Belitsky, Ji, Yuan; Boer, Mulders, Pijlman)

- a caveat :
 - data on A_N in “borderline pQCD” regime $p_T \sim \mathcal{O}(1)$ GeV
- in “soft regime”, description for A_N could be different : (Boros,Liang,Meng)
- quark-antiquark fusion “on front surface”

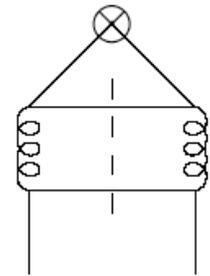


- a crucial feature of the quark singlet :

$$s^\mu \Delta\Sigma = \langle P, S | \underbrace{\bar{\psi} \gamma^\mu \gamma^5 \frac{1}{2} \psi}_{\text{singlet axial current } j_5^{\mu,0}} | P, S \rangle$$

- connection to **axial anomaly** :

$$\partial_\mu j_5^{\mu,0} \equiv \partial_\mu [\bar{\psi} \gamma^\mu \gamma^5 \psi] = n_f \frac{\alpha_s}{2\pi} \text{Tr} [G_{\mu\nu} \tilde{G}^{\mu\nu}]$$

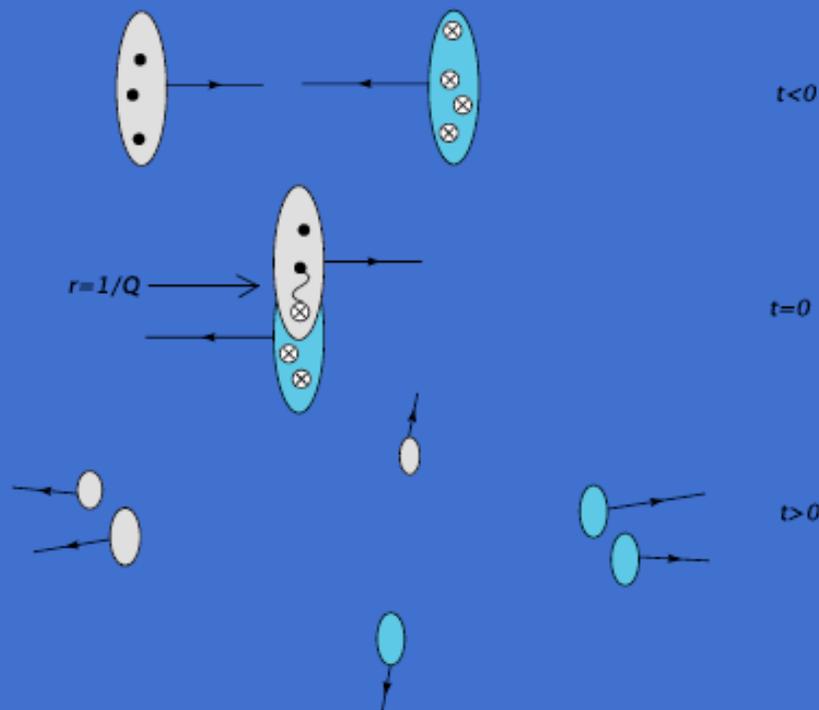


- a consequence (in $\overline{\text{MS}}$ scheme) :

$$\Delta\Sigma(Q^2) = \left(1 + \frac{6n_f}{(33 - 2n_f)\pi} [\alpha_s(Q^2) - \alpha_s(\mu_0^2)] \right) \Delta\Sigma(\mu_0^2)$$

\Rightarrow moderate decrease in perturbative region (Jaffe)

Recall the essence of the parton model:



$$\sigma_{AB \rightarrow X}(Q) = \sum_{ab} \int d\xi_1 \int d\xi_2 \times \phi_{a/A}(\xi_1) \phi_{b/B}(\xi_2) \hat{\sigma}_{ab \rightarrow X}(\xi_1, \xi_2, Q)$$

Key notions:

- i) Lorentz contraction of protons
- ii) Time dilations of dynamics
 → protons are static disks that only “see” each other when they overlap.

Hadronic cross section is weighted sum ($\int d\xi_1 d\xi_2$, ξ_i are momentum fractions) of partonic cross sections.

The parton distributions $\phi_{a/A}(\xi)$

Do classical fields behave like the parton model?

Scalar field at rest, and boosted ($\beta \simeq 1, \gamma \gg 1$)

$$\phi(x) = \frac{q}{|\vec{x}|}, \quad \phi'(x') = \frac{q}{\sqrt{x_T^2 + \gamma^2(t' - z')^2}},$$

Field lines also take pan-cake form!

Gauge field at rest, and boosted ($\beta \simeq 1, \gamma \gg 1$)

$$A^\mu(x) = \frac{q\delta_{\mu 0}}{|\vec{x}|}, \quad A'^0(x') = -A'^3(x') = \frac{q\gamma}{\sqrt{x_T^2 + \gamma^2(t' - z')^2}}$$

Gauge field does *not* die off, but for $\gamma \rightarrow \infty$ takes the form

$$A'^\mu(x') \rightarrow q\partial^\mu \ln(t' - z')$$

But this is gauge transformation of $A^\mu = 0$, so there is no physics in this!