

# GPDs and exclusive processes in $ep/eA$ scattering

Ch. Weiss (Jefferson Lab), EIC Workshop, BNL, July 17–22, 2006

3D quark/gluon  
structure of nucleon

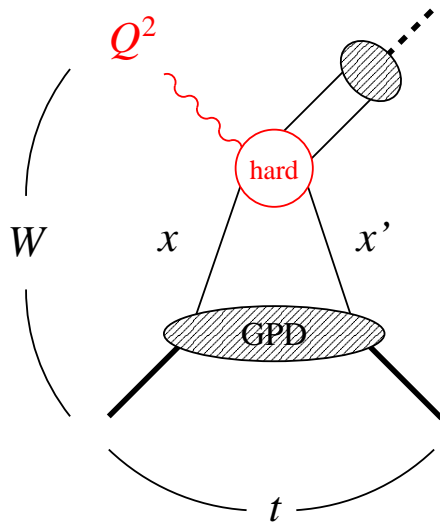
$$f(x, \vec{\rho})$$

longitud.      transverse  
momentum      position

- Quark/gluon imaging of proton
  - Gluon from  $J/\psi, \phi, \rho$  ← HERA
  - Gluon GPD  $\leftrightarrow$  dipole picture
- Exclusive processes in  $eA$ 
  - Coherence length  $\leftrightarrow$  nuclear size
- GPDs in  $pp$  with hard processes
  - Control “transverse geometry”
  - Unitarity limit in central  $pp$  → LHC
  - Diffractive scattering

## Hard exclusive processes in $ep$ : Factorization

[Müller et al. 94; Brodsky et al. 94;  
Collins et al. 96; Radyushkin 96, Ji 96]



- $\gamma^*$  reacts with quasi-free parton emitted/absorbed by target
- Generalized parton distribution  $H(x, x', t)$  universal (process-independent)!

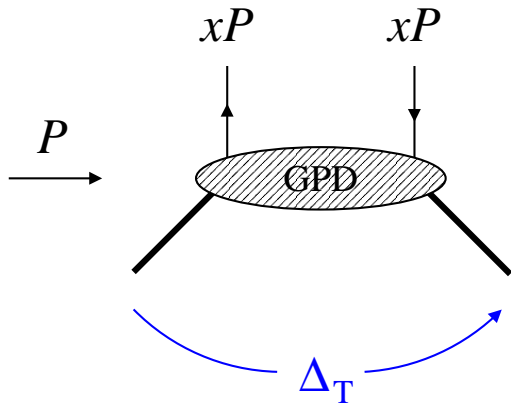
$\gamma^* p \rightarrow \gamma + p$  Deeply virtual Compton scattering

$\gamma_L^* p \rightarrow \rho + p$  Vector meson production

$J/\psi + p$  Heavy quarkonium  $\rightarrow$  gluon GPD

$\pi + p$  pseudoscalar

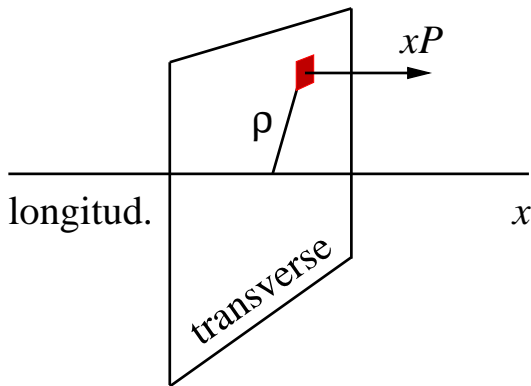
# Transverse spatial distribution of partons [Burkardt 02; Diehl 02]



$$H(x, t) = \int d^2\rho e^{-i\vec{\Delta}_T \cdot \vec{\rho}} q(x, \rho)$$

form factor  
of quarks with  
longitudinal  
momentum  $xP$

transverse spatial  
distribution

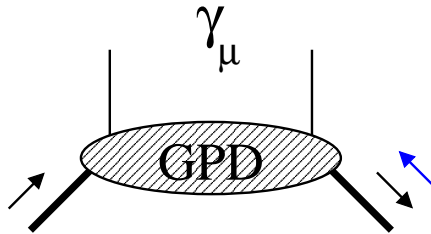


$$\int d^2\rho q(x, \rho) = q(x) \quad \text{total quark density}$$

$$\langle \rho^2 \rangle_q = 4 \frac{\partial}{\partial t} \frac{H(x, t)}{H(x, t=0)} \quad \text{transv. size of nucleon, } x\text{-dependent!}$$

# Quark distributions: Polarization

Quarks unpolarized:



$$= H, \quad E$$

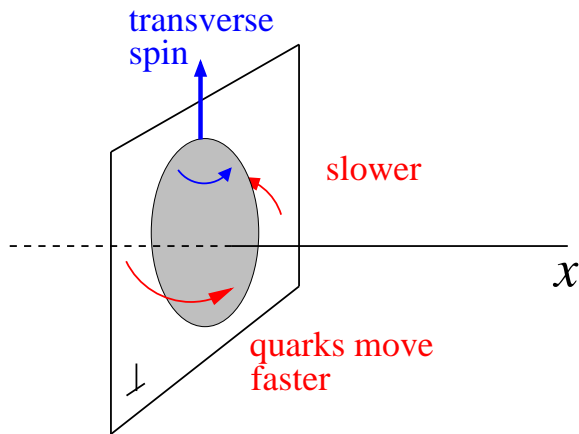
Dirac      Pauli

polarized:

$$\gamma_\mu \gamma_5$$

$$\tilde{H}, \quad \tilde{E}$$

axial      pseudoscalar



$E(x)$  : Distortion of longitudinal motion of quarks due to transverse spin  
 [Burkardt 03]

Also: Operator relations (sum rules), QCD evolution, . . .

## Towards quark/gluon imaging of the proton

- Strong differences between channels: Cross sections, energy dependence

$$\begin{array}{ccccc} J/\psi, \phi & \longleftrightarrow & \rho^0, \gamma & \longleftrightarrow & \pi, K, \rho^+ \\ \text{gluons} & & \text{gluons + sing. quarks} & & \text{non-sing. quarks} \end{array}$$

- DVCS at large  $x$ : Helicity components of quark GPDs from spin asymmetries in  $ep \rightarrow ep\gamma$  [HERMES, JLab 6 and 12 GeV]  
→ Talks by F. Ellinghaus, H. Avakian, A. Sandacz
- Factorization asymptotic statement . . . Need experimental tests of reaction mechanism ( $Q^2, W, t$ -dependence) and solid theory estimates of higher-twist
- Plenty of interesting information local in  $x, t$   
. . . no “fixation” on sum rules!

## Experimental requirements

- Broad range in  $Q^2$  and  $W$
- High luminosity . . . depends on channels → Talk by R. Ent
- Detection of recoil proton
- Accurate  $t$ -measurements for  $|t| < 1 \text{ GeV}^2$  ← beam optics
- $L/T$  separation . . . crucial for understanding reaction mechanism!
- Polarization (DVCS)

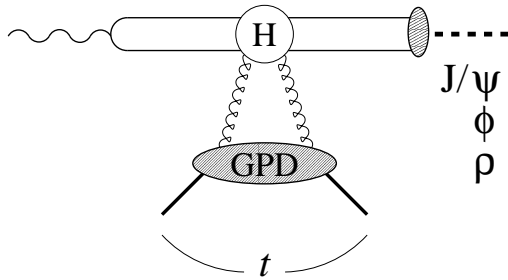
# Part II

## Gluon imaging of proton

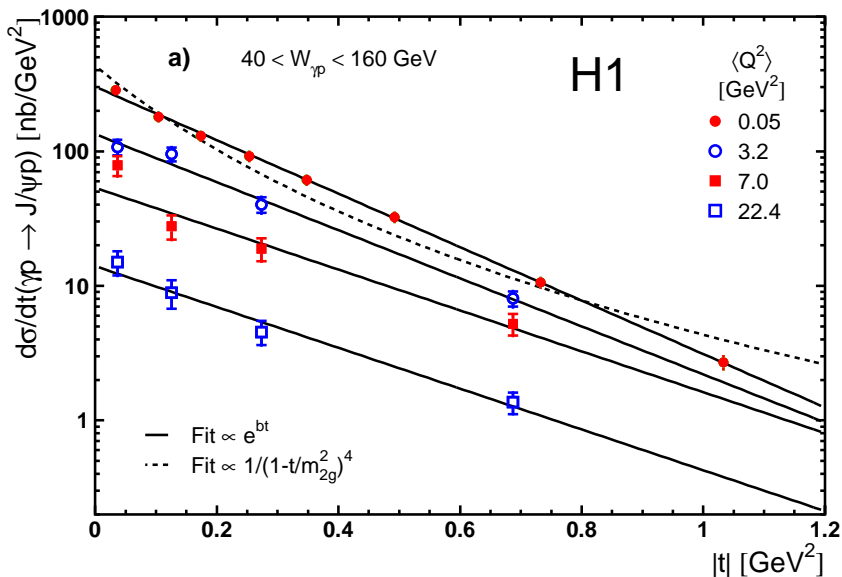
- Feasible! HERA + fixed target data
- Ideas about nucleon structure
- Related to dipole picture at small  $x$

Review: Frankfurt, Strikman, CW, Ann. Rev. Nucl. Part. Sci. **55**, 403 (2005)

# Gluon imaging of proton: $J/\psi$ , $\phi$ , $\rho$ (small $x$ )



- “Universality” of  $t$ -slopes at high  $Q^2$  demonstrates validity of QCD factorization



- $t$ -dependence of differential cross section

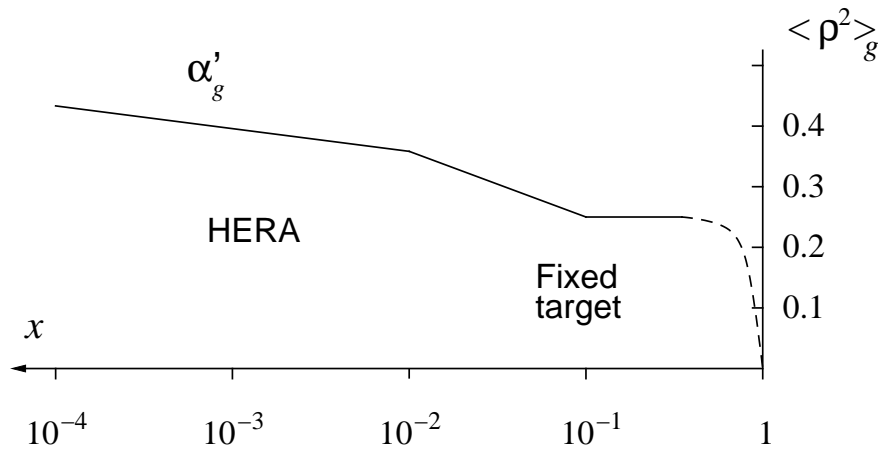
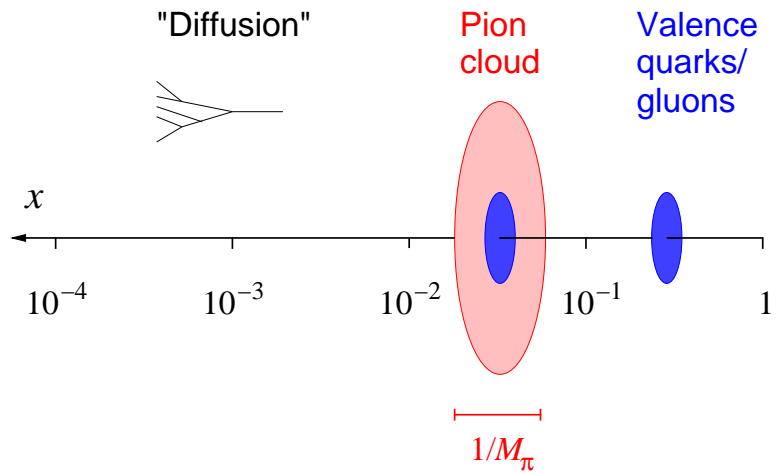
$$\frac{d\sigma}{dt} \propto \left[ \frac{H_g(x, t)}{H_g(x, 0)} \right]^2 \xrightarrow{\text{FT}} \text{spatial distribution}$$

- Also:  $J/\psi$  fixed-target data [FNAL, SLAC, Cornell, CERN]

[HERA H1 2005; see also: ZEUS  
 . . . no recoil detection!]



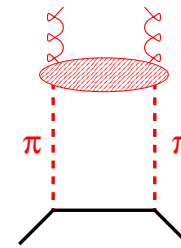
# Gluonic transverse size of proton: $x$ -dependence



(Scale  $Q^2 \approx 3 \text{ GeV}^2$ )

- Gluonic transverse size increases with decreasing  $x$

- Pion cloud contributes at  $x < M_\pi/M_N$  [Strikman, CW 03]



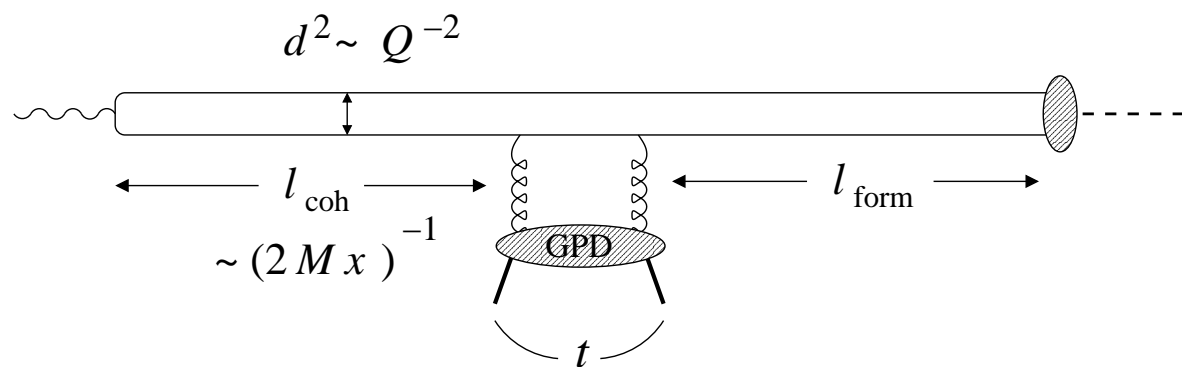
$$G(x, \rho) \sim e^{-2M_\pi \rho}$$

"Yukawa tail"

- Small  $x$ : Logarithmic growth with  $\alpha'_g \ll \alpha'_{\text{soft}}$  ("diffusion")

# Gluon GPD and the dipole picture at small $x$

[Brodsky et al 94;  
Frankfurt, Radyushkin, Strikman 96]



Target rest frame:  
Scattering of  
small-size  $q\bar{q}$  dipole  
from proton

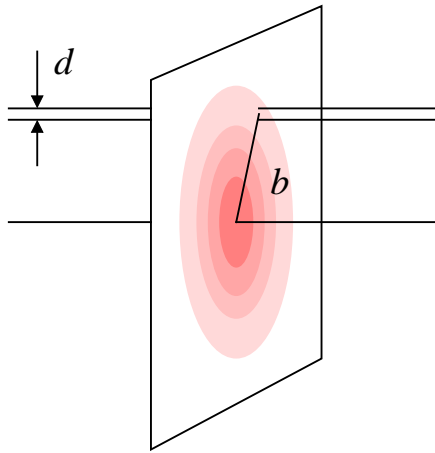
$$A^{dp} \propto d^2 \alpha_s x G(x, t)$$

$$\text{Scale} \approx \pi^2 d^{-2}$$

Dipole-proton  
scattering amplitude  
in leading  $\alpha_s \log Q^2$   
approximation

- QCD factorization  $\leftrightarrow$  “Color transparency”
- Gluon GPD  $\leftrightarrow$  “Color dipole moment” of proton
- Higher twist  $\leftrightarrow$  hadronic size configurations in  $\gamma^*$   $\rightarrow$  Talk by T. Rogers

## Dipole picture in impact parameter representation



- Dipole–proton interaction probes local gluon density in transv. plane  $x G(x, \vec{b})$

- Model–independent formulation of unitarity limit in hard interactions

$$A^{dp}(s, t) = \frac{is}{4\pi} \int d^2b e^{-i\vec{\Delta}_\perp \vec{b}} \Gamma^{dp}(s, b)$$

profile function

$\Gamma^{dp} \rightarrow 1$ : “Black disc limit”

Breakdown of twist expansion

→ Talk by T. Rogers

# Part III

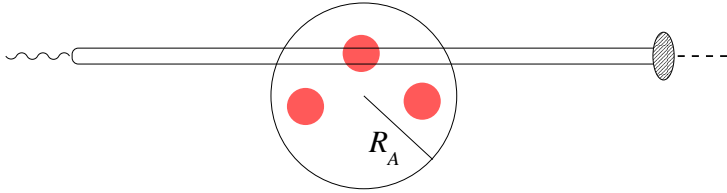
## Hard exclusive processes in $eA$

- New studies of small- $x$  dynamics
- GPDs as new probe of nuclear structure

→ Talk by V. Guzey

# Coherence length vs. nuclear radius

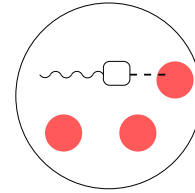
[with M. Strikman]



$$l_{\text{coh}}, l_{\text{form}} \gg R_A$$

Color transparency ( $d \ll 1 \text{ fm}$ )

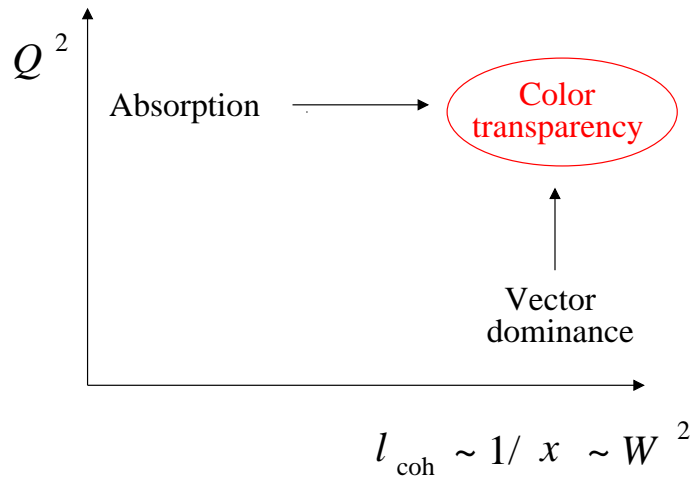
$$\sigma \propto A \quad (\text{incoherent})$$



$$l_{\text{coh}}, l_{\text{form}} \ll R_A$$

Absorption  $\sigma_{\pi N} \rho_{\text{nuc}} R_A \sim 1$

$$\sigma \propto A^{2/3}$$



- Nucleus as “filter” for small-size configurations
- Unique way to explore longitudinal direction in small- $x$  scattering

## Coherent scattering from nuclei

- $A$ -dependence in color transparency regime

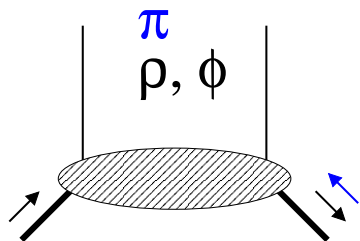
$$\frac{d\sigma}{dt}(t=0) \propto A^2, \quad |t| \propto R_A^{-2} \propto A^{-2/3}$$

- Polarized light nuclei

${}^4\text{He}$  Spin 0 “single GPD”

${}^2\text{H}$  Spin 1  $\Delta S = 2$  component

- Nucleus as “detector” for quantum number transfer



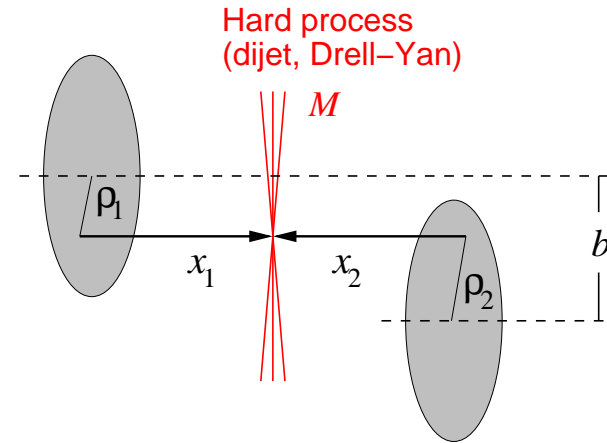
Very different probabilities  
for leaving nucleus intact

# Part IV

## GPDs in $pp$ with hard processes

- Control transverse geometry (impact parameters)
- Trigger for central collisions
- Rapidity gap survival in diffractive scattering

# Hard processes in $pp$ : Impact parameter dependence



$$pp \rightarrow M + X$$

$$\begin{aligned}
 P_{\text{hard}}(b) &\propto \int d^2\rho_1 d^2\rho_2 \\
 &\times \delta(\vec{b} - \vec{\rho}_1 + \vec{\rho}_2) \\
 &\times f(x_1, \vec{\rho}_1) f(x_2, \vec{\rho}_2)
 \end{aligned}$$

- Hard process induced by parton-parton collision

$$x_1 x_2 = M^2/s$$

- Calculate probability as function of  $pp$  impact parameter  $b$  in terms of  $f(x, \vec{\rho})$  known from  $ep$

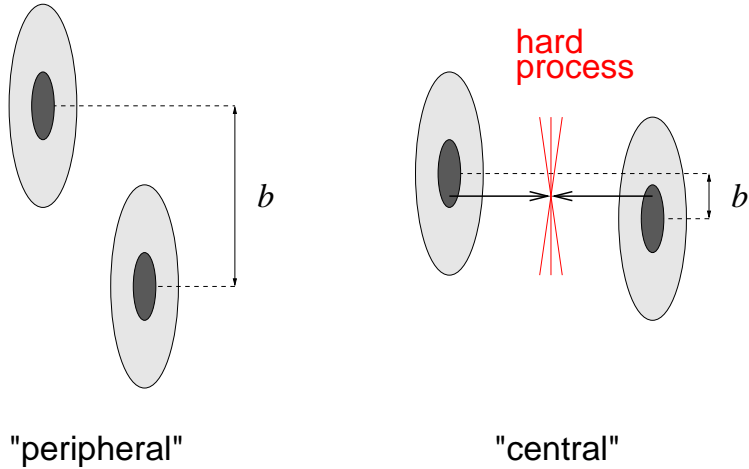
- “Control” impact parameter distribution even though  $b$  not observable!

→ Spectator interactions

→ Global event characteristics



# Hard processes as “filter” for central collisions [Frankfurt, Strikman, CW 03]

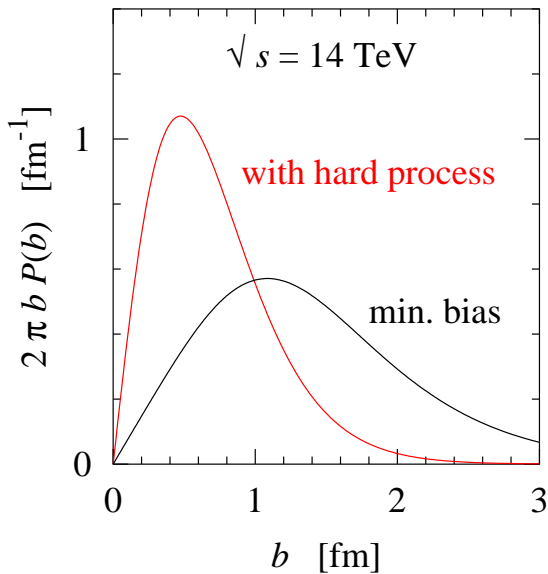


- Different transverse sizes in hard and soft interactions:

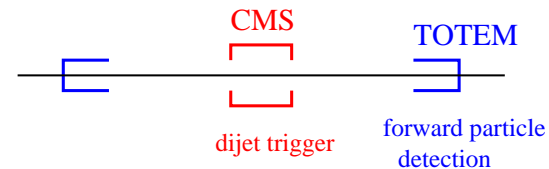
$$\langle \rho^2 \rangle (x \geq 10^{-2}) \ll R^2(\text{soft})$$

- Hard processes (e.g. dijets) as trigger on central collisions

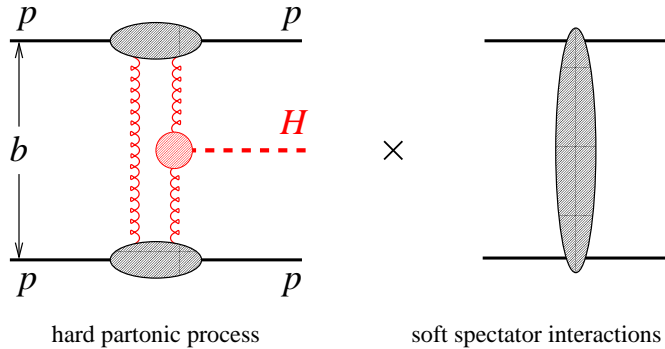
... Numerous applications!



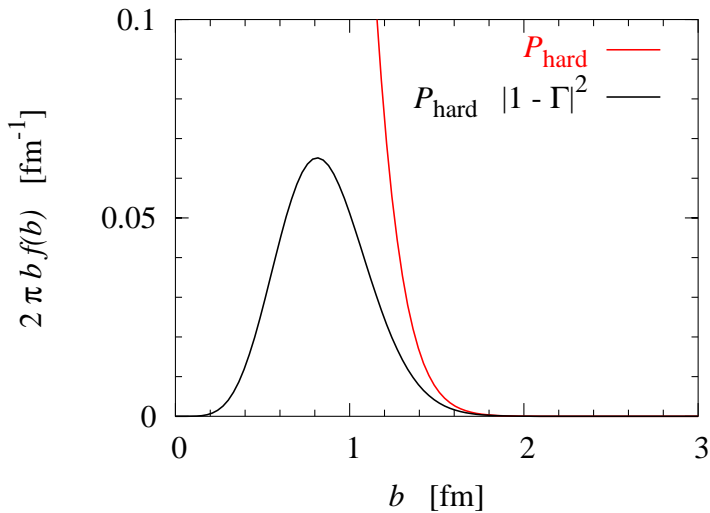
- Central collisions at LHC: Unitarity limit in spectator interactions (“black disc limit”); observable in forward particle production



# Diffractive processes $pp \rightarrow p + H + p$ : Rapidity gap survival



- Heavy particle produced in hard partonic process (2-gluon exchange)
- Soft spectator interactions must not destroy rapidity gaps!



- Gap survival probability

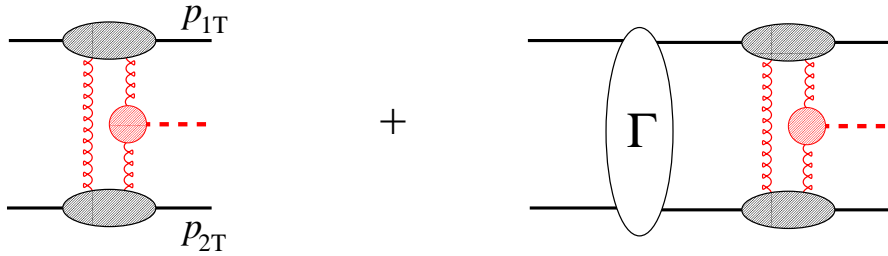
$$S^2 = \int d^2b P_{\text{hard}}(b) |1 - \Gamma(b)|^2$$

$$\approx 0.03 \quad (\text{Higgs at LHC})$$

... calculable, model-independent!

[Frankfurt, Hyde-Wright, Strikman, CW 06]

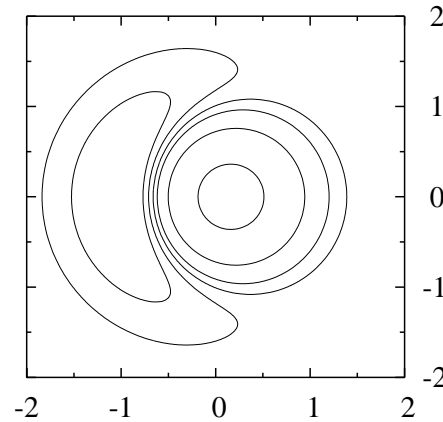
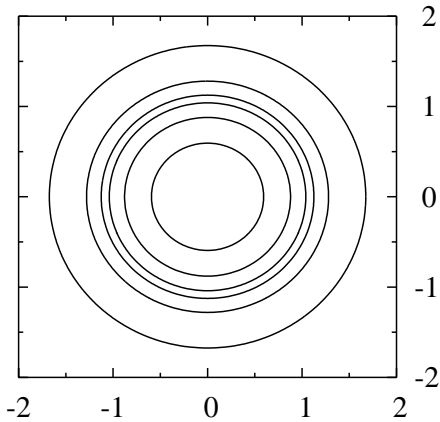
# Diffractive processes: Probing GPDs



- Interference between hard process alone and hard + soft rescattering

$$p'_{1x} = 0$$

0.5 GeV



- Diffraction pattern in  $\vec{p}_{T1}, \vec{p}_{T2}$
- Extract information about gluon GPD!

[Frankfurt, Hyde-Wright, Strikman, CW 06]

## Summary

- $ep/eA$  collider offers unique opportunities for quark/gluon imaging of proton and nuclei in hard exclusive processes

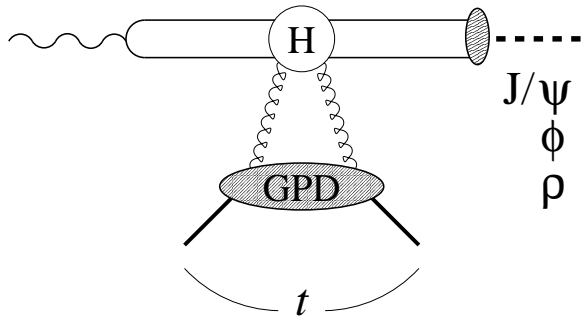
- Large differences between channels/kinematics:  
Need to carefully specify objectives!

gluons at $x < 10^{-2}$	$\longleftrightarrow$	quarks at $x > 10^{-2}$
high energy, moderate lumi		moderate energy, high lumi

- Gluon imaging: Feasible; important for unitarity studies at smaller  $x$
- Nuclei: New ways to explore small- $x$  QCD and nuclear structure
- Interesting “convergence”  $ep \leftrightarrow pp$

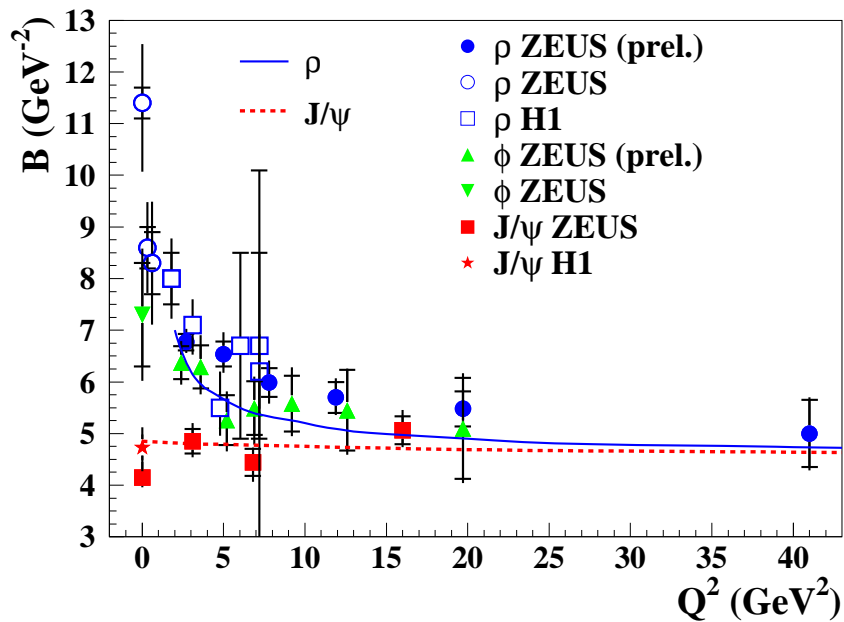
Supplementary material

# Vector meson production at HERA: Tests of factorization

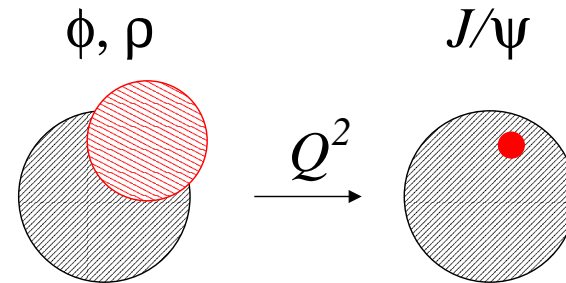


- $J/\psi$  and  $\phi, \rho$  (small  $x$ ) probe gluon GPD

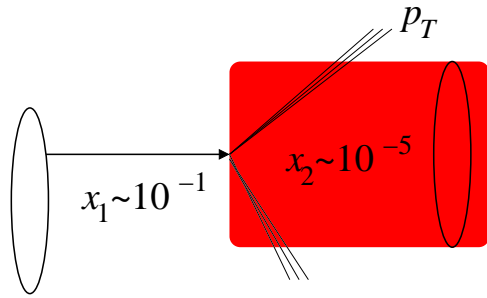
- “Universality” of  $t$ -slopes at large  $Q^2$  shows dominance of pointlike configurations



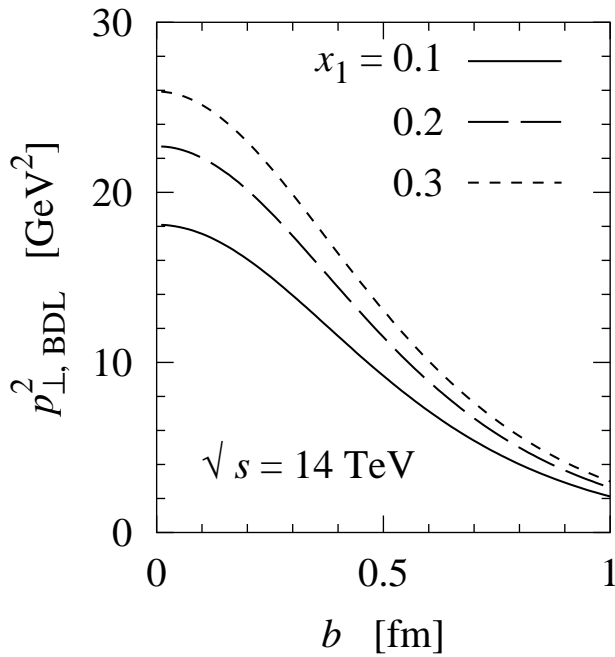
$$\frac{d\sigma}{dt} \propto \left[ \frac{G(x_1, x_2, t)}{G(x_1, x_2, 0)} \right]^2$$



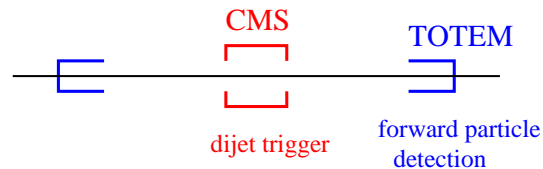
# Central collisions: Unitarity limit in hard spectator interactions



- Increase of gluon density at small  $x$  (DGLAP evolution)
- Interaction of large- $x_1$  spectator with small- $x_2$  gluons approaches “black-disk limit”:  $P_{\text{inel}} \rightarrow 1$



- Qualitative changes in forward particle production: Large  $p_{\perp}$ , energy loss, . . .
- Can be studied with LHC detectors



[Frankfurt, Strikman, CW 03/04]